Mr. Wingate's Arithmetick,

Containing Adams 8.67.14

A PLAIN AND FAMILIAR METHOD,

For attaining the

KNOWLEDGE and PRACTICE

COMMON ARITHMETICK.

The fixth Edition.

First composed by Edmund Wingate late of Grayes-Inne Esquire.

Afterwards upon Mr. Wingate's request, enlarged in his life time: Also since his decease carefully revised, and much improved; as will appear by the Preface and Table of Contents,

By JOHN KERSET, Teacher of the Mathematicks, at the Sign of the Globe in Shandois-street in Covent-Garden.

Boetius Arith, lib, 1. cap, 2. Omnia quecunque à primeva rerum natura construéta sunt, Numerorum widentur ratione formata: Hoe enim fuit principale in animo Conditoris Exemplar,

LONDON,

Printed by T. R. for R.S. and are to be fold by J.Williams in Cross-Keys Court in Little Britain. 1673.

W. Wingare's Arithmetick,

Concerning Address

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By #OHN K.S. L. S.E.Y. Teacher, of the Mathematicks, st the Sign of the Gibbs in Shankois-first in Covent-Garden.

Boerius Arichilib. 1. cap. 2.

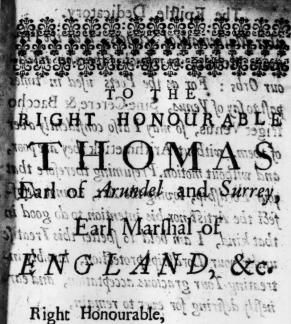
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finate summereum sidement actions formats a stoc enim
fine principale in animo Constraits Exemples.

LONDON,

Princed by 77 R. for R. L. and are to be fold by J. 1974.

Home is Crofs-Reys Court in Little Britain, 1673.



He good affection you bear to all kind of Learning, and in particular to the Mathematicks, makes me adventure to present your Lordship with this Tractate of Arithmetick, because that Art, compared with other EDM. WINGATE

The Epistle Dedicatory.

other Mathematical Sciences, is as the Primum Mobile, in respect of the other inferiour Orbs: For as the Poets used in times past to say of Venus, Sine Cerere & Baccho friget Venus, so may I also considently aver of them, without Arithmetick they are poor, and without motion. Presuming therefore that your Lordship, loving the Art, cannot disaffect the Artist, nor his intention to do good in that kind, I am hold to shelter this Treatise under your Lordships protestion, humbly intreating Your gracious acceptation, and earnestly desiring for ever to remain,

Ile ni erwono Hour Your Honor to all

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EDM. WINGATE

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PREFACE

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JOHN KERSET.



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Bout the year 1629 our learned Countreyman Edmund Wingate Esquire, publish'd a Treatise of Arithmetick divided into two Books, the one intituled Natural Arithme-

k, the other Artificial Arithmetick; and regard his principal delign in that Treatife,

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was

was to remove the difficulties which ordinarily arise in the practice of Common Arithmetick; by the help of artificial, or borrowed numbers, called Logarithmes; (whole proper work is to perform Multiplication by Addition; Division by Subtraction, &c.) he did then in his faid first Book omit divers pieces of Common or Practical Arithmetick, which for the perfect and univerfal understanding thereof, were necessary to have been inferted. But after the first impression of both these Books was spent, our said Author being importuned to take care of the fecond Edition, he promifed his affiftance therein, yet his other necessary employments not permitting him to purfue his faid purpofe, he was pleased to impart his thoughts concerning the fame unto me, together with his request, that I would peruse the faid first Book, and supply it with such pieces of Pra-Itical Arithmetick, which for the reasons aforesaid were wanting in the first Edition.

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In pursuance of which request, I have contributed my Talent rowards perfecting this Tractate, upon our Authors foundation partly in his life time to his good liking, and partly fince his decease, in several Edition

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committed to my care to be prepared for the Press, wherein I have used my best endear yours, as well to preserve this Book as a Monument of our said Authors worth, as also to make it a compleat Store-house of Common Arithmetick; from whence the ingenious may be surnished with the excellencies of that Art, in reference both to common affairs, as also to the practical parts of the Mathematicks. And in order to those ends I have made these following alterations and Additions, namely,

First, for the ease and benefit of such Learners, who defire only so much skill in Arithmetick , as is uleful in Accompts, Trade , and fuch like ordinary employments; the Dodring of whole Numbers? (which in the first Edition was intermingled with Definitions and Rules concerning broken Numbers, commonly called Fractions is now entirely handled apart; and to the end the full knowledge of Practical Arithmetick in whole Numbers might more clearly. appear, I have explained divers of the old rules in the first five Chapters, and framed anew, the Rules of Division, Reduction, and the Golden Rule in the fixth, seventh, eighth, and

and ninth Chapters; so that now Arithmer rick in whole Numbers is plainly and fully handled before any entrance be made into the craggy pathes of Fradions; at the fight whereof fome Learners are so discouraged, that they make a stand, and ory out, non plan ultra, there's no progress further.

defire to lay a good foundation for the attaining of a general knowledge in the Mathematicks, I have in a familiar method delivered the entire Doctrine of Fractions, both Vulgar and Decimal, which was omitted in the first Edition; and have also newly framed the Extraction of the Square and Cube roots, in a method which by experience is found to be much easier then that commonly used heretofore, and is exactly suitable to the Construction or Composition of Square and Cube numbers.

Lastly, I have added an Appendix, which is furnished with variety of choice and delightful knowledge in numbers, both Practical and Theoretical. In all which performances I have earnestly aimed at truth, perspicuity, and exact correction both of

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the Text and Numbers; so that I hope this Book is now supplied with all things necesfary to the sull knowledge and practice of Common Arithmetick, the usefulness whereof is so generally known, that there will be no need of Arguments to excite any one that desires his own or the publick good, to be acquainted with so excellent an Art.

But if the more curious Artist, after he is well exercis'd in vulgar Arithmetick, desires further inspection into the Mysteries of Numbers, his best Guide is the admirable Art called Algebra; the Elements whereof I have expounded at large in a Treatise lately publish'd.

From my house at the sign of the Globe in Shandois-street in Covent-Garden, the 23th day of July, 1673.

JOHN KERSEY.



The Table of Contents.

Where those Chapters of Mr. Wingate's, that have been altered and framed anew by John Kerfey, are distinguished by this mark , and those chapters that have been entirely composed by the said? K. may be discovered by this Asterisk*.

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ging of Vallels * Sports and Pallimes ERRATA	11 499

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Common Arithmetick

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eion propriet Chi Chi con capref. read of

Concerning Notation of Numbers.

Rithmetick is the Art of accompting by Number. As magnitude or greatnesse is the subject of Geometry, so multitude or number is that of Arithmetick.

thing is numbered; or that which an-

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twers to the question, how many? (unlesse the question be answered by nothing:) So if it be demanded, how many dayes are in a week, the answer is seven, which is called Number.

the Charalters
by which number is or Characters, by
which Number is ordinarily expect.
fed, are these; 1 one, 2 two, 3 three,
4 four, 5 five, 6 six, 7 seven, 8 eight,

o nine, o nothing.

IV. These Notes or Characters are either figni-

ficant figures, or a Cypher.

V. The lignificant figures are the first nine; viz. 1,2,3,4,5,6,7,8,9. The first whereof is more particularly called an Unit, or Unity, and the rest are said to be composed of Unities, so 2 is composed of two unities, 3 of three Unities, &c.

VI. The Cyphen lathe last, which though of it felf it signifies nothing, yet being annexed after any of the rest, it increases their value: As will ap-

pear in the following Rules.

VII. Arithmetick hath two parts, Notation and

Numeration.

VIII. Notation teacheth how to express, read, or declare, the signification or value of any number written, and also to write down any number propounded, with proper Characters in their due places.

The places or in the number; viz. when divers figures, whether they be intermixt with a Cypher or Cyphers or not, are placed together like letters in a word, without any point, comma, line, or other note of diffinction interposed.

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t,

. i, pofed, all those Characters make but one number. which consists of to many places as there are Characters fo placed together: fo this number 204 conlists of a places, and this 30600 of five places, &c.

Notation confifts in the knowledge of two things ; viz. the order of places, and the value of

every place in any number. aidion and

XI The order of the places is from the right hand towards the left : So in this The order of number 465, the figure 5 standeth in the number. first place, 6 in the fecond, and 4 in the made and

third, bkewife in this number 7560, a Cypher stands in the first place, 6 in the fecond, 5 in the third, and 7 in the fourth.

XII. The first place of a Number (which as before is the outermost towards the right hand) is called the place of Units or Unities ; in which place ?-

The values of places in any

ny figure fignifieth its own simple value; fo in this number 465, the figure 5 ftanding in the first place fignifieth five Unities, or five.

XIII. The fecond place of a number is called the place of Tens ; in which place any figure fignifieth fo many Tens as the figure containeth unities fo in this number 465 the figure 5 in the first place fignifieth simply five, but the figure 6 in the fecond

place lignifieth fix tens, or fixey con la anatoniq

XIV. The third place of a number is called the place of Hundreds in which place any figure fignia fieth fo many hundreds as there are unities comtain'd in the figure : So in this number 465, the fo gure a in the third place fignifical four hundreds; wherefore if it be required to read or pronounce this number 465, you are to begin on the left hand,

and

and according to the aforefaid rules to pronounce it thus, four hundred fixty five; likewife this number 313 is to be pronounced thus, three hundred and fifteen: and this number 203, two hundred and five; also this number 300, five hundred. Whence it is manifest, that although a Cypher of it self signifies nothing, yet being placed on the right hand of a figure it increases the value thereof, by advancing such figure to a higher place then that wherein it would be seated, if the Cypher were absent.

The true reading or pronouncing the value of any number written, as also the writing down any number propounded, depends principally upon a right understanding of the three first places before mentioned, and therefore I shall advise the Learn) or to be well exercised therein, before he proceeds

to the following Rules, wait seithed an stinil to

W. The fourth place of a number is called the place of Thousands; (that is, any number of Thou fands under ten thousand) the fifth place tens of thousands; the fixth place Hundreds of thousands; the feventh place Millions; fa Million being ten bundred thousand) the eighth place tens of Millions; the ninth place hundreds of Millions; the tenth place thousands of Millions; the eleventh place tens of thousands of Millions; the twelfth place hundreds of thousands of Millions : And in that order you may conceive places to be continued infinitely from the right hand rowards the left, each following place being ten times the value of the next preceding place, but to give names to them would be both a troublefome and an unnecefthis number 465, you are to begin on the kartyral

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XVI. From the rules aforegoing, an easie way may be collected to read or express the value of a Number propounded, Viz. Let it be re- A brief way of Notation. quired to read or pronounce this

number 521426341, First, Distinguish by a Commajor point, every three places, beginning at the right hand, and proceeding towards the left, fo will the aforefaid number be distinguished into parts, which may be called Periods,

and stand thus 321, 426, 341. where

you may note the first period towards

the right hand to consist of these figures 341, the fecond of these 426. and the third of these 521. condly, read or pronounce the figures in every Period as if they stood apart from the rest, so will the first Period be pronounced three hundred forty one, the second four hundred twenty fix: and the third five hundred twenty one. Thirdly, to every Period except the first towards the right hand, a peculiar denomination or sirname, is to be applyed, Viz. the sirname of the second Period is Thousands; of the third, Millions; of the fourth, Thousands of Millions, &c. Therefore beginning to pronounce at the highest Period, which in this Example is the third, and giving every Period its due firname, the faid number will be pronounced thus, Five hundred twenty one Millions; four hundred twenty fix Thousands, three hundred forty one.

Note, When a number is distinguished into Periods, as before, the highest Period will not always compleatly confift of three places, but sometimes of one place, and fometimes of two, nevertheless after such Period is pronounced as if it stood apart, the due sirname is to be annexed; so this

number 3204689. after it is divided into Periods, will stand thus, 3,204, 689. and to be pronounced thus, Three Millions, two hundred and four thousands,

six hundred eighty nine.

XVII. The aforesaid Rules for the right pronouncing or reading of a Number which is written down; being well understood, will sufficiently inform the Reader how to write down any number propounded to be written.

The Table of Notation.

1 ne 1	able of	Notat	lon.
 S.C. S.C. S.C. Twelfth place 3 Hundreds of Thouland Millions. Fleventh place 2 Tens of Thouland Millions. Tenth place 1 Thouland Millions.	9 Hundreds of Millions. 8 Tens of Millions.	6 Hundreds of Thonfands. Tens of Thonfands.	3 Hundreds. 2 Tens. 1 Unite.
CTwelfth place 3 Hum. Eleventh place 2 Tens Tenth place 1 Thon	Third Period, Bighth place 9 Hundreds	Second Period, Fifth place S	100
Fourth Period,	Third Period,	Second Period,	First Period,

Notation of Numbers by Latine Letters.

Top I was the state of the state of	211XXI.
2 II.	30 XXX.
3 III.	40 XL.
4 HIII. or thus IV.	49 XLIX.
	50 L.
6 VI. and same	59 [LVIIII. or thus LIX.
7 VII. ONDE SOLIDITAV	60 LX.
8 VIII. or thus IIX.	89 LXXXIX.
	100 C.
	20c CC.
	300 CCC.
12 XII.	400 CCCC.
18 XVIII. or thus IIXX	500 D. or thus ID.
19 XVIIII.or thus X1X	
20 XX.	700 DCC. or thus IOCC.

1000 CID. or thus M. 2000 CID. CID. 3000 CID. CID. CID. 5000 IDD.

50000 1000.
1000000 CCCCI. 2020.
1000000 CCCCI. 2020.
1672 CIDDCLXXII. or MDCLXXII.

CHAP. II.

Concerning English Moneys, Weights, Measures,

I. The things expressed by Numbers are principally, Money, Weight, Measure, Time, and things accompted by the dozen: Of the three first of these, there are infinite kinds and varieties according to the diversity of the several Common-wealths in which they are used, all which here to produce were both endlesse and needlesse: wherefore we intend here to treat only of such Moneys, Weights, Measures, &c. as are used in this Nation, being indeed only necessary for our present purpose.

II. The least piece of money used in England is a Farthing, from whence this follow. Money.

ing Table is produced.

I. Farthing) (I. Farthing
4. Farthing:	(makes) 1. Penny.
12. Pence	(Shilling.
20. Shillings) (1. Pound.

English (or sterling) Money is ordinarily written down with Figures after this manner,

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The first Rank of the faid Numbers signifies thirty four pounds, thirteen shillings, five pence, two farthings : the fecond Rank expresseth nine pounds, five shillings, ten pence, one farthing : the third Rank, fix pounds, no shillings, fix pence, three farthings, &c.

III. The smallest Weight used in England is a grain, that is, the weight Vide Statut. of a grain of Wheat well dried and de compositione gathered out of the middle of the ponderum, ear, whereof thirty two make another weight called a Penny weight, and twenty Penny weight make an

Ounce Troy.

Here observe, That by the Statutes quoted in the Margent, the weight of 31 Ed. 1. v. two and thirty grains of Wheat make Raft. weights, a penny weight, which weight being 76 3.12 Hen. once discovered by two and thirty fuch grains, the faid penny weight (being the twentieth part of an ounce Troy) is usually subdivided into four and twenty parts only, called also Grains, as appears by the ensuing Table.

A Table of Troy Weights. Troy Weight (24 Artificial Grains.

32 Grains of Wheat) 24 Grains) I Penny Weight. make 20 Penny Weight) I Onnce.

12 Ounces (1 Pound Troy.

Trey Weight is ordinarily written down with Figures after this manner.

> -05 -13 -- 13 00 --- 11 --- 07 -co - co - of - 20 B 3

The

The first rank of the said numbers expresset feventeen pounds, sive ounces, thirteen penny weight, thirteen grains, of Troy weight: the second rank, no pounds, eleven ounces, seven penny weight, six grains: and the third, no pounds, no ounces, sive penny weight and twenty grains.

Now this Troy weight ferveth only to weigh Bread, Gold, Silver, and Ele-Malynes lex Mercat. pag. ctuaries. And here observe also by the 49. way, that Troy weight regulateth and Malynes ib. prescribeth a form how to keep the pag.252. Money of England at a certain Standard. For about two hundred years before the Conquest, Osbright a Saxon, being then King of England, caused an ounce Troy of Silver to be divided into 20 pieces, at the same time called Pence; and fo an Ounce of Silver at that time was worth no more than twenty pence, or one fhilling eight pence, which continued at the same value until the time of Henry the fixth, who (in regard of the inhanling of Moneys in Forrain parts) valued the fame at thirty pence, fo that then there were accordingly thirty pieces made out of the Ounce, and the old pieces went then for three half pence, until the time of Edward the fourth, who valued the Ounce at forty pence, and then the old pieces went for two-pence a piece. After this, Henry the eight, valued the Ounce of sterling Silver at forty five pence, which value continued until Queen Elizabeths time, who valued the same old pence at three-pence the piece, fo that all Three-pences coined by the same Queen, weighed but a penny weight, and every Six pence two penny weight; and fo in like manner the Shilling and other pieces accoraccordingly; which made the Ounce Troy of Silver to be valued at fixty pence or five shillings, as it now remains at this day without alteration.

IV. The Weights used by Apothecaries are derived from a pound Troy Apothecaries which is subdivided as in the follow. Weights.

ing Table.

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A Table of Apothecaries Weights.

1b. A Pound Troy
3 An Ounce
3 A Dram
4 A Scruple
5 A Scruple
7 A Scruple
8 Drams.
9 A Scruple
10 Grains.

So that if you were to express in Figures 12 pounds 10 ounces, five drams, two scruples, and 16 grains; also three pounds, five ounces, seven drams, one scruple, and two grains, the ordinary way to write them down is briefly thus,

V. Besides Troy weight before mentioned, there is another kind of weight used in England, called Averdupois weight, a pound whereof is equal unto 14 Ounces, twelve penny weight Troy. This Averdupois weight serveth to weigh all kind of Grocery Ware, as also Butter, Malynes ib. p. Cheese, Flesh, Tallow, Wax, and every 49. other thing which beareth the name of Garbel, and whereof issues the results or waste.

VI. Averdupois weight is either greater or lefs.

VII. The greater is, when one hundred and twelve pounds Averdupois Averdupois are considered as one entire weight greater weight

B 4 commonly

commonly called an hundred weight, and then such hundred weight is subdivided first into sour quarters, and each quarter into eight and twenty pounds: again, each pound into sour quarters, or (if you will be more exact) into 16 Ounces, and if you please each Ounce into sour quarters. But ordinarily a pound is the least quantity that is taken notice of in Averdupois gross weights.

A Table of Averdupois greaten Weight.

28 pounds 4 quarters and ake an bundred weight, or 112 lb.

So that if you were to express by Figures eight hundred, three quarters, and five pounds; likewise, seven hundred, one quarter, and seventeen pounds: the ordinary way to write them down is briefly thus,

Averdapois is, when a pound is the highest name lesser weight. or Integer, each pound being subdivided into sixteen ounces, and each ounce again into 16 drams, and if you please, each dram into 4 quarters, as by the subsequent Table is manifest.

A Table of Averdupois lesser Weight.

4 Quarters of a Dram	7 (I	Dram.
16 Drams	make :	1	Ounce.
16 Ounces	5 6	1	Ounce. Pound.

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So that if you were to express by Figures eighteen pounds, twelve ounces, five drams, and three quarters of a dram; likewise five pounds, no ounces twelve drams, and one quarter of a dram, the ordinary way to write them down is briefly thus,

03. dr. 16. 18 — 12 — 05 — 3 05 — 00 — 12 — 1

IX. The measures used in England are either of

Capacity or Length.

X. The measures of Capacity are those which are produced from Weight, and they are either Liquid or Dry.

XI. The Liquid measures are those, Liquid Mes-

in which all kind of Liquid substances fures: are measured, and they are expressed in

the Table following,

A Table of Li	iquid Measures.
i Pound of Wheat	r I Pint.
Troy weight	
2 Pints	I Quart.
2 Quarts	I Pottle.
2 Pottles	1 Gallon.
8 Gallons	1 Firkin of Ale,
The state of the s	Sope Herring
9 Gallons	1 Firkin of Beer.
9 Gallons 10 Gallons and an	1 Firkin of Salmon
balf	or Eels.
2 Firkins	1 Kilderkin.
2 Kilderkins	1 Barrel.
42 Gallons	1 Tierce of Wine.
63 Gallons	I Hogshead.
2 Hogsbeads	1 Pipe or But.
2. Pipes or Buts	I Tun of Wine:
	VIII

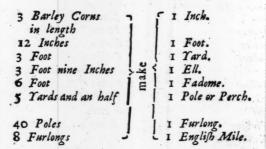
XII. Dry

XII. Dry Measures are those, in Dry Measures. which all kind of dry substances are meted, as Grain, Sea-coal, Salt, and the like; their Table is this that follows.

A Table of Dry Measures.

1 Pinte	7 [I Pinte.	
2 Pintes	1 Quart.	
2 Quarts	I Pottle.	
2 Pottles	I Gallon.	
2 Gallons	I Peck.	
4 Pecks	Bushel land measur	e.
S Pecks	E I Bushel water measure	6.
8 Busbels	1 1 Quarter.	
4. Quarters	I Chalder.	
5 Quarters	J 1 Wey.	

Long Mea- XIII. Long Measures are exprest in this Table following.



Note, That a Yard, as also an Ell, is usually subdivided into four Quarters, and each Quarter into four Nails.

XIV. Super-

XIV. Superficial or square Measures of Land are fuch as are exprest in the Land Mea-Table following.

45 Square Poles make I Rood or an Acre. (I Rood or quarter of

So that if you would express by Figures these quantities of Land, Viz. Thirty fix Acres, three Roods, twenty Perches: also seven Acres, no Roods, thirty two Perches, the ordinary way to write them down is thus.

--0--

XV. A Table of Time is this that follows.

I Minute I Minute. 60 Minutes I Hour. 24 Hours I Day natural. 7 Dayes I Week. I Moneth of twenty 4 Weeks C13 Moneths eight dayes. I Year very near. I Day, & 26 Hours

But in ordinary computations of time, the whole year confishing of three hundred lixty five dayes, is divided either into twelve equal parts or moneths, each moneth then containing thirty dayes and ten hours : or else into twelve unequal Kalender moneths, according to the ancient Verse.

Thirty dayes bath September, April, June, and November :

February hath twenty eight alone, and each of the rest thirty one. Note.

Note, That every Leap-pear (which happeneth once in four years) containeth three hundred fixty fix dayes, and in such year February con-

taineth twenty nine dayes.

of things accounted by the
dozen, a Gross is the Integer consisteounted by the
ing of twelve dozen, each dozen containing again twelve particulars: so
that if you would express in Figures, seven Gross
four Dozen, and five particulars; also four Dozen and eight particulars, they may be briefly
written thus.

G. D. P. 7 — 04 — 05 0 — 04 — 08

CHAP. III.

Addition of whole Numbers.

I. Concerning notation of Numbers; and how thereby the quantities of things are usually exprest, a full Declaration hath been made in the preceding Chapters; Numeration ensueth, which comprehends all manner of operations by Numbers.

II. In Numeration, the four primary or fundamental operations (commonly called Species) are these, Addition, Subtraction, Multiplication,

and Division.

III. Addition is that by which divers Numbers are added together, to the end that their fum, aggregate, or total, may be discovered.

IV. In Addition, place the Numbers given,

one

0

y

one above another in fuch fort, that like places or degrees in each number Addition of may stand in the same rank : that is Units above Units, Tens above Tens, Hundreds above Hundreds, &c. So these numbers 1213 and 462 being given to be added together, you are to order them as you fee in the margent.

numbers of one denomination

462

V. Having thus placed the Numbers, and drawn a line under them , add them together , beginning with the Units first, and faying thus, 2 and 3 make s, which write under the Rank of Units, then pro-

ceed to the fecond Rank and fay 6 and 1 make 7, which write under the fecond Rank (being the place of tens) again 4 and 2 make 6, whichwrite under the third Rank. Laftly, write down I being all that stands in the

1213 462 1675

2315

7423

141

fourth Rank, fo the fum of the faid given Numbers is found to be 1675, and the operation will stand as in the Margent.

In like manner the Numbers 2315, 7423; and 141, being given to be added together, their fum will be found to be 9879, and the operation thereof

will stand as you fee in the Example. VI. When the fum of the Figures of any of the Ranks amounts unto ten, or any number of tens without any excess, write down a Cypher under that Rank, but when the fum of any Rank exceeds ten or any number of tens, write down the excess under fuch Rank, and for every ten contained in the fum of any Rank , referve an Unite or I in your mind, and add fuch Unit or Units to the Fi-

gures

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G. D. P. 7 — 04 — 05 0 — 04 — 08

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one

-

1213

1675

462

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V. Having thus placed the Numbers, and drawn a line under them, add them together, beginning with the Units first, and saying thus, 2 and 3 make 5, which write under the Rank of Units, then pro-

ceed to the second Rank and say 6 and 1 make 7, which write under the second Rank (being the place of tens) again 4 and 2 make 6, which write under the third Rank. Lastly, write down 1 being all that stands in the

fourth Rank, fo the fum of the faid given Numbers is found to be 1675, and the operation will stand as in the Margent.

In like manner the Numbers 2315,
7423; and 141, being given to be added together, their sum will be found to be 9879, and the operation thereof

will stand as you see in the Example. 9879

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gures

gures of the next Rank towards the left hand; fo the Numbers 4937, 9878, and 394 being given to be added together, the opera-4937 tion will be thus, viz. beginning with 9878 the Rank of Units, I fay 4, 8 and 7 394 make 19, wherefore I write down 9; 15209 the excess above 10, and carrying I in mind instead of the ten contained in the faid 19. I fay 1 and 9 (9 being the first figure of the fecond Rank) make 10, which added to 7 and 3, the other figures of the same Rank, the whole sum of them is 20, wherefore fetting down a Cypher under the line in that Rank (because the excess above the two tens is nothing) I carry 2 to the third Rank, and fay 2 and 3 (3 being the first figure of the third Rank) make 5, which being added to 8 and 9 (the other figures of the same Rank) the sum of them is 22, wherefore writing down 2 (being the excesse above the two tens) under the line, in the third Rank, I carry 2 in mind (because there were two tens in 22) to the fourth Rank, and fay 2 and 9 make 11, which added to 4 makes 15, this 15 because it is the sum of the last Rank I write totally down under the line, on the left hand of the Figures before subscribed, fo the fum of the three Numbers given is found to be 15200, as in the Example.

Addition of ded to be added, do expresse things of divers denominations, you must begin with the least denomination first, and when the sum of any of the denominations amounts unto an Integer or Integers of the next greater denomination, add such Integer

or Integers to those of the next greater denomination, on the left hand; so these several sums 24l - 13s - 5d - 3f. Also 12l - os - 8d. and 5l - 18s - 2f, being propounded to be added, their total sum is 42l - 12s - 2d - 1f. For having written them down orderly according to the 2d. Rule of the 2d. Chapter, and drawn a line underneath, I begin with the Farthings first, and say, two Farthings and three Farthings make five Farthings, that is, one Penny with a Farthing over and above; wherefore setting down 1 under the denomination of Farthings, I carry one Penny to the denomination of Pence, then I say 1,8, and

five Pence make 14 Pence, which contain one shilling and two Pence, wherefore writing two under the denomination of Pence, I likewise carry 1 shilling to

the denomination of shillings: Then adding the faid I shilling unto 18 shillings and 13 shillings, the sum will be found I pound and 12 shillings, wherefore fetting down 12 under the denomination of shillings, I carry I pound in mind unto the denomination of pounds faying, I pound in mind, together with 5,2, and 4 pounds which stand in the first Rank of pounds; make 12 pounds, wherefore (according to the fixth Rule of this Chapter) I write 2, the excess above 10, underneath the faid first rank of pounds, and carry I in mind for the faid 10 to the fecond Rank of pounds, then saying in like manner, I in mind, together with 1 and 2 which stand in the fecond Rank of pounds make 4, which I write underneath

derneath the line, that done, I find the total of the three fums propounded to be 42 1.-12 s.-2 d.-1f:

In like manner 3 lb. -05 oz _19 p. w. 15 gr. Alfo 2 lb. -0 oz. -3 p. w. -7 gr. Alfo 0 lb. - 10 oz. -6 p. w. And 0 lb. -9 oz. -0 p. w. -17 gr. being given to be added together, their fum will be found to be 7 lb. -1 oz. -9 p. w. -15 gr. and the work will stand thus.

16.	02.	p.w.	gr.
03 -	- 05 -	19~	
02 -	- 00-	-03-	- 07
00 -	-10-	06_	- 00
00 -	_ 09 -	00-	-17
-		-	
07-	-31-	- 09_	-15

Note, In adding together the Numbers in the last Example, it must be remembred that 24 grains make one Penny weight, also 20 Penny weight make one ounce, and 12 ounces make one pound Troy, as before declared in the second Rule of the second Chapter.

More Examples of this Rule are these following.

Addition of English Money.

1b. s. d. f. l. s. d.

230 17 10 1 0 13 09

175 12 11 3 0 17 08

052 05 06 0 0 00 10

009 00 08 1 0 10 03

506 13 00 2 0 15 06

974 10 00 3 2 17 08

Ghap. III.	f whole Numb	ers.	21
Addit	ion of Troy Wes		4
16. oz. p.w.		p.w.	·or
23-07-16-	-13 53	613-	16
17-10-15-	-07 20	8-11-	
325-06-19-	-20 06	3 10-	
49-11-07-	-12 09	00-	
417-00-19-			
C. 9. 235 3 576 1 628 2 412 0	17 05-	0z. —13— —10— —00—	<u>-14</u> -06
852 3	10 06-	09 02	
e da il addenion,	f Measures of	ap ball	สาร์อ์ธนา
	11 99 11	9.	. s.
yards. q. n.	alls Ells		
yards. q. n. 26—3—2	15-	3	-2
26—3—2 13—1—3	15-	3 1	-3
26—3—2 13—1—3 12—0—1	15—	3 1 0	-3 - I
26—3—2 13—1—3	15— 16— 109— 12—	3 1	-3 - I

333

Addition of Superficial Measures of Land.					
Acres.	Roods	Per.	A.	R,	P.
136-	3	-13	240-	2	17
	<u> </u>			3-	13
212-	2	10	- 249-		36
517-	-0-	00	006 -		10
1379-	3	09	996-	3 -	:6

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CHAP. IV.

Subtraction of whole Numbers.

I. Subtraction is that by which one number is baken out of another, to the end that the remainder, or difference, between the two numbers given may be known.

II. The number out of which the Subtraction is

Subtrattion of numbers of one denominato be made, must be greater, or at least, equal with the other. As you may Subtract, 4347 or 9478 out of 9478, for can you not subtract 9478 out of 4347.

numbers one under the other as in Addition, with this caution, that the number placed uppermost may exceed or at least be equal unto the other: So if the number 4347 be given to be subtracted from 9478, I order them as in the Margent: then proceeding to the subtraction, I say,

7, taken out of 8, there remains one, which I place in the fame rank under the line. In like manner 4 being taken out of 7, the remainder is 3, which

likewise I set under the line in the next rank, again taking 3, from 4, the remainder is 1, which I likewise place under the third rank, lastly subtracting 4 from 9, there will remain 5, which I subscribe under the fourth rank, so the whole operation being sinished I find, that if 4347 be taken out of 9478 the remainder is 5131, or (which is the same) the difference between the

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numbers 9478 and 4347 is 5131 as in the example. In like manner if 106 be subtracted from 2856 the remainder will be found to be 2750; for after the numbers are orderly ranked I begin at the place of Units, and fay 6 from 6, there remains nothing, wherefore I subscribe o. then 2750 proceeding to the fecond rank I fay if o (or nothing) be taken from 5, there will remain , which I also subscribe under the line, again I from 8, there remains 7; lastly o from 2, there

remains 2. See the work in the Margent.

IV. When any of the figures of the number given to be fubtracted is greater than the upper figure out of which it is to be fubtracted, you must borow to of the next rank towards the left hand and add the faid to to the faid upper figure, then the figure of fuch next rank which is to be fubtracted must be efteemed an unite greater than it is ; wherefore in this cafe, keeping one in your mind add it to the next figure of the number given to be subtracted, and deducting all out of the figure above it, proceed in like fort till you have finished the whole operation. Example, let it be required to Subtract 374 out of 8023. Having ranked them as before, I fay four out of 3, that cannot be, wherefore borrowing ten of the next rank and adding the same to the said 3, I say 4 out of 13, there remains o, then writing ounder the line, and carrying 1 in my mind, I fay 1 and 7 make 8, 8 out of 2 that cannot be, but 8 out of 12/12, because 10 being bor-374 rowed, and added to 2, makes 12) there remains 4, which I subscribe under the

7649

line

line, again I in my mind being added to 3 makes 4, 4 out of nothing, that cannot be, but 4 out of 10 there remains 6 which I likewise subscribe under the line; lastly 1 in my mind being taken out of 8 there remains 7, thus you see that the remain-der after 374 is subtracted from 8023 is 7649. Note diligently, that as often as 10 is borrowed, 1 must be kept in mind to be added to the figure standing in the next place of the lower number, and the fum of fuch Addition must be subtracted from the upper place; but if it happen that there is no figure in the next place of the lower number, then the I in mind must be subtracted from the upper place, (as in the last rank of the last Example) Another Example. Let it be required to fubtract 92 from 62801. Having placed the greater number uppermost and the lesser orderly un-

derneath, I begin at the place of units, 62801 and fay, 2 from I I cannot take, but

borrowing 10, and adding it to the
faid 1, I say 2 from 11, there refazog mains 9, which I subscribe under the

line, then I proceed and fay, r in mind with 9 makes 10, 10 out of 0 I cannot take, but borrowing 10 I fay 10 out of 10 and there remains 0, wherefore I subscribe 0 under the line; again, 1 in mind out of 8, there remains 7; then because there are no more Figures in the lower number I say 0 out of 2 there remains 2; lastly, 0 out of 6 there remains 6; therefore I conclude

that 62801 exceeds 92 by 62709.

Subtraction of numbers of diners denominations, place wers denominations, them as before, and beginning with nations.

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the least denomination first , subtract the lower number from the upper when it may be fubtracted, and place the remainder underneath; but if it happen that the lower number cannot be taken out of the upper, you must borrow an integer of the next greater denomination on the left hand; which integer after it is converted into the same denomination with the faid upper number must be added to it: then from the fum of fuch Addition you are to subtract the lower number and write down the remainder, keeping I (that is the integer borrowed) in your mind to be added to the next place of the number given to be subtracted, as before : so 901.-14s.-10d.--3f. being subtracted from 1241,-115,-7d. -1f. the remainder is 331. -16s. -8d. -2f. For beginning with the farthings, I fay, 3 farthings out of I farthing I cannot take where- 1. 124-11-07-1 fore borrowing 1 penny (that

is an integer of the next grea- 90-14-10-3 ter denomination) and having converted this

33-16 08-2

makes

peny into four farthings, I add them to the aforesaid 1 farthing, so the sum is five farthings, out of which fubtracting 3 farthings there remains 2 farthings, which I place underneath the denomination of farthings, then I proceed to the next denomination, and fay, 1 penny which I borrowed and 10d. make 11d, this 11d. out of 7d I cannot take, wherefore borrowing I shilling or 12d. and adding 12d. to the faid 7d the fum is 19 d. from which I fubtract the faid 1 1d. fo there remains 8d. which I subscribe under the denomination of pence; again a shilling which I borrowed being added to 14s.

makes 15s, which I cannot subtract out of 11 s and therefore I borrow I pound or 20s. which being added to the faid 11s. makes 31s. from which Subtracting 15s. there remains 16s. which I subscribe under the denomination of shillings, then carrying I pound which I borrowed to the lower place of pounds, I fay I in mind with o makes I. which taken out of 4 there remains 3, again 9 out of 2, I cannot take, but 9 out of 12 (10 being borrowed and added to the faid 2 according to the fourth Rule of this Chapter) and there remains 3. laftly 1 (for the 10 that was borrowed) being taken out of 1, there remains nothing, and fo at last I find that if A. being indebted to B. in 1241-11s. -7d - If. hath paid in part thereof 901.-14s. - 10d. - 3f, there remains yet undischarged 33%. -16s, -8d. -2f.

VI. When many numbers are given to be subtracted from a number propounded, you must first add those numbers together, according to the rules of the third Chapter, and then

the fum found is to be subtracted from the number first propounded. Example, A. being indebted to B. in 3240l. paid thereof at one time 700 l. at a second payment 1236 l. and at a third 305 l. the

1. 3240 The Debt.

700 Payments. 305 Payments. 305 Total payd

999 Rest unpayd.

question is how much of the debt remained undischarged? First, I add together the sums paid, and find the total to be 2241 l. this I subtract from 3240l. so there remains 999 l. undischarged as you see by the operation in the Margent.

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Another Example of -00 The Debt. like nature. A. being indebted to B. in 500/ 340-12-067 paid in part thereof 13-18-03 Payments: at one payment 340 1 -12s. -- 06 d. at a fecond payment 131 372-07-07 Paid in all. - 18s. - 3d. at a 127-12-05 Rest unpaid. third 174 -- 16s. 10d. the question is how much was in arrear ? Here if the operation be prosecuted as before, it will appear that there was 127 l. -12 s, -05 d. unpaid, fee the work in the Margent.

VII. Addition is proved by subtraction, and subtraction by Addition. For having added divers numbers together, if you subtract one of them

The proof
of Addition
and subtraction.

out of the fum, the remainder must be equal to all the rest, as you may observe by the Example following, viz. supposing these 4 num-

bers are given to be added, viz.
236, 452, 29, 217. and that
their fum is found to be 934
(by the Rules of the 3d. Chap.)
it is required to prove whether the faid fum be true or
not; to perform this I draw a
line under the uppermost num-

452 934 29 236

236

698

217 698

ber 236, to seperate it from the

rest, and seek the sum of all the numbers given, except that uppermost, which sum I find to be 698. Then I subtract the said uppermost number 236 from 934 (the total sum of all the numbers first sound) and because the remainder 698 is the same

C4

with

with the sum of all the numbers excluding the uppermost, I conclude that the sum of all the numbers first found was truly computed.

In like manner is Subtraction proved by Addition, for if you add the remainder, and the num. ber given to be subtracted together, the sum

must be equal to the Example 1 Example 2 number out of 1. s. d. which the Subtration of 9478 24—13—07 ction is made; so if subtr. 4347 19—15—08 4347 be subtracted Rest 5131 04—17—11 from 9478 the re-Proof 9478 24—13—07 mainder is 5131,

for if 5131 be added to 4347, the sum is 9478, which is the same with the number out of which the Subtraction was made. Again, if a Servant receive 241. ——135. ——7d. and lay out of disburse 191. ——155. ——08d. there must remain in his hands 41. ——175. ——11d for this being added to 191. ——155. ——08d. which was the Money he expended, the sum will be equal to 241. ——135, ——07 d. (being the Mony wherewith he was first charged.)

More Examples of Subtraction are thefe that

Subtraction of English Mony.

	1 1 1			1	111111111111111111111111111111111111111	
	i. s. d.	f. 1	1.	5.	d.	f.
Bec.	3090-10-07	1	24	00-	00-	-0
paid	0099-14-08	-3	05-	17-	11-	- 3
	2993-15-10		18-)2	00-	
proof	3090- 10-07		24			
					C	ash is

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Subtraction of Trey Weight.

Subtraction of Averdupois Weight.

	C. 9.	16.	16.	oz.	'dr.
Bought	256-2-	-23	25-	-13-	12
Sold	0793-	-26	00-	-14-	-13
	1762-		24-	-14	-15
Proof	256-2-		25 -	-13-	-12

Subtraction of Superficial Measures of Land.

	Acres, Roods, Perches	A.	R.	P.
Bought	780-2-35	2040-	-1-	-20
Sold	090-3-36	919-	_3-	-30
Rest	689-2-39	1120-	-1-	-30
Proof	780-2-35	2040	-1-	-20

Questions to exercise Addition and Subtraction.

Quest. 1. Two persons, A. and B. owe several debts, the lesser debt being that of A. is 3045l. the difference of their debts is 104 l. what is the debt of B? Answer, 3149 l.

Quest.

Quest. 2. Two persons A. and B. are of several ages, the age of the elder, being that of A. is 70, the differences of their ages is 19, what is the age of B? Answer \$1.

Queft. 3. What number is that which being ad-

ded to 168 maketh the fum to be 205? Anf. 37.

Queft. 4. The sum of two numbers is 517, the

leffer is 40, what is the greater ? Auf. 477.

Quest. 5. A certain person born in the year of our Lord 1616, desires to know his age in the year

1672, what was his age ? Auf. 56.

Quest. 6. The greater of two numbers is 130, their difference is 49, what is the lesser number? Answ. 81:

CHAP. V.

Multiplication of whole numbers.

I. Ultiplication teacheth how by two numbers given to find a third, which shall contain either of the numbers given, so many times as the other contains 1 or unitie.

II. Of the two numbers given in Multiplication, one (which you will) is called the Multiplicand, and the other the multiplicator (or both are called Fa-

ctors.)

III. The number fought, or arising by the multiplication of the two numbers given is called the product, the Fact, or the Rectangle: fo if y be given

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given to be multiplied by 3, or 3 by 5, the product is 15, that is 3 times 5, or 5 times 3 makes 15: and here 5 may be called the Multiplicand, and 3 the Multiplicator, or 3 may be called the Multiplicand, and 5 the Multiplicator 5 and as 3, (one of the two numbers given) containeth 1 or unity thrice, fo 15 the product containeth 5 (the other given number) thrice; likewife as 5 (one of the given numbers) contains unity 5 times, fo 15 (the product) contains 3 (the other given number) five times.

IV. Multiplication is either single or compound.'

Single multiplication is, when plication. the Multiplicand and Multiplicator consist each of them of one only figure as in the last Example; In like manner if you multiply 9 by 5, the product is 45, this is likewise single multiplication: now the several varieties of single multiplication are well express in the Table following, usually called Pythagoras bis Table.

The Table of Multiplication:

		1 100	2 11000	9 212				-
1	2	3	4	5	6	7	8	9
2	4	6	8	10	12	14	16	18
3	6	9	12	15	18	21	24	27
4	8	12	16	20	24	28	32	36
5	10	15	20	25	30		40	45
6	12	18	24	30	36	42	48	54
7	14	21	28	35	42	49	56	63
8	16	24	32	40	48	56	64	72
9	18	27	36	45	54	63	72	81

The use of the Table is this, having one figure

given to be multiplied by another to know the product of them, find the multiplicand in the top of the Table, and the multiplicator in the first Column thereof towards the left hand; this done, in the angle of polition just against those two figures you shall find the product. So 9 being given to be multiplied by 5, I find 9 in the top of the table, and 5 in the first column towards the left hand, then carrying my eye from 5 in a right line equidistant to the upper side or top line of the Table, until I come to that fquare which is directly under 9, I find 45, which is the Product required. The particular varieties of this Table ought to be learned by heart, (that is a man must be able to give the Product of any fingle multiplication without the least pause or stay) before he can readily work compound multiplication, as will farther appear hereafter.

Compound VI. Compound multiplication is, Multiplication. when the multiplicator and multiplication. cand either one or both confift of more figures than one.

VII. In compound Multiplication, when the numbers given do end with fignificant figures, place them as in Addition and Subtraction. So 134 be-

ing given to be multiplied by 2, place them 34 thus: then proceeding to the multiplication

2 fay thus: two times 4 is 8, which write un268 der the line in the rank of your multiplying
figure; again, fay two times 3 is 6, which likewise
write under the line in the next rank, Lastly, two
times 1 is 2, which being likewise written down
under the line in the next rank, the Product is discovered to be 268, and the work will stand as in
the Margent.

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VIH. When the multiplicator consists of more figures than one, as many figures as it hath, fo many feveral products must be subscribed under the line, which at last being added into one sum, gives you the total product of all. So 1232 being given to be multiplyed by 23, the operation thereof will stand thus, for 1233 being 1232 multiplied by 3 (according to the 23 last rule) the product is 3696. Again, 3696 1232 being multiplied by 2, the pro-2464 duct is 2464, which several products, 28336 after they are placed in their due order (that is, the first figure arising in 1321 each product under his respective mul-123 tiplying figure) and added together 3963 produce 28336, the product required : 2642 In like manner 1321 being given to be 1321 multiplied by 123, the product is 162483 162483, and the operation will stand

as you fee in the Margent. IX. When the product of any of the particular figures exceeds ten, place the excess under the line as before, and for every ten that it so exceeds, keep one in mind to be added to the next Rank.

Example, 3084 being given to be 3084 multiplyed by 36, the work will stand 36 thus; for 6 times 4 being 24, I write 4 under the line, and referve 2 in mind 18504 for the two tens, then I lay 6 times 8 9252 is 48, unto which if I add 2 kept in 111024 mind, the whole is 50, wherefore fub-

fcribing o in the next rank under the line (o because there is no excess of 50 above 5 tens) I referve 5 in mind for the 5 tens; again, I fay 6 times nothing

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nothing is nothing, to which adding & that I kept in mind, the whole will be but 5, which I likewise fubscribe under the line in the next rank ; again, 6 times 3 is 18, which fin regard 3 is the last figure of the multiplicand) I write wholly down, fo that the particular product arising from the multiply. ing figure 6 is 18504 : in like manner proceeding with the multiplying figure 3, the particular product arising will be 9252. Lastly, these several products being placed in due order, and added to. gether (after the manner of the 8th. Rule of this

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Chapter) will give 111024, which is the total product arising from the multiplica-5073 tion of 3084 by 36, and the operation 256 will stand as in the Margent. After the same manner if 5073 be given to be multiplied by 256, the product will be 25365 found to be 1298688, and the operation

1298688 will ftand as you fee in the Example. X. When the two numbers given to be multiplyed, do one or both of them end with a Cypher or Cyphers towards the right hand, multiply the fignificant figures in both numbers, one by the other, neglecting such Cyphers, and when the multiplication of the fignificant figures is finifhed, annex on the right hand of the number pro-

duced by the multiplication, the Cypher or Cyphers with which one or 43100 both of the numbers first given did end, 15000 fo will the whole give you the true 2155 product demanded : Example, 43100 43 I being given to be multiplied by 15000 646500000 the product will be found to be 646500000, for omitting the Cyphers which stand

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in the last places towards the right hand as well in the multiplicand as the multiplicator, I multiply the significant figures 431, by the figures 15 (according to former rules) so there will arise 6465, to which annexing on the right hand all the Cyphers before omitted, the true product will be \$46500000: more Examples hereof are these following.

43125	5108000
1500	125
215625	25540
43125	10216
64687500	5108
e danie divis ob l	638500000

XI. When in the multiplicator, Cyphers are included between fignificant figures, multiply by the faid fignificant figures, neglecting fuch Cyphers or Cypher, but observe diligently to fer the particular products of the fignificant figures in their due places, according to the 8th rule of this Chapter. So if 563 24 be given to be multiplied by 20006, I first multi-96324 ply the whole multiplicand 56324. 20006 by 6, and place the product orderly 337944 underneath the line, then paffing 112648 over the three Cyphers, I multiply 1126817944
56324 by 2, and place 8 (which is the first excels of this particular product) directly under the multiplying figure '2, and the reft in their order, so at last the true product will be found to be 1126817944, and the work will stand as you fee in the Example. More

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More Examples bereof are thefe that follow.

3094	23765 10302
104	47530
12376	71295
3094	23765
321776	244827030

Note, That one of the principal cautions to be observed in Multiplication, is the due placing of the particular products arising by each multiplying figure, and that may be performed either by taking care to place the first figure or Cypher which ariseth in each product under the respective multiplying figure; or at least the first place arising in the second product must stand under the second place of the first product, and the first place of the third particular product under the third place of the first, &c.

XII. When a number is given to be multiplied by a number that confifts of 1 (or an unit) in the first place towards the left hand, and a Cypher or Cyphers on the right hand of such unit (such are 10, 100, 1000, 10000, &c. the multiplication is performed by annexing the Cypher or Cyphers of the multiplicator at the end (to wit on the right hand) of the multiplicand; so if 326 be given to be multiplied by 10, the product is 32600, if by 100, the product is 326000, in like manner if 170 be multiplied by 10 the product is 1700, if by 100, 17000, &c.

XIII. When more numbers than two are given to be multiplied one by the other, that kind of Multiplication

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is called Continual, and is thus performed Viz. first multiply any two of the numbers given one by the other, then multiply the product by another of the numbers given, and this product by the fourth number given (if there be fo many) and in that order till every one of the given numbers hath been made a Mul-18 tiplicator, fo the last product is the true product required. Ex-72 prod. I. ample, If 4, 18, and 22 were gi-22 ven to be multiplyed continu-144 ally, first 18 multiplyed by 4 144 produceth 72, which multiplied

by 22 (the third number) pro- 1584 Prod.2 duceth 1584, the last product or number required; see the work in the Margent. The proof of Multiplication is by Division as will appear by the next

Chapter.

CHAP. VI.

Division by whole numbers.

I. Division is that by which we discover, how often one number is contained in another, or (which is the same) it sheweth how to divide a number propounded into as many equal parts as you please.

II. In Division there are always three remarkable numbers which are commonly called by these names, the Dividend, the Divisor, and the Quotient.

III. The Dividend is the number given to be di-

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IV. The

IV. The Divisor is the number by which the dividend is to be divided; that is, it is the number which declareth into how many equal parts the di-

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vidend must be divided.

V. The Quotient is the number arising from the division, and shewesh one of the equal parts required: so if 15 were given to be divided by 5, or into 5 equal parts, the number arising, or one of the equal qurts will be 3, for 5 is found three times in 15: And here 15 is the Dividend, 5 the Divisor, and 3 the Quotient.

Division by a VI. Division being the hardest lefsingle Figure. son in Arithmetick, must be heedfully

intended by the Learner, for whose ease I shall use my utmost endeavours to make the way smooth by Rules and Examples, beginning with the easiest first, which will be in that case when the Divisor consists of one figure only; for example, Let it be required to divide 192 by 8, or 192 pounds into 8 equal parts or shares; here 192 is the Division and the Quotient or one of the equal parts is sought.

VII. Place a crooked line at each end of the Dividend, that on the left hand ferving for the place of the Divisor, and that on the right for the Anotient; then if the Divisor be a single figure, subscribe a point under the first figure of the Dividend towards the lest hand, if such first figure be either equal unto, or greater than the Divisor,

but if such first figure be less than the What the Divisor, put a point under the next dual is.

place of the Dividend; which number

8) 192 (fo distinguished by the point may be called the Dividual; so in the example given

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given in the 6 Rule, 192 being the Dividend, and 8 the Divisor. I subscribe a point under 9, not under 1, because it is less than the Divisor. This done the Dividual, or number whereof the question must

be asked, is 19.

VIII. Having thus prepared the numbers, ask now often the Divisor is contained in the Dividual. and write the number which answers the question in the Quotient, then multiply the Divisor by the number placed in the Quotient, and subscribe the product underneath the Dividual. Lastly, having drawn a line under the product, subtract it from the Dividual and subscribe the remainder orderly anderneath the line : So demanding how many times the Divisor 8 is found n the Dividual 19, the answer is two 16 times, wherefore I write 2 in the Quotient, then multiplying the Divisor 8

by 2 (the number placed in the Quotient) the product is 16, which I subscribe orderly under the Dividual 19, and after a line is drawn underneath the product 16, I fubtract it from the Dividual 19, and

place the remainder 3 underneath the line.

1X. Put another point under the next place of the Dividend towards the right hand, and bring down the Figure or Cypher standing in that place to the remainder ; that is, fet it next after it, fo the whole will be a new Dividual: Thus a point being placed under 2 which stands in the next place of the Dividend, I write 8) 192 (2. 2 next after (to wit, on the right hand 16 of) the remainder 3, fo is 32 a new: Dividual, or number whereof the fecond question must be asked, & the work will stand as you fee in the example.

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X. A new Dividual being fet apart, renew the question and proceed according to the 8th. Rule of this Chapter. Thus demanding how often the Divisor 8 is found in the Dividual 32, the answer is four times, wherefore I write 4 in the Quotient, then multiplying the Divisor 8 by four (the figure 8) 192 (24 last placed in the Quotient) the product is 32, which I subscribe under the Dividual 32, and after a line is drawn underneath, I subtract the product 32 from the Dividual 32, and there being

no remainder I subscribe o under the line, so the whole work being finisht, the Quotient is found to be 24, and the operation stands as you see in the Example, wherefore I conclude, if 192 pounds be equally divided amongst 8 persons, the share of each person will be 24 pounds.

A second Example, Let it be required to divide 936 pounds into 9 equal parts, having distinguished the first Dividual by a point (according to the 7th. Rule of this Chapter) I demand how often 9) 936 (1 the Divisor 9 is found in the Dividual 9, and finding it once contained in it,

I write I in the Quotient, then multioplying the Divisor 9 by 1, the product is 9, which I subscribe under the Dividual 9, after this, a line being drawn under the product 9, I subtract it from the Dividual 9, and there being no remainder, I place o underneath the line, as you fee in the Example.

Again, placing a point under 3 which stands in 9) 936 (10 the next place of the Dividend, I transcribe the said 3 next after the remainder 0, for a new Dividual, then asking

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how often the Divisor o is contained in the Dividual 3, and not finding it once contained therein, I write o in the Quotient, and now because the product which ought to arise from the Multiplication of the Divisor by o (the Cypher last placed in the Quotient) amounts to 0, the Dividual 3, out of which that product should have been subtracted, remains the same without alteration; wherefore after a point is subscribed under 6 the next place of the Dividual 3, so there will be a new 9) 936 (104 Dividual, to wit, 36; then deman-

Dividual, to wit, 36; then demanding how often the Divisor 9 is found in the Dividual 36, the answer will be 4 times, wherefore I place

4 in the Quotient, and multiplying the Divisor 9 by 4, the product is 36, which I subscribe under, and subtract from the Dividual 36, so the remainder is 0, thus the whole work being sinisht, the Quotient is found to be 104, as you see in the Example; wherefore I conclude if 936%, be divided equally amongst 9 persons, the share of each will be 104%. In like manner if 296163 be divided by 7 the Quotient will be 42309.

The whole work of Division is The substance of briefly contained in this following division by what we the discover.

Verle.

Dic quot, multiplica, subduc, transferque secandum. Or thus,

First you must ask how oft, in Quotient answer make.

Then multiply, subtrast, a new Dividual take.

XI. When in the Division the Acompendicus Divisor consists of a single Figure way of dividing onely, the Quotient may be written by a fingle figure.

down,

down, and all the operation performed in mind, without writing down any part thereof; fo 82506 being given to be halfed or divided into two equal parts, the work will be thus, The Divifor 2 is found in 8, four times; in 2, once; in 5, twice; and there will remain 1, which 1 being supposed to stand before the Cypher makes 10, then I say 2 is found in 10 five times; and last of all in 6 three times; so that the true Quotient or one half of the

given number 82506 is found to be 41253.

In like manner if \$2506 be given to be divided by 3 or into 3 equal parts, the 3) 82506 (27502 work will be thus, the divifor 3 is found in 8 twice & there will remain 2, which 2 being supposed to stand before (to wit, on the left hand of) the following 2 makes 22, then I fay 3 is found in 22,7 times; in 15,5 times, in o not at all; and laftly in 6, twice; fo that the true quotient or one of the 3 equal parts required is 27502. the same manner may division be wrought by any fingle figure, without much charge to the memory. A Note, concerning the Note, here the Learner may ask remainder after the what shall be done with the last Division is ended, if remainder, if any happen, when any happen. the Division is finished? For a full

answer to this, I refer the Reader to the Note in the fifth Rule of the seventh Chapter; yet I shall here propound an example where the said case happens, viz. Let it be required to divide 351 by 8, or 351 pounds equally amongst 8 persons; now if the opera-

tion be profecuted according to the former rules, the Quotient will be 8) 351 (43 found to be 43, and after the Division

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is finisht there will remain 7, that is, each person must have 43 pounds and there will be an overplus of 7 pounds, which must be also divided equally among the 8 persons, but that cannot be done till the 7 pounds be reduced into shillings, and then those shillings must be divided by 8 to give every person his due share of the shillings contained in the said 7 pounds; again, if there yet remain any surplusage of shillings, they must be reduced to pence, which must also be divided by 8 to give every person his due share of pence, so that when this question is fully answered each persons share will appear to be 43 1.—17 s.—6 d. But how the before mentioned Reduction is performed will be made manifest in the sith rule of the next Chapter.

XII. When the divisor consists of pivision by two, three, or how many places soever or more figures, the operation is more difficult than the first and eathe former, but depends upon the same first method. grounds, and therefore the learner being well vers'd in the preceding method of dividing by a single figure, will the more readily understand these that follow, which are two, whereof the first is the easier, but the latter more expeditious, and that which indeed is principally to be aimed at: For an example of the former, let it be required to divide 4112772 by 708, or (which is the same) to divide

4112772 into 708 equal parts.

First, a Table is to be made to shew at first sight any Multiple or product of the Divisor, it being taken twice, thrice, or any number of times under ten, so having first written down the Divisor it self 708, and drawn a line on the right hand thereof, I place I on the right hand of the line directly

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against

The Divisor. 708 1 against the Divisor; then un-14162 derneath the Divisor 708 I fubthe double thereof 2124 3 fcribe 2832 4 which is 1416, and place the 354c s figure 2 directly against the 4248 6 said double, to wit, on the o-49567 ther fide of the line. Again 56648 adding 1416 (to wit the dou-6372 ble of the Divisor) to the Divifor it felf 708, the fum is 2124 for the triple of the Divisor,

this triple I subscribe under the double and place 3 on the other side of the line right against the triple; Again adding 2124 (the triple of the Divisor) to the Divisor 708 I find 2832, for the quadruple of the Divisor, which quadruple I subscribe under the triple, and proceeding in like manner, at last the Table is finisht, which readily shews the Divifor, with the duple, triple, quadruple, quintuple, (extuple, septuple, ostuple, and noncuple of the Divisor.

Now for a proof of the faid Table, adding the last number thereof to wit 6372 (which was found to be nine times the Divisor) to the Divisor 708 I find the sum to be 7080 which (by the 12th. Rule of the fifth chap.) is evidently ten times the Divilor. wherefore I conclude that the Table is true, in regard that the last number thereof is derived from

all the superiour numbers.

The Table of Multiples or Products of the Divifor being thus prepared, write down the dividend on the right hand of the Divifor, then diftinguish by a point so many of the formost places of the dividend towards the left hand as are either equal in value (being considered apart) to the Divisor, or which

which being greater	70811)	4112772 (5809
yet come nearest to the		3540
value thereof, thus I	21243-	
subscribe a point under		5727
2, thereby fetting apart		5664
4112, being the fewest of the formost places		6372
which will contain the		6372
Divisor 708, so is 4112	63729	. 0

the dividual, (or num-

ber whereof the first question must be asked) then demanding how often the Divisor 708 is contained in the dividual 4112, the answer will be found by the Table to be five times, for looking in the Table I cannot find the dividual exactly, but I fee that 6 times the Divisor is the next greater than the dividual 4112, and five times is the next leffer; wherefore I write 5 in the quotient and the number in the Table which stands against 5, to wit, 3540 I fubscribe under the dividual 4112, then having drawn a line underneath, I fubtract 3540 (which is five times the Divisor) from the dividual 4112, and subscribe the remainder 572 underneath the line; that done, I put a point under the next place of the dividend towards the right hand, and because the figure 7 stands in that place, I transcribe 7 next after the remainder 572, fo there is 5727 for a new dividual.

Then demanding how often the Divisor 708 is contained in the dividual 5727, the answer will be found by the Table to be 8 times, for looking in the Table 1 find that 9 times the Divisor is the next greater, but 8 times is the next lesser than the dividual, wherefore I write 8 in the quotient, and

the number in the Table which stands against 8, to wit, 5664 I subscribe under, and subtract from the dividual 5727, placing the remainder 63 underneath the line.

Again, I put a point under the next place of the dividend, where I find the figure 7, and therefore transcribing 7 next after the remainder 63, the new dividual will be 637; then demanding how often the Divisor 708 is contain'd in the dividual 637, and not finding it once contain'd therein, I write o in the quotient, and since in this case (that is, when a cypher answers the question) the dividual remains the same without alteration, the figure or cypher standing in the next place of the dividend is to be transcribed after the dividual for a new dividual, so writing 2 next after 637, the new dividual is 6372, wherefore demanding how often the Divisor 708 is contain'd in 6372, I find by the Table it is contain'd in it 9 times, wherefore writing 9 in the Quotient, and placing the number which stands against 9 in the Table, to wit, 6372 under the dividual 6372, and subtracting it from the dividual there will remain o. Wherefore I conclude if 4112772 be divided by 708, or into 708 equal parts, the true Quotient or one of the equal parts

Diviso	r. 188	1)	
9.	376	2	20304 (10
Mustiples of the Divisor	564	3	188
O	752 940	+ -	
fth	1128	6 -	1504
3	1316	7	1504
tipl	1504		0
Tut	1692	9	
7			1 1

required is 5809.

In like manner if 20304 be divided by 188, that is into 188 equal parts, the quotient ariling or one of those equal parts will be 108, and the operation will stand as you see, The

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The preceding method of Division by the help of a Table of the Multiples or Products of the Divisor, as it is most easie, so in some Cases, namely, where the Divisor is great, and a Quotient of many places is required, as in calculating Tables of Interest, Astronomical Tables, and such like it excells all other wayes of Division, both in respect of certainty and expedition, but for common practice it is too tedious, and therefore I shall proceed to the choicest practical method.

XIII. I now come to the last and principal method of Division, when the Divisor consists

The latter and choiof many places, which to such as have cest practical method
the Table of Multiplication by heart of Division, when the
will not be difficult; for example,

let 56304 be a number given to many places.

be divided by 184, that is, into 184 equal parts, and the Quotient or one of the equal parts is re-

quired.

First, distinguish by a point (as before) so many of the formost places of the dividend towards the left hand as are either equal in value (when they are consider'd apart) to the Divisor, or else which being greater, yet come nearest unto it, thus I subscribe a point under the figure 3, thereby fetting apart 563, being the fewest of the formost places which will contain the Divi-184) 56304(for, fo is 563 the dividual, or number whereof the first question muit be asked. Having thus prepar'd the numbers. I demand how often the Divisor 184 is contained in the dividual 563, and fince to answer this question and such like, there is a necessity of tryal, it will be requisite to shew how this tryal may fitly be made . first, therefore

fore compare the number of places, in the dividual. with the number of places in the Divifor, and when the number of places is the same in both, let it be asked how often the first or extream figure of the Divisor towards the left hand is contained in the first figure of the dividual towards the same hand; so here demanding how often 1 is contained in 5, the answer is 5 times, whence linfer that the Divisor 184 is not contained oftner than 5 times in the dividual 563 (for 6 times 184 is manifestly greater than 563) but whether it be contained 5 times in it or not, examination must be made either by multiplying (in some by-place) the Divifor 184 by the faid 5, and comparing the product with the dividual 563, or else thus, faying 5 times I (to wit the I in the Divifor, is contained in 5, to wit, the first figure of the dividual 563, 5 times, but then 8, the following figure of the Divifor, cannot be found 5 times in 6, the following figure of the dividend, and confequently the Divisor 184 is not contained 5 times in the dividual 563. wherefore I make another tryal to fee whether it may be contained 4 times in it or not; faying 4. times 1 is 4, which is found in 5, and there will remain 1. but then 4 times 8 which is 32 cannot be had in 16, (for the 1 before remaining being fupposed to stand before 6 maketh 16) hence I conclude again, that the Divisor 184 is not contained 4 times in the dividual 563, wherefore I make another tryal to fee whether it may be contained 3 times in it or not, faying 3 times 1 is 3, which is found in 5, and there will remain 2, again, 3 times 8 is 24, which is found in 26, (for the 2 before remaining being supposed to stand before the 6 in the

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the dividual makes 26) and there will remain 2: lastly, 3 times 4 is 12, which is likewise found in 23, (for the 2 remaining being supposed to stand before the 3 in the dividual makes 23) whereby I see that the Divisor 184 is contained 3 times in the dividual 563, wherefore I write 3 in the Quotient, and proceeding according to the 8th. Rule of this Chapter. I multiply the Divisor 184 by 3 184) 56304 (3 (the figure placed in the Quotient) so the Product is 552, which I substitute orderly underneath the divi
dual 563, then having drawn a line underneath the

faid Product, I subtract it from the dividual, and subscribe the remainder which is 11 under the line.

Again, according to the oth. Rule of this Chanter . I bring down o which stands in the next place of the dividend, to the remainder 11, fo there is 110 for a new dividual, then demanding how often the Divisor 184 is found in the dividual 110, and not finding it once contained in it, I write o in the Quotient ; (which is to be done as often as the question is answered by nothing) now because the Product arising from the multiplication of the Divifor by o, (the Cypher last placed in the Quotient) amounts to 0; the dividual 110 184) 56304 (306 out of which that Product should be subtracted, remains the same 552 without alteration; wherefore 1104 after a point is subscribed un-1104 der 4 the following place of the dividend, I annex 4 to the last di-

widnal 110, fo there will be a new dividual, to wit, 1104; and here the question at large is to know how often 184 is found in 1104, but to lessen the

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the tryal, because the dividual consists of one place more than is in the Divisor, it must be asked how often the first figure of the Divisor on the left hand is contained in the two formost places of the dividual towards the left hand, viz. I demand how often I is contained in II, and although it may be had II times, yet I need never begin the tryal above 9 times, therefore I make tryal with 9, faying 9 times 1 is 9, which is found in 11, and there will remain 2: but then o times 8 which is 72 cannot be found in 20, (20 because the 2 remaining being supposed to stand before o in the dividual makes 20) therefore I make tryal with 8, faying 8 times 1 is 8, which is found in 11, and there will remain 3, but then 8 times 8 cannot be had in 30, (30 because the 3 remaining being supposed to stand before the o or Cypher makes 30) therefore I make tryal with 7, faying 7 times 1 is 7, which is found in 11, and there will remain 4; but then 7 times 8 cannot be had in 40, therefore I make tryal with 6, faying 6 times 1 is 6, which is found in 11, and there will remain 5; also 6 times 8 is 48, which is found in 50, and there will remain 2; lastly, 6 times 4 is 24, which is found in 24, whereby at length I fee that the Divisor 184 is contained 6 times in the dividual 1104, wherefore I write 6 in the Quotient, and proceeding according to the 8th. Rule of this Chapter, I multiply the Divisor 184 by 6 (the figure last placed in the Quotient) fo the Product is 1104, which being subscribed under and subtracted from the dividual 1104, the Remainder is o, fo at last I conclude that the Quotient fought is 306.

Note, if the figure affumed for the Quotient, holds

holds good upon tryal as aforesaid, by two or three of the formost places of the dividual, it will for the most part hold throughout the dividual, but this must be a perpetual Rule, that whensoever the Product of the multiplication of the Divisor by the figure placed in the Quotient, happens to be greater than the dividual from which it ought to be subtracted, such Product must be struck out of the work, and a lesser figure is to be placed in the Quotient.

For a fecond Example, let it be required to divide

15114220 by 2987, or into 2987 equal parts.

First, the Divisor 2987 being greater than 1511, (to wit, the four formost places of the Dividend) I set a point under 4, thereby setting apart 15114 for a Dividual, then because the Dividual consists of one place more than the Divisor. I ask how often 2 (the 2087) 15114220 (5

visor, I ask how often 2 (the 2987) 15114220 (5 first figure of the Divisor to-

wards the left hand) is contained in 15 (the two for-

most places of the dividual) and finding the answer to be 7 times. I infer thence that the Divisor 2987 cannot be contained more than 7 times in the dividual 15114, but whether it will be contained 7 times in it or not, examination must be made, either by multiplying 2987 by 7, and comparing the Product with the dividual 15114, or else by the manner of tryal before delivered in the last Example, so at length it will be discovered, that the Divisor 2987 will not be found above 5 times in the dividual 15114, wherefore (according to the 8th. Rule of this Chapter) writing 5 in the Quotient, and multiplying 2987 by 5, I subscribe the Product

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duct of that multiplication which is 14935, under the dividual 15114, then drawing a line underneath the faid Product, and subtracting it from the dividual 15114, I subscribe the Remainder 179 under the line.

Again, (according to the 9th. Rule of this Chap-2987) 15114220 (50 ter) I bring down 2, the next place of the Dividend, to the faid Remainder 179, fo the new Dividual will

be 1792, that done, asking how often the Divisor 2987 is contained in the dividual 1792, and not finding it once contained in it, I write o in the Quotient, and here because the question is answered by 0, the next place of the dividend, to wit 2,

is to be brought down 2987) 15114220 (5060 to the dividual 1792, fo

the new dividual is
17922 Then renewing
the question, and proceeding as before, 2t
length the Division be-

ing finisht, the Quotient will be found 5060 exactly, without any Remainder; but if any Remainder had hapned after the subtraction of the last Product, it must have been prosecuted according to the directions before given in the example at the latter end of the 11th. Rule of this Chapter.

In like manner if 1208939550 be divided by 19999, or into 19999 equal parts, the quotient, or one of those equal parts will be found 60450,

and the Work will stand as here you fee.

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This latter method of Division is to be prefer'd before any of the common wayes of dividing by dashing out of Figures, where the steps of the Division are

19999) 1208939550 (60450

	119994	
	89995	
1	79996	-
	99995	
	99995	
1	00	

fo confounded, (besides the burden upon the memory by a promiscuous Multiplication and Division,) that if any errour happen, it can hardly be corrected without beginning the work anew; But in the way before explained, the particular Multiplications, Subtractions, and Remainders, which belong to every figure of the Quotient, are so distinctly and clearly exprest, that if an errour happen, the work may easily be reformed.

XIV. So often as the Question is repeated in Division, so many places there must be in the Quotient (which may be discovered by the number of Points berosplaces in the Quotient placed under the Dividend) and so many be discony times is one and the same kind of weed.

operation repeated, the substance whereof is contained in the Verse before mentioned at the end

of the 10th Rule of this Chapter.

XV. When the Divisor consists of 1 or an unit in the extream place towards the left Acompensions hand, and nothing but Cyphers to-way of divisional wards the right, the division is per-ding by 10, formed by cutting off with a line so 100,1000.00 many places of the Divisor hath Cyphers; so the figures which

which stand on the left hand of the line give the Quotient, and those cut off to the right (if they be significant sigures) are to be proceeded with as a surplusage or overplus remaining, according to the Note at the end of the eleventh Rule of this

10) 472 | 0 (472

1000) 4 720 (4

Chapter. So if 4720 l. were given to be divided equally amongst 10 persons, the share of each would be 472 l. also if the said 4720 l. were to be di-

vided equally amongst 100 persons, the share of each would be 47 l. and there would be a surplusage or remainder of 20 l. to be also subdivided amongst them, after the said 20 l. are converted into shillings, according to the fifth Rule of the next Chapter. Lastly, if the said 4720 l. were to be divided amongst 1000 persons, the share of each would be 4 l. and there would be a remainder of 720 l. to be also divided as aforesaid. See the form of the Work in the Margent.

XVI. When the Divisor confifts of any fignificant figure or figures in the first or

Another Compendium in Livision. cant figure or figures in the first or formost place or places towards the left hand, and nothing but a Cypher or Cyphers towards the right, cut off

by a line fo many places of the Dividend towards the right hand as the Divisor hath cyphers towards the right; then divide the figures of the Dividend which stand on the lest hand of the line, by the figures in the Divisor which remain when the said Cypher or Cyphers are omitted, remembring after the division is finished, to write down next after the last remainder the places of the Dividend which were first cut off: So if 36732 were given to be divided

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divided by 20, the Quotient will be 1836, and there will remain 12, viz. if you cut off one place from the Dividend towards the right hand (because the Divisor ends with one Cypher) and then divide the rest, to wit, 3673

by 2 (according to the 11th. 2 0) 3673 2 (1836 will arise in the Quotient 1836, and the last remainder after such division is finisht will be 1, unto which if 2 (the figure first cut off from the Dividend) be annexed, the total remainder is 12.

In like manner if 7456787 were given to be divided by 304000, the Quotient will be 24, and there will remain 160787; viz. If you cut off 3 places from the Dividend towards the right hand

(3 places because the Divisor ends with 3 Cyphers) and then divide 7456 by 304, there will arise in the Quotient 24, and the last remainder after

304 | 000) 7456 | 787 (24 608 1376 1216 160787

fuch division is finisht, will be 160, sunto which if 787 (the places first cut off from the Dividend) be annexed, the total remainder or surplusage is 160787, which is to be proceeded with as is directed in the Note at the latter end of the eleventh Rule of this Chapter.

XVII. Division and Multiplication do interchangeably prove one another; for
in Division if you multiply the Divifor by the Quotient, the Product will
be equal to the Dividend: So in the

Example of the 13th Rule of this Chapter; if 184

56

the Divisor be multiplyed by 306 the Quotient, the Product is 56304, which is the same with the Dividend ; but when after the whole Division is finished any figures remain of the last Subtraction, add them likewise to the Product : So in the last Example of the 16th Rule of this Chapter, the Divifor 304000 being multiplyed by the Quotient 24, produceth 7296000, unto which if you add the number remaining, to wit, 160787, the fum is 7456787, which is the same with the Dividend. Again, in Multiplication, if the Product be divided by the Multiplicator, the Quotient will give you the Multiplicand, or if the Product be divided by the Multiplicand, the Quotient will give you the Multiplicator : So in the first Example of the 9th Rule of the last Chapter, if the Product 111024 be divided by the Multiplicand 3084, the Quotient gives the Multiplicator 36.

There is also of Multiplication a Common proof argued from the Multiplicand, the Multiplicator and the Product by cafting away nines, but by that way of proof (though rightly used) a false Product will be affirmed to be true : Example, if 3462 be multiplyed by 786, the true Product is 2721132, but if I fay 4953132 or 3153132 is the Product, (or many others which may be given) the proof by nines will confirm them to be true Products, though they are falle, as will be evident to fuch as know the Rule, which I mention here only to fet a brand upon it, that it may be avoided

by all lovers of Truth,

Book I.

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CHAP. VII.

Reduction.

In Orasmuch as in Mony, there are diversities of kinds, viz. in England, Pounds, Shillings, Pence, and Farthings; also divers kinds of Weights, Measures, &c. as hath been fully declared in the second Chapter; and because it is oftentimes required to find how many pieces of one kind of Mony are equal in value to a given number of another (and so likewise of Weights, Measures, &c.) it will be convenient in this place to shew how that is performed, since thereby the Rules of Multiplication and Division before delivered will be exercised; this kind of operation is called Reduction.

II. Reduction is either descending or ascending.

III. Reduction descending is when a number of a greater denomination being given, it is required to find how many of a lesser denomination, are equal in value to that given number of the greater: As when it is required to find how many sollings are contained in 301. Likewise how many pence in

320 s, or how many hours in 365 days, &c.

IV. Reduction ascending is, when a number of a lesser denomination being given, it is required to find how many of a greater denomination, are equal in value to that given number of the lesser: As when it is required to find how many pence are contained in 500 farthings? likewise how many shillings in 348 pence? or how many days in 864 hours? &cc.

V. Re-

V. Reduction descending is performed by MulReduction describes, for if the given number of
feending is performed by be multiplyed by such number of InMultiplication. tegers of the lesser as are equal to one
of the Integers given; the Product is the number
of Integers of the lesser denomination required.

So 2301. of English Mony will be reduced into 4600 s. for if 230 be multiplyed by 20 (the number of spillings which are equal to 1 pound) the

230 Pounds.	4600 s. will be reduced into
4600 Shillings.	contained in I shilling) the pro-
92 46	duct is 55200. Also 55200 pence being multiplyed by 4. (because 4 farthings make a pen-
55200 Pence.	ny) are reduced into 220800 Farthings as by the operation in
220800 Farthings.	the Margent is evident.

345 Ounces.	The like method is to be observed in Weights Mea- fures, &c. So 345 Ounces
6900 Penny Weights	Troy are reduced into 6900 Penny Weights, and 6900
276 138	Penny Weights to 165600 Grains, as by the operation
165600 Grains.	in the Margent you may

Compare this with the Note upon the last Example of the 11th rule of the 6th, Chapter. Note, By this Rule the Learner is furnished with skill to resolve that case in Division when the Division is less than the Divisor:

Example

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Example, Let it be required to divide 7 ponnds of English Money equally amongst 8 Persons : here it is evident that the Dividend 7 is less than the Divisor 8; that is, the number of Pounds is less than the number of Persons, and consequently each share must be less than a Pound; so that in effect it is required to find how many Shillings and Pence belong to each Person for his share : First, therefore reduce the 7 Pounds into Shillings, which will be 140, these divided by 8 give 17 Shillings to each Person, and there will yet be a remainder of 4 Shillings to be also equally divided into 8 parts, but thele 4 Shillings must be first reduced into Pence, which will be 48, then dividing 48 by 8, the Quotient will give 6 Pence more to every Person, so at last it appears that if 7 Pounds of English Money be equally divided into 8 parts, the entire Quotient (or one of the equal Thares) will be 17 Shillings and 6 Pence.

In like manner, if 354 Pounds of English Money be given to be divided equally amongst 125 Persons, the share of each will be found to be 2 Pounds, 16 Shillings, 7 Pence, 2 Farthings, and somewhat more, but the parts of a Farthing being of no moment (and not properly to be handled

in this place) are neglected.

Compare these two Examples with the last Example of the eleventh Rule of the sixth Chapter.

In Reduction descending, the Learner may receive farther help by the subsequent Tables,

E 4

1. Of English Money.

Pounds
Shillings
Pence

Pence

Pence

Pence

Pence

Farthings.

2. Of Troy Weight.

Pounds
Ounces
Penny W.

Ounces

A 20

Response of the point of the poi

Also in Apothecaries Weights.

Ounces Troy (8) Drams.

Drams

Scruples

Scruples

Ounces Troy (8) Scruples

Grains.

3. Of Averdupois Weights.

Hundred W. 28 Quarters.

Quarters 28 Pounds.

Pounds 16 Counces.

Ounces Drams.

4. Of Liquid Measures.

Hogheads
Gallons
Pottles
Quarts
Quarts

5. Of Dry Measures. Busbels. Quarters Pecks. Bushels Gallons . Pecks Pottles. Gallons Pottles Quarts Of Long Measures. English miles Furlongs. Farlongs Tards Feet Barley Corns. Inches Alfo. Yards or Ells Quarters 7. Of Superficial Measures of Land. Acres Roods (Perches or Poles. 8. Of Time. Weeks

Weeks
Dayes
Hours

\$\frac{2}{24} \frac{2}{5} \quad \text{Houres.} \text{Minutes.}

VI. Integers of divers denomina-Tereduce intetions are reduced into the least of gers of divers those denominations according to the into the lowest fifth Rule aforegoing, by descending of those denoorderly to the next inferiour denomi-minations.

nation,

nation, and adding to each Product fuch Integers (if there be any) which are of the same name.

So 12 Pounds, 13	Shillings, and 10 Pence, are re-
l. s. d.	duced into 3046 Pence in this manner, viz. 12 l. multiplied
12-13-10	by 20(because 20 s. make one
20	1.) produce 240 Shillings, un.
240	to which adding 13 s. the fum
add 13	is 253 Shillings : Again, 253 s.
253 Shillings.	multiplied by 12 (because 1
12	Shilling is equal to 12 Pence)
506	produce 3036 Pence, unto
253	which if 10 Pence be added,
3036	the sum is 3046 Pence, as by
add 10	the operation in the Margent
3046 Pence.	is manifest.

So 35 Ounces, 16 Penny Weights, and 12 Grains Troy will be reduced into

17196 Grains.

VII. Reduction ascending is performed by Division, for if the number of Integers Reduttion afcending is per- given, be divided by fuch a number formed by Di- of the same Integers as are equal to vision. one of the Integers required, the

Quotient is the number of Integers fought.

So 220800 Farthings being divided by 4 (the number of Farthings in a Penny) give 55200 Pence in the Quotient; In like manner if 55200 Pence be divided by 12 (the number of Pence in a Shilling) the Quotient is 4600 Shillings. Lastly 4600 Shillings being divided by 20 (because 20s. make a Pound sterling) the quotient is 230 Pounds sterling) which are equal to 220800 Farthings first given. The operation is as followeth.

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12) 20) 4) 220800 (55200 (460) 0 (230 l.

In like manner, 34268 Grains Troy will be reduced to 5 l. 11 Ounces, 7 Penny Weight, and 20 Grains. This kind of Reduction may be made the eafier to the Learner by the following Tables.

1. Of English Money.

Pence
Shillings.

2. Of Troy Weight.

Grains
Penny W. 3 24 SPenny Weights.
Ounces Onnces.
Pounds Troy.

Also in Apothecaries Weights.

Grains
Scruples
Scruples
Scruples
Scruples
Scruples
Scruples
Scruples
Drams
Ounces Troy.

3. Of Averdapois Weight.

Drams (16) Ounces.

Quarters (16) Pounds.

Pounds 28 20 Quarters of C.

Quarters (4) Hundred Weight.

4. Of

4. Of Liquid Measures.

Pints
Quarts
Pottles
Gallons

Gallons

Pints

2
Quarts
Pottles

Compared to the property of th

5. Of Dry Measures.

Pints
Quarts
Pottles
Gallons
Pecks
Bufbels

Pints

Quarts.
Pottles.
Pallons.
Pecks.
Pallons.
Pecks.
Pallons.
Pecks.
Pallons.
Pecks.
Pallons.
Pecks.
Pallons.

6. Of Long Measures.

Barley C. 3 3 | Inches. Feet. Feet 3 3 | Yards. Furlongs. English Miles.

Also,

Nails \554\ 2 Quarters of Yards,
also of Ells.

Quarters \60 \text{Yards, also Ells.}

Of Superficial Measures of Land.

Perches San Acres.

Roods San Acres.

8. Of Time.

Note;

I.

Note, that if after Division is finisht in Reduction ascending there be any remainder, it is of the same denomination with the Dividend.

Note also that Reduction descending and ascending do mutually prove one another, by inverting

the question.

Questions to exercise Reduction.

1. In 257 1. how many shillings? Answer, 5140.

2. In 3076 1, how many shillings ? Answ. 61520.

3. In 902 shillings how many pence? An. 10824.

4. In 2179 shillings how many farthings? Anfmer, 104592.

5. In 491.—13 s.—7 d. how many pence? An-

[mer,11923.

6. In 2053 l. —14 s. —9 d. —, 2 f. how many farthings? Answ. 1971590.

7. In 354 lb. of Troy weight, how many grains?

(of Gold-smiths weight?) Answ. 2039040.

8. In 300 English miles, how many yards? Ansper, 528000.

9. In 1 English mile, how many barley cornes

length? Answ. 190080.

10. In 560 Acres, how many Perches? Answer, \$9600.

11. In 225 Acres, 3 Roods, and 30 Perches, how many Perches? Answ. 36150.

12. 30565 pence how many pounds? Answer,

127 1. -7 s. - 1 d.

13. In 5764684 farthings, how many pounds? Answ. 6004 !. 17 s. - 7 d.

14. In 234678 Perches, how many Acres? Anfiner, 1466 Acres, 2 Roods, and 38 Perches.

15. In 525960 minutes of an hour, how many dayes?

dayes? Answ. 365 dayes and 6 houres, (or 1 year very near.)

16. In 10080 Pintes, how many Hogsheads?

Answ. 20.

17. In 34678 grains of Apothecaries weight, how many ounces Troy? Answ. 72 Ounces, 1 Dram, 2 Scruples, and 18 Grains.

18. In 106735 Pintes of wheat, how many Quarters? Answ. 208 Quarters, 3 Bushels, 2 Pecks,

I Gallon, 1 Pottle, 1 Quart, 1 Pinte.

19. In 3969301 Barley corns length, how many Miles? Answ. 20 Miles, 7 Furlongs, 12 Yards, 2 Feet, 4 Inches, and 1 Barley corns length.

20. In 19008co Barley corns length, how ma-

ny Miles ? Anfw. 10.

CHAP. VIII.

Of the Rule of Three Direct.

I. THE Rule of Three is so called, because by three numbers known or given, it teacheth to find a fourth unknown, it is also called the Golden Rule for the excellency thereof; Lastly, it is called the Rule of Proportion for the reason hereafter declared.

II. The Rule of Three is either fingle or com-

pound.

III. The single Rule is, when three terms or numbers are propounded, and a fourth pro- The Rule portional unto them is demanded.

of Three-

IV. Four numbers are said to be proportionals, when the first containeth the second, or is containether.

ned by the second in the same manner as the third container the fourth, or is contained by the sourth: so these 4 numbers are said to be Proportionals, 8,4,12,6, for as 8 containeth 4 twice; so doth 12 contain 6 twice, and therefore 8 is said to have such proportion to 4 as 12 hath to 6; likewise these are Proportionals, 4,8,6,12. For as 4 is the half of 8, so is 6 the half of 12; and therefore 4 is said to have such proportion to 8 as 6 hath to 12.

V. The terms or numbers of the Rule of Three, (to wit, the three numbers given, and The divers dethe fourth fought) confift of two dif- mominations ferent denominations, viz. two of the of the terms in three given terms have one name, and the Rule of the other given term with the term required have another: fo this question being demanded, if four Students spend 19 pounds in certain moneths, how much money will ferve 8 Students for the same time, and at the same rate of expence? Here Students and pounds are the two denominations of the terms in the question, viz. 4 and 8 (being two of the terms propounded) have the denomination of Students, and 19 the other term given, together with the term required, have the denomination of pounds.

VI. In the Rule of Three, two of the three given terms imply a supposition, and the third moves a question: so in the aforementioned question a supposition is made, that 4 Students spend 19 pounds, and a question is moved with the number 8, to wit, how many pounds will 8 Students

fpend?

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VII. In the Rule of Three, the numbers given The right orde- must be fo ranked , that the known ring of the number or term upon which the que-terms given. Ition is moved, must possess the third place in the Rule, also of the other two that which hath the same denomination with the third, must be in the first place : lastly, the other known term which is of the same denomination with the fourth term fought (or answer of the question) must possess the second place :' fo in the question before mentioned, the terms 4, 19, and 8, are to be thus placed, viz. 8 is the term upon which the question is moved, and therefore to posses the third place in the Rule, 4 is of the same denomination with 8, viz. of Students, and therefore to be in the first place. Lastly, 19 being of the same denomination with the term fought, viz. of money is to be in the fecond place, and fo they will be placed in the Rule thus,

That is to say, if 4 Students spend 19 pounds, what will 8 Students spend? And here for the better discerning of the term or number upon which the question is moved, you may observe, that for the most part it is the known number in the question which immediately followeth these or such like words; viz. How many? How much? What will? How long? How far? &c.

VIII. The Rule of Three is either Direct or

Inverse.

IX. The Rule of Three Direct is, when the sense The Rule of or tenour of the question requireth Three Direct, that the fourth number sought must have

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have such proportion to the second, as the third number hath to the first; so in the afore-mentioned question, if 4 Students spend 19 pounds, how many pounds will 8 Students spend at the same rate of expence? It is evident that the thing required is to find a number which may have such proportion to 19, as 8 hath to 4; that is, as 8 is the double of 4, so ought the fourth number to be the double of 19; for if 19 pounds be required to maintain 4 Students a certain time, as much more must needs be required for the maintenance of 8 Students the same time; and therefore in this case we may say in a direct proportion, as 4 is to 8, so is 19 to a number which ought to be as much more as 19.

X. In the direct Rule of Three, if you multiply the fecond term by the third, or

(which is all one) the third term by the How to work fecond, and then divide the Product the Rule of the Rule of the first, the Quotient will give the the three given fourth term or fourth proportional terms beingsinarequired: so in the question before gle numbers. propounded, if you multiply 19 by 8, the product is 152, which if you divide by 4, the quotient will

give you 38 the fourth term demanded, and the work will fland thus;

A fecond Example may be this, if 8 yards cost 9 pounds, how much will 3 yards cost?

Answer, 3 l. — 7 s. — 6 d.

Stud. 1. Stud. 1. If 4-19-8-(38

8 4) 152 (38 pounds, 12 32 32

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This question being stated according to the feventh Rule of this Chapter,

y. 1. y. 1. s. d 8-9-3- (3:7:	will stand as here you see, 6 then multiplying (as before)
3	the fecond term 9 by the
8)27(3 pounds	third term 3, the Product is
24	27, which being divided by
3 the remainder.	the first term 8 the quotient is 3 pounds, and there is a
8)60 (7. shillings.	remainder of three pounds which must be reduced into 60 shillings, and after those
4 the remainder	faillings are divided by 8, and the rest of the work

8)48(6 pence. profecuted according to the Note at the latter end of the 11th Rule of the 6th. Chapter, at length the entire quotient or anfwer of the question is 31. 7 s. - 6d.

A third Example, if 51 ounces of filver plate be fold for 13 pounds sterling, what is the price

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	I			
	13	-		
	20			
51)2	600	5 Shilli	ngs.	
-	55			
	5			
241	12			
51)	50 (1	penn	y.	
	1			
!	9	:		

of I ounce of that plate? Ans. 5 s - 1d, and somewhat more. The operation is thus, After the three known terms of this question are rightly ordered, they will stand as here you fee in the Example. then multiplying the fecond term 13 by the third term 1. the product will be also 13. (for multiplication by 1 makes no alteration) which 13 being divided by 51, after the manner of operation delivered

livered in the note upon the 5th Rule of the 7th Chapter, the entire Quotient or answer of the question will at length be found to be 5s -- 1d. and somewhat more, but the surplusage being less than a farthing is omitted as ufelefs.

Example 4. What must be paid to a labourer for his wages for 27 weeks at the rate of 4 s. for I

week? Answer, 51. -. 8 s.

After the 3 given terms are rightly placed in the Rule, they will stand as you Weck. Shil. Week fee in the Example ; then multiplying the third term 27 by the second term 4 the product is 108, which I should divide by the first term i, but in regard division by I makes no alteration, the Quotient is also 108, forthat the fourth term sought is 108 shillings, which being reduced to pounds, according to the seventh Rule of the seventh Chapter. give 51. 8 s. for the answer of the question.

XI. In the Rule of Three, if after the question

is stated according to the seventh Rule of this Chapter, any of the 3 given terms be a compound term contifting of divers denominations, as when they are pounds, shillings, and pence; or weeks, days, hours, &c. such compound term must first be reduced into the lowest

To prepare the terms of the Rule of Three compounded of divers denomi nations.

of those denominations (by the fixth Rule of the feventh Chapter) to the end that the three given terms may be three lingle numbers; also of these three fingle numbers the first and third must always be of one and the fame denomination: for if it happen that they express things of different

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names, fuch of the two which hath the greater name (or denomination) is to be reduced into the same name with the leffer (by the fifth Rule of the feventh Chapter) these preparations being obferved, the rest of the work is to be prosecuted according to the tenth Rule of this Chapter. Example, what will 48 ounces, 17 penny weight, and 20 grains of filver plate amount unto at the rate of 5 s, -6d. the ounce ? Answer, 13 l. -8s .- 10d, - 3f. very near.

oz. s. d. oz.p.w.gr. 1-5-6-- 48-17-20 being stated ac-20 20 60 960 17 6 24 480 66 977 24 3908 1954 23448 20

This question cording to the feventh Rule of this Chapter, will stand in the Rule as you fee in the Example, to wit, if I ounce cost 5 s. - 6 d. what will 48 oz. -17p. w. - 20 gr. cost ? 23468 grains. Here because the

third term compounded of divers denominations, it must be reduced into the lowest of those denominations, to wit, grains, fo by the fixth Rule of the feventh Chapter there will be found 23468 grains for the third term ; likewise, because the second term gs. -6d. is a compound term, whose lowest name is pence, it must be reduced into pence (by the aforefaid rule) fo there will be found 66 pence for the second term ; moreover because the first term hath the name ounce and the third term the name grain,

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grain the first term I ounce must be converted into 480 grains (which are equal to 1 ounce)then will the three terms or fingle numbers stand in the rule, as here you fee, viz. if 480 grains cost 66 pence, gr. pence. gr. how many pence will 23468 480 66 23468 grains cost? Now proceeding according to the tenth Rule of this Chapter, there will arise in the quotient 3226 pence, besides a remainder of 407 pence, which being reduced to farthings, and those divided by the first term 480 the quotient will be 3 farthings, fo that the entire quotient is 3226 pence, 3 farthings, and somewhat more (but the parts of a farthing being of no moment, may be neglected.) Lastly, the said 3226 pence being reduced according to the feventh Rule of the feventh Chapter, give 131.—8 s. — 10 d. — 3 f. fo that 13 1. - 8s. - 10 d. - 3 to and somewhat more, will be the Answer of the Question.

XII. For the proof of the Direct Rule of Three multiply the fourth term by the first, The proof of the which done, if that Product be equal Rule of Three to the Product of the second term direct. multiplyed by the third, the work is right, otherwise it is erroneous: so in the first Example,

38 the fourth term, being multiplyed by the first term 4, the Product is 152 which is also the Product of 19 multiplied by 8. But if it happen that after the fourth term, or answer of the question. is found in the same denomination with the second term, there is yet a remainder, fuch remainder must be added to the Product of the first term, multiplyed by fuch fourth term, and then the fum must be equal to the Product of the second and

third

third terms: (the fecond term consisting of the fame denomination with the fourth) so in the last Example the fourth term is 3226, and there happens to be a remainder of 408, which being added to the Product of the multiplication of the said 3226 by the first term 480, gives 1548888, which is the same with the Product of the third term 23468 multiplyed by the second term 66 as will appear by the work.

AIII. When the first of the three given numAcompositions operation bers in the Rule of three Direct,
on in the Rule of is 1 or unity, the question may ofthree directs when the fully than by the Rule of Three,
even by those who have but little skill in Arithmetick, as will partly appear by the following Exam-

ples, viz.

1. At 17 s. —9d. the yard, what will 84 yards cost? Answer, 74l. —11 s. For reason sheweth that 84 yards must (at the said rate) cost 84 Angels, 84 Crowns, 84 half Crowns, and 84 Three pences, all which being computed and added together, will give the full value of 84 yards, Viz.

	1.	s.	d.
84 Angels make -	 -42-	- 00-	00
84 Crowns. ——	 -21-	- 00-	-00
84 Half Crowns-	 -10-	- 10-	00
84 Three-Pences -	 I-	-01-	00
	 -		
	 	15	

Sum 74 11 --- 00

2. At the rate of os, the Bushel of Wheat, what will 51 Quarters amount unto? Answer, 1831. — 125. — od.

It is evident that the price of 1 Quarter (which confilts of 8 Bushels) will be 8 Angels wanting 8 Shillings ; therefore.

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		1.	5.	d.
from 8 Angels, to wit-		4-	- 00-	-00
fubtract				
		-	-	
remains the price of 1	Quarter	3-	12	-00

Then the value of 51 Quarters at the rate of 31 .- 12s. - od. the Quarter may be found in manner following, Viz.

51-00-00 51 times 3 1. or 3 times 51 1. is 51-00-00 251-00-00 5-02-00 51 Shillings doubled make the price of 51 Quarters - 183 - 12 - 00

3. What is a Cheft of Sugar worth, that weigheth neat weight (the Tare being fubtracted) 7 C. 3 9. 7. lb. at Tare is that wherein any thing is put as a the rate of 61. -- 3s. -- 4d. Bag for Pepper, a (heft for I C? Answer, 481. -- 35. for Sugar. 6 d. ___ 2 f.

	1.	\$.	d.	
7 times 6 pounds make-				
7 times 3 Shillings	- I -	-01-	00	
7 Groats			04	
for 2 qu. is	1d. Z 2 -	01-	08	
for 2 qu. 15 ———	-2,			
The half of 3 1 15 8	Bd. Z .	10-		
for 1 qu. is	-2			
The fourth part of 1 l.				
10 s. — 10 d. (1	be-			f.
cause 71. is a four		-07	08-	2
part of 28 l. or of 1	gu.			
is —————	-)			

48-03-06-2

Practical rules of this nature cannot be compleatly understood without some skill in fractions, as will hereaster appear in the second Chapter of the Appendix, and therefore I shall conclude this Chapter with the following Questions, whose Answers are annexed to them, and may be found out by the preceding Rules; but the operations are purposely omitted, and left as an exercise for the Learner.

Questions to exercise the Rule of Three direct.

1. If 17 yards of Cloth cost 19 l. 2 s 6 d. what will 35 yards cost at that rate? Answer, 39 l. 7s.6d.

2. If 35 yards cost 39 l. 7 s. 6 d. how many yards may be bought at that rate for 19 l. 2 s. 6 d. Answer, 17 yards.

3. If 35 yards cost 39 1. 7 s. 6 d. what are 17 yards worth at that rate? Answer, 19 1. 2 s. 6 d.

4. If 17 yards be fold for 19 l. 2 s. 6 d. how many yards will 39 l. 7 s. 6 d. buy at that rate? Answ. 35 yards.

5. What

I.

5. What must I pay for the carriage of 17 hundred weight, 3 quarters, and 11 pounds Averdapois, at the rate of 7 shillings the hundred weight, Answ. 61.—45.—11 d.—1 farth.

6. If 61.—41.—11 d.—1 f. be pay'd for the carriage of 17 hundred weight, 3 quarters, and 11 pounds, what was pay'd for the carriage of 1

pound weight? Answ. 3 Farthings.

7. What must I pay for 39 ounces, 7 penny weight, and 18 grains of white Plate at the rate of 5s. and 5d. the ounce? Answ. 10l.—13s.—4d. and three quarters of a farthing.

8. What must 1 l. (or 20 s.) pay towards a Tax, when 326 l.—6 s.—8 d. is assessed at 41 l.—16 s.—

2 d.-3 f. Answ. 2 s.-6 d.-3 f.

9. What will the Interest of 876 l.-17 s.-6 d. amount unto for 1 year at the rate of 6 l. for 100 l. for the same time? Answ. 52 l.-12 s.-3 d.

CHAP. IX,

Of the Inverse Rule of Three.

I. THE Rule of Three Inverse is, when the fourth term required ought to proceed from the second term, according to the same rate or proportion that the first proceeds from the third: so this question being propounded, if 8 Horses will be maintained 12 dayes with a certain quantity of Provender, how many dayes will the same quantity maintain 16 Horses? Here as 8 is half 16, so ought the south term required to be half

here followeth.

half 12; for if certain bushels of Provender serve 8 Horses 12 dayes, 16 Horses will eat up as much Provender in half that time; and therefore you cannot fay here in a direct proportion (as before borses dayes horses in the Rule of Three direct) 8----16 ther number which ought to be in that case as great again as 12, but contrari. wife by an inverted Proportion, beginning with the laft term firft , as 16 is to 8 , fo is 12 to another number which ought to be in this case half 12. And by the due observation of this definition, together with that of the Rule of Three direct (propounded in the ninth Rule of the eight Chapter) when any question belonging to the single Rule of Three is propounded, you may readily discern by which of those Rules it ought to be refolved; for if the three terms given look for a fourth in a direct proportion as they stand ranked in the Rute, you must resolve the question by the direct Rule; contrariwise when the proportion is inverted or turned backwards, it ought to be resolved by the Inverse Rule of Three, which

How to work the Inverse Rule of Three, after the three given terms are rightly placed in the Rule, and reduced (if there be need) according to the eleventh Rule of the eighth Chapter, multiply the first term by the second, or (which is the same) the second term by the first, and then divide the Product by the third term, so the quotient will give you the sourch term required, or answer of the question; thus in the question premised

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mised in the last Rule, if you multiply 12 by 8, the Product is 96, which if you divide by 16, the Quotient gives you 6, the fourth term required, as by the subsequent operation is manifest.

III. For the more ready discovering, whether a question propounded belongs to the Rule of Three Direct, or there a question in the to the Rule Inverse, observe the Rule of Three is to be directions following, Viz. 1. By resolved by the Rule the sense and tenour of the que. Direct, or by the Rule stion, consider whether more be

required or less; that is, whether the number fought must be greater or less than the second term: Secondly, esteeming the first and third terms as extreams in respect of the second, this will be a general Rule; namely, When more is required, the lesser extreme is the Divisor; but when less is required, the greater extreme is the Divisor. Lastly, the Divisor being sound out, it will be apparent whether the Rule be Direct or Inverse, for when the Divisor is the first term it is a Rule Direct; but when the Divisor is the third term, the Rule is Inverse. Another Example of the Rule Inverse may be this; If 12 Mowers do mow certain Acres

in 4 dayes, in what time will 23 Mowers perform the same work? Answer, 2 dayes, 2 hours, and

M. D. M.

12—4—23
4
23) 48 (2 dayes.

46
2
24
23) 48 (2 hours.
46
2

fomewhat more. Here, the 3 known terms being rightly placed in the 23 Rule, will stand as you fee in the Example; and since it is evident that 23 men will require less time than 12 men to finish the same work, therefore (by the Rule aforegoing) the greater of the two extream numbers 23 and 12 must be the Divisor; and because the Divisor 23

stands in the third place, this question is to be wrought by the Rule Inverse; wherefore multiplying the first term 12 by the second term 4, the product is 48, which being divided by the first term 23, the *Quotient* gives 2 dayes, and there is a remainder of 2 dayes, which being reduced to hours, and those divided by 23, the *Quotient* will be 2 hours, and there is yet a remainder of 2 hours to be subdivided into 23 parts if you please; so that the fourth term sought, or answer of the question is 2 dayes, 2 hours, and somewhat more.

Again, take this for a third Example, If I lend my Friend 356 pounds for one year and 35 dayes (the year being supposed to consist of 365 dayes) how long time ought he to lend me 500 pounds to requite my courtesse? Answer, 284 dayes and somewhat more, as by the subsequent operation

is manifest.

1. y. D. l.
356—1: 35—500

365
add 35

multiply \$400
5100 (284 dayes.)

10

42
40
24
20
400

IV. The proof of the Inverse Rule of Three is this, multiply the third term by The proof of the fourth, then if this Product be ethe Rule of qual to the Product of the first term Three Inver fe. multiplyed by the fecond, the work is true, otherwise erroneous; so in the Example of the second Rule, the Product of 16 and 6 is equal to the Product of 8 and 12. But if it happen that after the fourth term or answer of the question, is found in the same denomination with the second term, there is yet a remainder, such remainder must be added to the Product of the third term multiplyed by the fourth, and then the fum must be equal to the Product of the first and fecond terms (fuch fecond term being of the fame particular denomination with the fourth;) fo in the last Example, the fourth term is 284 dayes, and there is a remainder of 400 after the divilion was finisht, this 400 being added to the Product of

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of the Multiplication of the third term 500, by the fourth term 284 gives 142400, which is equal to the Product of the first term 356, multiplyed by the second term 400 dayes.

CHAP. X.

The double Golden Rule Direct, performed by two single Rules.

I. THE Compound Golden Rule is, when more than three terms are propounded.

II. Under the Compound Golden Rule is comprehended the double Golden Rule, and divers

Rules of plural proportion.

III. The double Golden Rule is, when five the double Golden Rule is terms being propounded, a fixth proportional unto them is demanded: as in this question; If 4 Students spend 19 pounds in 3 moneths; how much will serve 8 Students 9 moneths? Or this, if 9 Bushels of Provender serve 8 Horses 12 dayes, how many dayes will 24 Bushels last 16 Horses?

IV. The five terms given in this Rule consist of two parts, Viz. A supposition expressed in the three first terms; and a demand propounded in the two last: So in the first Example of the last Rule, this clause (If four Students

fpend 19 pounds in 3 moneths) is the supposition, and this (how much will serve 8 Students nine moneths)

moneths) is the demand: likewife in the other Example of the fame Rule, this clause (If nine Bushels of Provender serve 8 Horses 12 dayes) is the supposition, and this (How long, or how many dayes will 24 Bushels last 16 Horses) is the demand propounded.

V. Here for ranking the terms propounded in

their due order, first observe amongst the terms of supposition, which of The righ orthem hath the same denomination with the term required, then refer-

dering of the terms.

ving that term for the fecond place, write the other two terms of supposition one above another in the first place; and lastly the terms of demand likewise one above another in the third place of the Rule, in such fort that the uppermost may have the fame denomination with the uppermost of those in the first place : Example, if 4 Students fpend 19 pounds in 3 moneths, how much will ferve 8 Students o moneths ? Here the three terms of supposition are 4, 19, and 3, and of these terms 19 hath the fame denomination with the term required, Viz. of Pounds, for you are to enquire how much Money is requifite for the maintenance of 8 Students o moneths, wherefore

referving 19 for the second place, I write 4 and 3 one above another thus: then drawing a line upon the right hand of 4, I write 19 in the second place; this done, the Work will stand as in the Margent. Last of all, the terms of demand being 8 and 9,

and 8 having the denomination of Students, I place it in the same line with 4 and 19, and write 9

under

under it; all this performed, the terms in this question rank themselves as followeth:

Buffiels of provender farte 5

In like manner, if the second question of the third Rule of this Chapter were propounded, the terms thereof ought to be disposed

VI. Questions belonging to the double Golden Rule may be resolved by two single Rules of Three, or by the Golden Rule Compound of five Numbers.

The Proportions of the this nature are resolved by double Golden Rule, two single Rules, the proportions it is performed by two single Rules, the proportions are as followeth:

I. As the uppermost term of the first place, is to the middle term; So is the uppermost term of the last place to a fourth Number.

II. As the lower term of the first place is to that fourth Number; so is the lower term of the last place to the term required.

So in this Example before recited, uling tacitly the lower term of the 4-19-8 first place as a common number in 301-9

the first proportion, say thus,

I. If 4 Students spend 19 pounds (in three moneths) what will serve 8 Students (the same time d)

Or thus, If 4 Students spend 19 pounds, what

will 8 spend?

Which Rule of Three will be discovered to be direct (by the third Rule of the ninth Chapter) therefore the fourth proportional proceeding from the said three given numbers 4, 10, and \$ 10,38 (by the 10th Rule of the 8th Chapter aforegoing.) Again, to find the term required, using satisfy the appearanch term of the third place as a common Number in this last proportion, say as followsth.

II. If in three moneths 38 pounds are spent (by 8 Students) how much will serve them for 9

moneths?

Or thm, If 3 give 38, what will 9 yield you?
Which Rule of Three will likewife be discovered to be direct (by the third Rule of the ninth Chapter) therefore the fourth proportional proceeding from the said 3 numbers, 3, 38, and 9, you shall likewife find (by the 10th Rule of the 8th Chapter before-recited) to be 114, for 38 being multiplyed by 9, the Product is 342, which divided by 3 yields you in the Quotient 114: So that I conclude, If four Students spend nineteen pounds in three moneths, 114 pounds will serve 8 Students

dents o monethe; as you may further observe by

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3-61-4	3 sits to m		CHILL OS
. 8	8- (38	o.Qion, fay.ri	9 53 (H14
4)152(13 8 SALSI	13 1342	(1141 .1
11dw , 32	og Qı basql	(64,m	fame ti
refed to be	All bedifications of the nu	read to 12	A doldW A doldW AdoldW

In like manner if two single Rules of Three be formed (according to the preceding 7th Rule) out of the five numbers given in the last mentioned question, the same being ranked according to the latter manner of ordering the said numbers in the laster manner of ordering the said numbers in the laster manner of ordering the said numbers in the laster manner of ordering the said numbers in the laster manner of ordering the said numbers in the laster manner of ordering the said two Rules of Three will be a Rule direct, and the same answer of the question, to wit, 114 pounds will be discovered, as you may see by the subsequent operation.

3-19-9-(57	8-(114	14
3) 171 (57	4)456(114	HH
15	1 1 2d 42 Chearage	MSS IOI
21	O5	(d-)
0	1600	110
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VIII. The double Golden Rule it either Di-

IX. The double Golden Rule Direct is, when both the lingle Rules do each of them look for a fourth term in a direct proportion: As in the Example of the seventh Rule, where each the double Golof the two single Rules of Three is a dear Rule direct.

Rule direct.

For another Example take this, if the carriage of 8 C. weight 128 miles, cost 48 shillings, for how much may I have 4 C weight carried 32 miles after the same rate? The terms of this question according to the fifth Rule of this Chapter, rank themselves in this order:

Now taking tacitly the lower term of the first place, as a common number, I form the first Rule of Three according to the feventh Rule, (aying.

I. If the carriage of a certain weight (to wit, 8 C.) 128 miles will cost 48 shillings, what will the carriage of the same weight 32 miles cost?

Here it is easie to discern that the sewer miles any weight is carried, the less money will pay for the carriage of that weight, therefore the sourth number sought by the said Rule of Three must be less than the second number 48: And for a smuch as by the third Rule of the ninth Chapter, when less is required, the greater extreme (whether it be the first or third number 128 is the Divisor, therefore the first number 128 is the Divisor, and confequently the Rule of Three above propounded is a Rule direct, wherefore finding out the fourth num-

ber by the centh Rule of the eighth Chapter, to be 12 shillings, I proceed to the second proporc Colden Rule Die velibne noit

II. If the carriage of 8 C, (32 miles) coft 12 shillings, how much must I give to have 4 C.

carried the fame diffance :

And here likewise finding a fourth number to be looked for in a direct proportion , I discover that fourth, by the faid tenth Rule of the eighth Chapter, to be 6 . which is the term demanded, and the answer to the question propounded : fo that at last I conclude, If the carriage of 8 C. 128 miles cost 48 s. the carriage of 4 C. 32 miles will coft 6 s. according to the fame rate : fee the whole Work.

And then work by two five is eales of

The Double Golden Rule Inverse, performed

THE Double Golden Rule Inverse is, when one of the single Rules looks for a fourth term in an inverted proportion; As in the ate double Gollass Example propounded in the fifth and Rule of the last Chapter. For if you sarfe, rank the terms of that question, according to the said fifth Rule, these.

8 4 3 4 2 4 3 4 16 24

And then work by two fingle Rules of Three, formed according to the seventh Rule of the last Chapter, you shall find by the third Rule of the ninth Chapter, that the first of the said two Rules of Three will be inverse, and the laster direct for saying first, if 8 horses be maintained 12 dayes (by 9 bushels of Provender) how many dayes will 16 horses be kept by so much Provender? Mere the answer 6 dayes, will be found out by the Rule of Three inverse: Secondly, saying, if 9 bushels of Provender be eaten up (by 16 horses) in 6 dayes, in how many dayes will 24 bushels be spent: here the answer 16 dayes will be found out by the Rule of Three direct.

But if you order the given terms of the same

question, thu,

8 JX SAH 216

And then work by two single Rules of Three, formed according to the seventh Rule of the last Chapter, you shall find by the third Rule of the ninth Chapter, that the first of the said two Rules of Three will be Direct, and the laster Inverse, for saying first, If 9 bushels of Provender will last 12 dayes (to maintain 8 horses) how many dayes will 24 bushels serve the same number of horses: The answer 32 dayes will be found out by the Rule of Three direct; secondly saying, If 8 horses will be maintained 32 dayes (by 24 bushels of Provender) how long will 16 horses be kept by the same quantity of Provender? Here the answer 16 dayes will be found out by the Rule of Three direct.

Wherefore, when loever a question belonging to the double Rule of Three is severed into two lingle Rules of Three (according to the preceding Rules) if one of them happens to be a Rule inverse, that double Rule is called the double Rule inverse.

Now the Resolution of the Question propounded being ranked after the first manner, is as followeth.

salwer 6 dayer, will be long two by the Rule of Three inverte: Secondly, taying, if 9 bulbele of

Provender be searn up (by 10 horise) in 6 depends bear many dayes with each will be found out by the Role of Three direct.

Three direct.

Three direct.

Three direct.

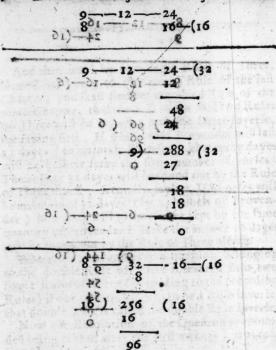
and the state of the green of the state of t

Chap.XI. of Three Inverse.

Again, The Resolution of the same Question, being ranked after the last manner, is this:

Sorb t at laft lay, it g Buffuls of Provender ferve tillogies to days, extenditely will laft to rest to days, which are resolution of the

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Again, The Resoluti 88 of the same Question, being ranked after the last manner, it this:

So that at last I say, If 9 Bushels of Provender serve 8 Horses 12 dayes, 24 Bushels will last 16 Horses 16 dayes, which is the resolution of the Question propounded.

CHAP.

So that if 4 Students spend 19 1 in three moneths, 14 1-will be regulate for the maintenance of 8 Students 9 mone HN Seek H Bale operation, at followeth.

The Golden Rule compounded of five Numbers.

I. THE Golden Rule compound of five numbers is, when the terms being ranked, as before, instead of the double terms we use their products, and then proceed to find the term required

by one fingle Rule of Three.

II. Here when the Queltion propounded ought to be performed byahe deuble Rule direct , multiplying the terms of Rule compound the first place, the one by the of five numother, take their praduct for the first bers performed term, the middle number for the fe- by one fingle cond, and the product of the two last terms for the hird term; this done, having found by the Rule of Three direct, a fourth proportional unto those three, that fourth term fo found is the number you look for! fo this question being again propounded, if 4 Students spend spilial a meldens, how much will feever & structures bearing another translate for the selection of the selection of rings of 8 C. 128 miles, collander, side prolitiders carriage 8: 4 0. camiles fe ma in ? the Antwer

The product of 4 multiplyed by 3 is 12, and the product of 8 multiplyed by 9 is 73; wherefore I fay, As 12 to 19, fo 72 to the term required, which I find by the lingle Rule of Three direct to be 114.

The Rule of Three Compound | Book L.

So that if 4 Students spend 19 1. in three moneths, 114 1. will be requisite for the maintenance of 8 Students 9 moneths, see the whole operation, as followeth,

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The Cours 8 8 common de de free	
TO HE Golden Spie compound of five n	-
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be perforger) \$30 pr(equble Kule 7 m Called treet, multiplying rise terms of Rale com	ib
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ther take their project for the first bur purfices, the middle at the for the terms and the second	0
Over 201 10 10 10 200 005 1 010	2.3
if come for the 84 ord come this done, ha	3 8

In like manner this being the Question as before (in the last Rule of the tenth Chapter) if the carriage of 8 C. 128 miles, cost 48 s. what will the carriage of 4 C. 32 miles stand me in? the Answer thereunto will be 6 s. as appears by the Work.

product of 8 mornidaed by o fers, wherefore I far, Arra to to, to varo the term required, white I find by the image wall of Three which to be tra-

portional paro the breed that fourth term to lound is the minion you look for: to this queflies being again proposated, if a Scutents fread 1024) 6144 (6 Smilings

be resolved by the double Rule Inverse, having multiplyed the double The Golden Rule terms a cross, that is, the uppermost compound of five term of the first place by the lower of the last, and the uppermost of the Rule direct or last place by the lower of the first, inverse.

term by which it is produced, and then if the inverse proportion benfound in the uppermost line, using those products is single terms, proceed to find the term required by the single Rule of Three directs. But in case you find the Inverse proposition in the lower line, perform the Work by the single Rule of Three directs.

So in the Example above mentioned, if 9 bushels of Provender serve 8 horses 12 dayes, how long will 24 bushels last 16 horses? Here is if you rank the rems thus, you shall 8—12—16 find the Inverse proportion in the 9 24 first line, as is observed in the last Chapter: And therefore having subscribed the products

36 The Rule of Three Compound, &c. Book 1.

products according to the direction given you in this Rule, I proceed to fatisfie the demand of this question by the single Rule of Three direct, as appears by the Work following.

1		0	-12	-16
	200	184 . b 3	1.2.172	24 (1
	1	14	PVIO	192
		W112-14		13
			0	284
or ide	nded on	HORO-14.	notifiend	384

21.) 4968 144 the double The Golden & ale cerms a croff, the ts abe uppermoft compened of fice serm of the first place by the lower Manderspring of the last, and by one hope and by one hope the last place by 400 ower of the first, more, write each periouel under the lower

cerm by which tisproduced, and then it the inon But the perms of this Queftion being ranked of hospital proportion is interms, proceed to 12 24 found in the lower line as you Sogard strate may oblerve likewife by the daft adi vd 20W ad Chapter: whereupon in this cafe to resolve the Question, I proceed by the single Rule of Three inverse, asappears by the Work hereunto annexed : howfoevertherefore you work the Question ; wou shall find the term required to be 16; fo that in last I conclude, as before in the laft Chapter : Il gibufbels of Provender forve 8 horfes 12 dayes, 24 bull dis will laft 16 horfes 16 'And therefore' baying fublicale syels.

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CHAP. XIII.

The Rule of Fellowship.

I. THE Rules of plural proportion are those, by which we resolve Questions, that are discoverable by more golden Rules than one, and yet cannot be per- Rules of plural formed by the double golden Rule proposions. mentioned before in the three last Chapters. Of these Rules there are divers kinds and varieties according to the nature of the question propounded, for here the terms given are sometimes sour, sometimes five, sometimes more, and the terms required sometimes more than one, Sec.

11.

II. Two particular Rules of plural proportion; are these, the Rule of Fellowinip, and the Rule

of Alligation.

III. The Rule of Fellowship is that , by which The Rule of in accompts amongst divers men (their relieves fip. feveral stocks together with the whole Zellow (bip. gain or loss of each particular man may be discovered: As in this Example. A and B were sharers in a parcel of Merchandize, in the purchase of which A laid out 7 l. and Bit l. and they having fold this Commodity, find that their clear gains amounts to 5+ s. Now here the Question to be refolved by this Rule is, what part of that 54 s. accrews to A, and what to B, according to the rate of the feveral fums or flocks which they adventured ? Again, A, B, and C, fraight a Ship from the Canaries for England, with 108 Tuns of Wine, of which A had 48, B36, and C24, the Mariners meeting with a florm at Sea, were conftrained for the fafety of their lives, to cast 45 Tun thereof over-board; here the Question to be refolved is, How many of the 45 Tun each particular Merchane bath loft, according to the rate of his Adventure?

W. The Rule of Fellowship is, either single or

V. The single Rule is, when the stocks propounded do continue in the Adventure (or common Bank) equal times, to wit, one stock as long time as another.

How to work thip, take the total of all the flocks for the fingle Rule. the first term, the whole gain or loss,

for

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for the fecond , and the particular stocks for the third terms; this done, repeating the Rule of Three fo often , as there are particular focke in the Question, the fourth terms produced upon those several operations, are the respective gains or loffes of those particular flocks propounded : So in the first Example above-mentioned 7 1. and 11 14 are the stocks propounded, whose total is 18 4 which I take for the first term : Again , 54s. the common gain, is the second term, and 71. the first particular stock , is the third term of the first proportion; whereupon I fay, as 18 1. to 54 . fo 71. to another number, which by the direct Rule of Three I find to be 21 s. viz. the part of the gain due to A, that expended the 7 1. flock. Then for the fecond proportion, I fay, as 181, to 54 , fo 11 1. to another number, which I likewise find by the Rule of Three direct to be 33 s, viz. the part of the gain due to B, for his 11 1. fock.

Again, in the other premifed Example, the particular loss that happens to A, is 20 Tun, to B 15, and to C 10 Tun.

VII. The double Rule of Fellowship is, when the stocks propounded are 2. Double, double numbers, viz. when each stock

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hath relation to a particular time; Example, A; B, and C, hold a passure in common, for which they pay 45 l. per annum. In this passure A had 24 Oken went 32 dayes, B had to there 48 dayes, and C fed 16 Oken there 24 dayes i now the Question to be resolved by this Rule is, what part each of these Tenants ought to pay of the 41 l. sant i and here you may observe, that the stocks propounded are double numbers, viz. each stock of Oken hath reference to a pareicular time, for the respective stock of A is 24 Oken, and its pareicular time is 32 dayes; again, the stock of B is 12 Oken, and the respective time is 48 dayes; and lassly, the stock of C is 16 Oken, and its peculiar time is 24 dayes, which as you see are double numbers.

VIII. In the double Rule of Fellowhip, multiply each particular stock by its re-Hew to work foective time, and take the total of the double their Products for the fieft term, the Rule. whole gain or loss for the second, and the faid particular Products of the double numbers for the third term : This done, repeating, as before, the Rule of Three, fo often as there are Products of the double numbers ; the fourth terms produced upon those several operations, are the numbers you look for : So in the Example of the last Rule, the Product of 24 and 32, is 768, the Product of 12 and 48, is 576, and the Product of 16 and 24, is 384, the fum of thefe Products is 1728, which is the first term in the Question, then 45 % the rent, is the second term, and 768 the first Product, is the third term of the first proportion. Wherefore I fay, as 1728 to 451. fo 768 to another number, which I find by she direct

Chap.XIII. The Rule of Fellowship.

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rect Rule of Three to be 201, viz. the part of the rent that A ought to pay? Then for the fecond proportion I fay, as 1728 to 45 1. fo 576 to 15 1. which is the part that B ought to pay: And lastly, as 1728 to 45 1. fo 384 to 10 1. viz. the part that C muft pay, ordered thenom to

A second Example of the eight Rule. Three Merchants, A, B, and C enter Partnership, and agree to continue in a joynt Adventure 16 moneths; A puts into the common flock at the beginning of the faid term 100 pounds mar 8 moneths end he takes out 40 pounds, and 4 moneths after fuch ta-, king out he puts in 140 pounds. B puts in at first 200 pounds, at 6 moneths end he puts in 50 pounds more, and 4 moneths after the putting in of the 50 pounds, he takes out 100 pounds. C puts in at first 150 pounds, at four moneths end he takes out 50 pounds, and 8 moneths after fuch taking out puts in 100 pounds. Now at the end of the faid 16 moneths they had gained 357 pounds, the Queflion is how much of the faid gain belongs to each Merchant for his share.

In Questions of this nature, two things are principally to be observed, 1. The whole time of partnership. 2. The respective time belonging to each mans particular flock; fo here, it is evident that the whole time is 16 moneths, and the particular stocks and times belonging to each Merchant will be as followeth, viz.

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Then adding the faid three totals together, to wit, 1840,3100 & 2200, the fum is 7140, wherefore proceeding as in the last Example; I say by the Rule of three direct, as 7140 is to the total gain 357 pounds;

The total of the products of money and 2200

time for C. is-

Chap. XIV. The Rule of Attation. 103 pounds; fo is 1840 to 92 pounds the gain of A:

again, As 7140 is to 357 3 fo is 3100 to 155 the gain of B: Laftly, as 7140 is to 357; fo is 2200,

to 110 the gain of C.

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h. IX. The Rule of fellowship is proved by Addition of the terms required, The proof. whose sumi ought to be equal to the

fecond term in the Question , otherwise the whole Work is erroneous : fo in the first Example of the fixth Rule afore-going, 21 s. and 33 s. being added together are equal to 54 s. the fecond term in that Question : likewise in the last Example of the fame Rule, as also in the first Example of the last Rule, the fum of 20, 15, and to the terms required are equal to 45, the fecond term propounded. a tilling is worth? Now the amoi tol 10, 10, 20,

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The Rule of Alligation. Car 24 d the ballel.

I. THE Rule of Alligation is that, by which we resolve Questions, that concern the mixing of divers simples together.

II. Alligation is either Medial or Alternate. III. Alligation Medial is when having the feveral quantities and rates of divers simples propounded, we discover the Allingian mean rate of a mixture compounded of those simples. So 10 bushels of wheat at 41. or (which is all one) 48 d, the bushel; 40 bushels

of rye at 3 s. or 36 d. the bushel; and 50 bushels of barley at 2 s. or 24 d. the bushel; being mixed

with 20 bushels of oats at 12 d.the bushel, the Rule of Aligation medial sheweth you the mean price of that milling.

The operations and proportions of the same Rule.

IV. In Alligation medial, first fum the given quantities, then find the total value of all the simples: this done, the proportion will be as followeth.

As the fum of the quantities is to the total value

of the simples :

So is any part of the mixture propounded to the required mean rate or price of that

part.

Repeating again the premised Example of the third Rule ; I demand how much one bushel of that missling is worth? Now the sum of 10, 40, 50,20, (the given quantities) is 120 bushels, and the value of the 10 bushels of wheat at 48 d. the bushel, amounts to 480 d. for 48 being multiplied by 10, the product is 480: again, the value of the 40 bushels of rye at 36 d. the bushel, is 1440 d. lue of the 50 bushels of barley at 24 d. the bushel, is 1200 d. And the value of 20 bushels of oats at 12.d. the bushel is 240 d. All these values being added together, their total is 3360 d. I say then by the Rule of Three Direct, if 120 bushels give 3360 d. what will I bushel yield? The Rule presently anfwers me 28 d whereupon I conclude, that a bushel of that milling may be afforded for 28 d. that is, 2 s. 4 d. which is the resolution of the Question propounded.

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In like manner if It be demanded what 8 Bushels or a Quarter of that Mistling is worth? The Answer will be 224 d. which being divided by 12, and by that means reduced into skillings, is 18 s. 8 d.

Barley, and Bow mail of the control of the color of the character of the character of the color
V. In Aligation Medial, the tryal of the Work is by comparing the total value of the feveral simples with the value of the the Proof. whole mixture: For when those sums accord, the operation is perfect; so in the first Example of the last Rule.

All which amount to 14-0-0 which is likewise the value of 120 Bushels at 28 d. or 2 s. 4 d. the Bushel, for that also amounts to 14 l.

VI. Alligation Alternate is, when having the feveral rates of divers Simples given, we discover such quantities of them, as are necessary to make a mixture, which may bear a certain rate propounded.

Example: A man being determined to mix 10 Bushels of Wheat at 4 s. or 48 d. the Bushel, with

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Rye of 3 s. or 36 d. the Bufhel , with Barley of 2 . or 24 d. the Buffel, and with Dats of 1 .. or 12 M. the Bushel the Rule of Alligation Alternate will discover unto you how much Rybar how much Barley, and how much Oats he ought to add unto the 10 Bushels of Wheat; in such fort that the mixture of them altogether may bear a certain rate or price propounded.

VII. In Queftions of Alligation Alternate, you must rank the terms in such fort to that The right orthe given rate of the mixture may redering of the present the root, and the several rates Terms. of the Simples may fland as branches

issuing from that root : So the Example of the last Rule being propounded, I demand how much Rye, Barley, and Oats, ought to be added to the 10 Bushels of Wheat, that the mixture of all together may bear ther ate or price of 28 d. or 2 s. 4 d. the Bushel : And therefore drawing a line of connexion, I place 28 d. the given rate of the mixture, upon the left hand thereof by it felf re-

presenting the Root, and likewise write 28 36 d. 24 d. and 12 d. one above another upon the right hand of that line

(12 of Connexion, which rates are con-

eeived to iffue from 28 d. as branches from the Root, the fabrick here of appears plainly

in the Margent.

VIII. Having ranked the terms in their due order, link the branches together by How to couple certain Arks, in fuch fort, that one the Terms. that is greater than the Root or rate of the mixture, may alwayes be coupled with ano. ther

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ther that is less than the fame. So in the premised Example, 48 may be linked with 12, and 36 with 24, or otherwise 48 may be coupled with 24, and 36 with 12, and then the Work will stand

Thus,
$$28 \begin{cases} 48 \\ 36 \\ 24 \\ 12 \end{cases}$$
 or thus, $\begin{cases} 48 \\ 36 \\ 28 \end{cases}$

IX. Having alligated the branches, and found the differences betwire them and the Root, write the differences of each branch just against his respective yokefellow. So the branches of the Example afore-going being linked after the first manner, and the difference between 28 and 48 (by the third or fourth Rule of the fourth Chapter of this Book) being 20, I place 20 just against 12, the respective yoke-fellow of 48. Again, 16 be-

ing the difference betwirt 28 and 12 . I write it

just against 48. In like manner 8 being the diffo-

place it right against 24. And lastly, 4 the difference betwixt 28 and 24, I write just against 36: In the end the whole Fabrick of the Work (as the branches are thus linked) will stand as in the Example.

 $\begin{array}{c|c}
 & 48 \\
 & 36 \\
 & 48 \\
 & 24 \\
 & 12
\end{array}$

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But

But the branches being linked after the other, manner, the Work will be thus disposed.:



For in this case 48 hath 24 for his yoke fellow, and the respective Comerado of 36 is 12; and here the interchangeable placing of the differences (as in the premised Examples) is that which is more

particularly termed Alternation.

X. When one branch is linked to divers other branches, and not to one alone, the differences ought to be as often transcribed, as it is so diversly linked. So in the premised Example, you may (if you please) conceive 12 to be coupled both with 48 and 36; likewise 24 may be conceived to be linked with the same 48, and 36; wherefore the difference betwixt 28 and 12 being 16, I write it both just against 48 and 36: In like manner the difference between 28 and 24, being 4, I write it likewise over against the same numbers 48 and 36. Again, 20 being the difference betwixt 28 and 48,

I place it just against 24
and 12; and 8 being the
local difference between 28 and
local diffe

this Performed, the whole frame of the Work will frand as in the Margent.

2. Take this for another Example : It is requi-

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red to mix 10 bushels of Wheat at 48 d. the bushel with Rye of 36 d. the bushel, with Barley of 24 d. the bushel, and with Oats of 12 d. the bushel, and the Question now is, How much Rye, Barley, and Oats ought to be added to the 10 bushels of Wheat, that the entire mixture may be afforded at 16 d. the bushel? Here the branches of this Question (according to the eighth Rule of this Chapter) ought to be linked thus,

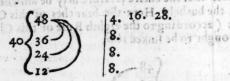


And as for the Alternation of the differences, it is evident (by the present Rule) that the difference between 16 and 12 being 4,0 ught to be thrice transcribed, viz. first just against 48, then against 36, and last of all against 24. Again, 32 the difference betwixt 16 and 48, as also 20 the difference between 16 and 36; and lastly, 8 the difference betwixt 16 and 24, ought all to be placed just against 12.

$$\begin{array}{c|c}
48 \\
36 \\
24 \\
12
\end{array}$$

3. I determining to mix to bushels of Wheat at 48 d, the bushel, with Rye of 36 d, the bushel, with Barley of 24 d, the bushel, and with Oats

of 12 d. the Bushel, desire to know how much of each I ought to take, that I might afford the whole mixture at 40 d. the Bushel: Here the whole Work being ordered according to the Rules aforegoing, it will stand as followeth.



4. A man intending to mix 10 Bushels of Wheat at 48 d. the Bushel, with Rye of 36 d. the Bushel, with Barley of 24 d. the Bushel, with Pease of 16 d. the Bushel, and with Oats of 12 d. the Bushel, desires to know how much Rye, Barley, Pease, and Oats he ought to add to the 10 Bushels of Wheat, that the whole mass of Corn so mixed might be afforded at 20 d. the Bushel? This Question being thus propounded, the terms thereof (by the Rules aforegoing) may be Alligated, and the differences of the terms Alternated, as followeth.

(48	4. 4. 4. 8. 28. 16. 4.
36	4.
20 24	4. 8. 08
116.	28. 16. 4.
(12)	4.

5. Lastly, A Goldsmith hath some Gold of 24 Caretts, other of 21 Caretts, and other some of 19 Caretts fine, which he would so mix with Alloy, that 192 Ounces of the entire mixture might bear

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17 Carects fine; now the Question is how much of each fort, as also how much Alloy he must take to accomplish his delire? Before you

can well understand this Question, it fine, and what will be necessary to explain what a Alloy is a o Tom

Carett fine, and what Alloy is: the

Mint-Masters and Goldsmiths to distinguish the different fineness of Gold, esteem an entire ounce to contain 24 Caretts, and one ounce of Gold that being tryed in the fire loferh nothing of the weight, is faid to be 24 Carelle fine : again, the ounce that being tryed lofeth one four and twentleth part of the weight, is faid to be 23 Carells fine: In like manner that which lofeth two four and twentieth parts of the ounce, is effeemed to be 22 Careds fine, and fo confequently of the reft : And as for Alley it is filver, copper, or fame other bafer mertal, with which the Goldfmiths ufe to mix their Gold, to the intent they may moderate, or abate the finenefs thereof. Here you may also observe, that as the fineness of Gold is meafured by Carelly, To is the finenels of Silver estimated by ounces: In fuch fort that a pound of Silver, which being tryed a certain time in the fire, lofeth nothing of the weight, is faid to be 12 ounces fine. But a pound that being tryed lofeth fomewhat of the weight, is faid to be the remainder of the weight fine. Example ; a pound of Silver that loseth in the fire one ounce 8 p. is estimated to be 10 ounces 12 p. fine, and that which lofeth 2 ounces 8 p. 10 grains, is said to be 9 ounces, 11 p. 14 grains fine, &c. Now to rank the terms of the last mentioned Question, as also the differences of the terms in their due order, because the three given branches (viz. 24 Carects.

Caretts, 21 Caretts, and 19 Caretts) are all greater than 17 Caretts the root or rate of the mixture. I adde 0 as another branch which I conceive to be less than the root, and then proceed as in the former operations; the whole frame of the Work is expressed here, as followeth:

$$17\begin{cases} 24 \\ 21 \\ 19 \\ 0 \end{cases} \qquad \begin{vmatrix} 17 \\ 17 \\ 17 \\ 7.4.2. \end{vmatrix}$$

XI. When in one and the fame line there are found more differences than one, add them together, and write the fum just against the same differences before a straight line drawn towards the

right hand of the Work.

So the first Example of the last Rule being propounded, the sum of 16 and 4 (the differences placed just against the first branch) being 20, I write it over against the same differences, before the new line drawn upon the right hand of the Work, and so consequently the rest in their due order, as appears by the Example hereunto annexed.

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In like manner the last Example of the last Rule being offered, the whole Fabrick of the Work will stand, as followeth:

(24	17	17
	17	17
17 21	7.4.2.	13

XII. Alligation Alternate is, either Partial, or Total.

AIII. Alternation Partial is, when having the several rates of divers Simples, and the quantity of one of them given, we discover the several quantities of the Partial. rest, in such fort that a mixture of those Simples being made according to the quantity given, and the quantities so found, that mixture may bear a certain rate propounded: Of this kind is the Example of the fixth Rule, as also all the Examples of the tenth Rule, except the last.

XIV. In Questions of Alternation Partial, the proportion is as followused in this ship this call.

As the difference annexed to the first branch is to the feveral differences of the rest:

So is the quantity propounded to the feveral

quantities required.

So the Example of the fixth and feventh Rules of this Chapter being again repeated, and the terms thereof, as also the differences of the terms being ordered after the first manner (shewed you in the ninth Rule aforegoing) it is evident that for

The first 28 \(\begin{pmatrix} 48 \\ 36 \\ 24 \\ 12 \end{pmatrix} \]

for every 16Bulk-16 els of Wheat that 4 I take in the mix-8 ture, I ought to take 4 Bulhels of Rye, 8 Bulhels of

Barley, and 20 Bushels of Oats 5 and therefore I

I. As 16 the difference annexed to the first branch (being the rate of the Wheat) is to 4 the difference annexed to the next, being live the rate of the Rye; so is 10 the given quantity of the Wheat to another number, which being found by the Rule of Three direct, to be two Bushels and an half (or two pecks) is the quantity of Rye necessary in the mixture.

II. As 16 to 8, so is 10 to another number, which being likewise found by the Rule of Three to be five Bushels, is the quantity of

Barley, necessary in the mixture.

III. As 16 to 20, so is 10 to another number, which being in like fort found by the Rule of Three to be 12 Bushels, and half of a Bushel is the quantity of Oats requisite in the mixture.

So that at last I conclude, a heap of Corn being composed of 10 Bushels of Wheat, 2 Bushels and a half of Rye, 5 Bushels of Barley, and 12 Bushels and an half of Oats (when those several Grains bear the prices aforesaid) may be afforded at 2 s. 4 the Bushel.

The same Example being ordered after the second manner (expressed likewise in the 9th Rule of this present Chapter) I say;

I. As

1. As 4 the difference annexed to the rate of the wheat, is to 16 the difference annexed to the rate of the rye; so is 10 the given quantity of the wheat, to 40 bushels the required quantity of the rye.

II. As 4 to 20, fo is 10 to 50 bulbels, the re-

quisite quantity of the barley.

III. As 4 to 8, so is 10 to 20 bushels, the quantity of the oats necessary in the mixture.



So that I conclude again, a mass of Corn being compounded of 10 bulliels of wheat, 40 bushels of rye, 50 bushels of barley, and 20 bushels of oats, (when those Grains bear the prices propounded in this Example) may be afforded at 25. 4 d. the bushel as before.

3. That Example being disposed after the third manner (expressed in the tenth and eleventh Rules of this Chapter) I say,

I. As 20 the sum of the differences annexed to the rate of the wheat, is to 20 the sum of the differences annexed to the rate of the rye; so is 10 the given quantity of the wheat, to 10 bushels the required quantity of the rye.

II. As 20 to 28, fo is 10 to 14 bushels the re-

quisite quantity of the barley.

III. As 20 to 28, fo is 10 to 14 bushels, the quantity of oats demanded in the mixture.

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28 \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\	16.4 20.8 20.8	28

Whereupon this third time likewife I conclude, that (those Grains still retaining the given rates) 10 bushels of Wheat, 10 bushels of Rye, 14 bushels of Barley, and 14 bushels of Oats being all mixed together, will constitute a mass of Corn, that may

be afforded at 28 d. or 2 s. 4 d. the bushel.

By this Example thus diversified it plainly appears, that the quantities required may be altered as often as the Question given will admit divers Alligations, and yet the mixture produced will still hold the rate propounded; but when the Question propounded will admit but one only way of Alligation, the quantities required to make the mixture, cannot be varied; so the second Example of the tenth Rule of this Chapter, being again produced, and ordered according to the direction of the eleventh Rule aforegoing, Isay,

I. As 4 to 4, so 10 to 10 bushels of Rye.

II. As 4 to 4, so 10 to 10 bushels of Barley.

III. As 4 to 60, so 10 to 150 bushels of Oats.

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So that for this Question I conclude, to 10 bunshels of wheat you ought to add 10 bushels of eyes 10 bushels of barley, and 150 of oats, to the end that a mixture of Corn might be made, which may be fold at 16 d. the bushel: And here the quantities found (viz. 10, 10, and 150) cannot be altered, because the terms of this Question will not admit any other variety of Alligation.

XV. In Alternation Partial, the proof is likewife

by comparing the total value of the

feveral simples, with the value of the the Prof.

whole mixture : So in the fecond

example of the last Rule, the total value of the robushels of wheat, 40 bushels of are, 50 bushels of barley, and 20 bushels of oats amounts to 141, which is also the value of the whole mixture at 25.44. the bushel, as appears by the example of the fifth Rule of this present Chapter.

XVI. Alternation total is, when having the to-

tal quantity of all the simples toge-

ther with their feveral rates, we Alternation

produce their feveral quantities, in soral.

fuch fort, that a mixture of them being made according to the quantities so found,
that mixture may bear a certain rate propounded:
Of this fort is the last example of the tenth Rule
aforegoing; as also this, a Goldsmith having divers forts of Gold, viz. some of 24 Carects, other
of 22 Carects, some of 18 Carects, and other some
of 16 Carects fine, is desirous to melt of all these
sorts so much together, as may make a mass containing so ounces of 21 Carects fine: Now this
Rule of Alternation total shewesh you how much you
are to take of each sort, to the end the whole mass

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the balled :: the dranti--Marhe fum of all the differences is to the total quantity of all the simples so is the correfpondent difference of each rate to the re-

spective quantity of the fame nate.

So the laft example of the laft Rule being propounded, Ifly, look

ned Ifb, lossly said or signal larges.

I. As 12 the fum of the differences is to 60 Qunces the road quantity of all the simples: 10 is the conrespondent diffenence of ,24 Carects the first rate, to 25 dunces, was, the required quantity of the Gold of the fame rate, which may be taken to make the mixture propoun-

TH. As 12 to 60, fo is 3 the correspondent difference of 22 Carecis the fecond rate, to 15 ounces, viz. the quantity of the Gold of 22 Carects, that ought to be used in the mixture. III. As 12 do 60; fois 1 to 5 ounces of the

Gold of 18 Carects fine . anbros

TV. As 12 to 60, fo is 3 to 15 ounces of the Gold of no Carects fine, which are requilite to be taken for the mixture propounded.



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whereupon Limited, that 25 ounces of 24 Carects fine, its ounces of 22 Carects, 5 ounces of 28 Carects, and 15 ounces of 16 Carects fine, being all melted together will produce a mass of Gold containing 60 ounces of 21 Carects fine, which is the resolution of the Reastion propounded.

Again, the last Example of the tenth Rule being there irepeated, and ordered according to the di-

irection of the deventh Rule, Ifay, diagos babbs

I. As 64 to 192, fo is 17 to 51 ounces of 24 64-

II. As 64 to 192, fo is 17 to 51 ounces of 27 Carecte fine. . VX . A H D

Carects fines. fo is 17 to 31 ounces of 19

IV. As 64 to 192, fo is 13 to 39 ounces of Alley.

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And therefore for conclusion I say; that 31 ounces of Gold, 24 Carects fine, 31 ounces of 21 Carects fine, 31 ounces of 19 Carects fine, and 39 ounces of Alloy being all mixed together, will produce mass containing 192 ounces of Gold, 17 Carects fine, which is the fatisfastion of the question premised.

And here observe (as before in the Exposition of the fourteenth Rule of this Chapter) that the operations of the first of these Examples may be married according to the diversity of the Aligarians

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which it will admir, whereas the last Example is not subject to any variety, the Alligations thereof remaining alwayes the same.

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WIII. Here the operation is perfect, when the fum of the quantities found agrees So in the first Example of the last Rule, 25, 35, 5, and 15 (the quantitles found) being all added together amount to 60, which is the total I. As 64 to 192, fo is 17 bennoquequeque I.

II. As 64 to 192, 10 is 17 to 51 0 mccs of 21 CHAP. XV. san about

rects fine.

. III. As 64 to'192, fo is 17 to 51 cunces of 19

The Rule of Falfer from VIV. As on to 192, Out of 192,

I. THE Rule of False, is alwayes performed by false and suppositivial pumbers taken at pleafure after the Proposition is prade, and the Que-Rion propounded; for thing are faid to be found out by the Rule of False, when by false terms sup-posed, we discover the true terms required.

II. The Rule of Falle, is either of fingle or

double polition al In afferno is to as Illio The Rule of Tingle polition is, The Rule of when at once, viz, by one falle polition fincle Polition. we have means to discover the true refolution of the Question propounded.

For Example: A, B, and C, determining to buy together a certain quantity of Timber, that should coft them 36 1, agree amongst themselves that B shall pay of that sum a third part more than A, and that C shall pay a fourth more than B. Now the Question is, What particular sum each of these parties

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parties ought to pay of the 36 l. To resolve this Question; first, put the case that A ought to pay 61. of the 36 l. and then B must pay 8 l. because he pays one third part more then A. And lastly, C ought to pay 10 l. because he is to lay out one fourth part more then B. This done, although by addition of these three sums, via. 6, 8, and 10, I find that I have made a wrong Position (their total amounting onely to 24 l. which ought to have been 36 l. I nevertheless by those suppositions Nums bers, I have means to discover the true sums which the several parties ought to pay: for I say by the Rule, of Three Direct.

I. As 24 to 36, fo is 6 to 91. the part that A must pay,

II. As 24 to 36, fo 8 to 12 L, the part that B ought to pay.

III. As 24 to 36, fo is 10 to 15 l. the part of the 36 l. that C'must pay.

total of the sums found ought to accord with the sum given: So in the Example of the last Rule, 9, 12, and 15 being all added together amount to 36, the sum propounded.

When two falle Positions are supposed the Rule of for the resolution of the Question propounded. As in this, A Workman having thresht out 40 quarters of Grain (part thereof being Wheat, and the rest Barley) received for his labour 28 s. being paid after the rate of 12 d. for every quarter of Wheat, and 6 d. for each quarter of Barley: Now here the question is, how many of those 40 quarters were Wheat, and

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how many Barley? Here therefore I first suppose at random, that there was 26 Quarters of Wheat, and 14 of Barley, and then to discover whether I have gueffed right or wrong, I find how much money is due unto the Workman at the rate of 12 d. the Quarter of Wheat, and 6 d. the Quarter of Barley, which I find to be 33 s. (viz. 26 s. for the 26 Quarters of Wheat, and 7 s. for the 14 Quarters of Barley) which he ought to have received, if my supposition had been right; but because it differs from 28s. the true fum that he received, I perceive I have mist the mark, and therefore difcovering how much I have err'd by finding the difference betwixt 28 s. and 33 s. I keep in mind T their difference, which is called the first error, or the error of the first Position : Again, I propound for the fecond Position, that there was 30 Quarters of Wheat, and 10 Quarters of Barley; and then the fecond error I find to be 7; for there is then due to the Workman for the 30 Quarters of Wheat 30 s. and for the 10 Quarters of Barley 5 s. in all 35 s. which differs from 28 s. the true fum that he received, by 7 s. and here by thefe two falle Politions, together with their errors, you may discover how many Quarters of Wheat, and how many of Barley the Workman threfit, as shall be farther explained by the Rule following.

The Operation. WI. In the Rule of double Position having drawn two lines acros, and placed the terms of the false Position

(viz. those that have the same Denomination) at the uppermost end of that Cross, as also each error under his respective Position at the lower end of the same Cross, multiply each error by the contrary Position a

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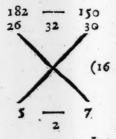
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Position; that is, the second error by the first Position, and the sirst error by the second Position; this done, when both the errors are of one and the same kind, (viz. both excesses or both defects) subtract the less Product out of the greater, and then the remainder is your Dividend; but if the errors be of differing kinds, (viz. one of them an excess, and the other a defect) add those Products together, and then the sum will be your Dividend, which if you divide by the difference of the errors, (when they are of one and the same kind) or by their sum (when they are of different kinds) the Quotient will give you a number you look for, having the same Denomination with the false Positions placed at the upper end of the Cross.

again propounded, I place these terms, viz. 26 (having the Denomination of the Quarters of Wheat in the first Position) and 30 (having the same Denomination in the second Position) at the upper end of the Cross: As also 5 and 7 the two errors respectively under them at the lower end of the same Cross, as you may see it exemplified by

the Pattern following.



Mote that this Charafter—fignifies that the lefter of the two Numbers, betwitt which it is found, oughs to be subtra-ded from the greater.

This done, having multiplyed 26 by 7, the product is 182, and likewise 30 by 5, the product is 150, which being deducted out of 182 (because the errours here are both of the fame kind, that is, are each of them an excess above 28 s. the summe that the workman received) the remainder is 32, which being divided by 2 (the difference betwixt 5 and 7 the two errours) leaves in the Quotient 16, for the quarters of Wheat that the workman thresht, whose complement to 40 viz. 24 are the quarters of Barley, that he likewise thresht : so at last I conclude, the Workman receiving 28 s. for his wages in threshing out 40 quarters of Grain (being part Wheat, part Barley) at 12 d. the quarter of Wheat, and 6 d. the quarter of Barley, threshed in all 16 quarters of Wheat, and 24 quarters of Barley.

2. Example. The same Question being again propounded, I suppose for my first Position that there are 8 quarters of Wheat, and 32 quarters of Barley, and then the first errour will be 4 s. for 8 s. being accompted for the 8 quarters of Wheat, and 16 s. for the 32 quarters of Barley, make in all 24 s. which wants 4 s. of 28 s. the fum received: Again, Supposing that there are 12 quarters of Wheat, and 28 quarters of Barley, the second errour will be 2 s. for 12 s. being allowed for the 12 quarters of Wheat, and 14 s. for the 28 quarters of Barley, the fum is 26 s. which comes 2 s. Thort of 28 s. the right fum: now then 8 being multiplyed by 2, the Product is 16; likewise 12 by 4 produceth 48, out of which if you deduct 16 (because the errours in this case happen to be both defects under 28 s. the fum received) the remainder is 32, which being

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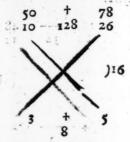
being divided by 2 (the difference of the errours) gives you in the quotient 16, viz. the quarters of Wheat, as before.



3. Example. The same demand being the third time produced, I take for my first Position 10 quarters of Wheat, and 30 quarters of Barley, and then proceeding as before, the first errour will prove 3 ... which upon that Position, I want of 28s. the right fum : Again here for the fecond Position I take 26 quarters of Wheat, and 14 quarters of Barley, and then the second errour will be 5 s. which upon that Position I have exceeded 28 s. the true fum : now then multiplying 10 by 5, the Product is 50, and 26 by 3, the Product is 78 : And here (because the errours are of different kinds, one of them being a defect, and the other an excess of 28 s, the true fum) you are to add 50 and 78 the two Products together, whose sum is 128, which being divided by 8, the fum of 3 and 5 the two errours, gives you in the quotient 16 for the quarters of Wheat, as before in the former resolutions. So that what Positions soever you take in this Question, you shall alwayes find, that the Workman threshed 16 quarters

ters of Wheat, and 24 quarters of Barley, which is the resolution of the Question propounded.

Mote that this (barafter + intimates that the Numbers, betwint white it found, aught to be addit together.



VII. Here the trial is the same with that which is used in finding out the errours: So in the Example premised 16 and 24 being the numbers found, and 16 s. being allowed for the 16 quarters of Wheat, likewise 12 s. for the 24 quarters of Barley, their summe is 28 s. which was the summe

received by the Workman.

4. Example. A certain man being demanded what was the age of each of his 4 Sons? Answered, that his eldest Son was 4 years elder then the second; his second Son was 4 years elder then the third; his third son was 4 years elder then the fourth or youngest; and his sourth or youngest, was half the age of the eldest; the Question is, what was the age of each Son? Here I guesse the age of the eldest Son to be 16, then it may be inferred from the Question, that the age of the second Son was 12, the age of the third 8, and the age of the fourth or youngest 4, this 4 should be half 16 (for the Question saith, that the age of the youngest was half the age of the eldest) but it wants 4 of what it ought

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ought to be : wherefore I make a second Polition. and take 20 for the age of the oldeft, then the age of the second must necessarily be 16, the age of the third 12, and the age of the fourth 8, which should be half 20, but it wants 2: now (according to the Rule) multiplying 16 (the first Position) by 2 (ithe fecond errour) the product is 32, also multiplying 20 (the

fecond Polition) by 4 (the first errour) the Product is 80, and because the errours are both of one kind, to wit, both defedives I fuberact the leffer Product from the



greater, fo the remainder is 48 for a Dividend. alfo fubtracting the leffer errour from the greater, the remainder is 2 for a Divifor : Laftly, dividing 48 by 2, the quotient is 24, and fuch was the age of the eldeft Son, therefore the age of the fecond was 20; the age of the third 16, and the age of the fourth 12, which is half the age of the eldelt. as was declared by the Question.

The Doctrine of Vulgar Fractions.

CHAP. XVI.

Notation of Vulgar Fractions.

I. Thus far of Arithmetick in whole numbers only, the doctrine of Fractions ensueth, which depends upon this supposition, that Unity, or at least one whole thing, whatsoever it be, may in mind be conceived divisible into any number of equal parts: some will not allow 1 or unity to be a number, when it is considered in the Abstract, and separated from matter, but for a smuch as that Prince of Arithmeticians Diophaneus of Alexandria, in divers of his subtil Problemes doth mention unity as a number, and propounds it to be divided into numbers, I shall take the like liberty to esteem 1 or unity as a number, and likewise suppose it divisible into any number of equal parts.

II. A broken number, otherwise called a Fraction, is only part of an In-

teger or whole thing, as if you would express in figures the length of a piece of cloath, that contains three fourths, or (which is all one) three quarters of a yard, you are to write it thus 1, that is, an entire yard being supposed to be divided into four equal parts, the length of the piece propounded

pounded is three of those four parts. In like many ner (a Foot being divided into 12 inches) you must write six inches thus that is, fix twelfth parts of a foot; or if the foot be divided into one hundred equal parts, to express five and twenty of those parts, set them down thus to that is five and twenty hundredth parts of a foot.

III. A Fraction confifts of two parts, the Nulmerator and the Denominator, which are placed one above the other, and separated by a little line.

the line, and the Denominator is the number placed underneath: so in 3 Numerator, the aforementioned Fraction 3 the 4 Denominator number 3 placed above the line is the Numerator, and the number 4 placed underneath is the Denominator. Also in this Fraction 3 the Numerator is 6, and the Denominator is 12. The Denominator is so called, because it denominates or declares into how many equal parts the Integer or whole thing is supposed to be divided, and the Numerator is so called, because it numbreth or expressent how many of those equal parts of the Integer are signified by the Fraction.

V. A Fraction is either proper or improper.

VI. A proper Fraction is that whose
Numerator is less than the Denominator, such are the Fractions before-mentioned $\frac{3}{4}$ $\frac{6}{12}$, $\frac{25}{100}$ and the like.

VII. A proper Fraction is either fingle or com-

VIII A fingle Fraction is that which A fingle consists of one Numerator, and one Fraction.

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Denominator; fuch are 1 12 and the like, IN A fingle Fraction doth often arife in Divifion of whole numbers, for when Division is finisht, if any number remain, it is to be esteemed as the Numerator of a Fraction, which hath the Divisor for a Denominator, and is to be annexed to the Integer or Integers in the quotient as part of the quotient; which Fraction doth always express certain parts, or at least a part of an Integer or entire unity, which hath the fame denomiposion with one of the Integers in the quotient; fo if 17 pounds be given to be divided equally amongh sperions, there will arife 3 entire pounds in the quotient, and there will be a remainder or furplulage of 2 pounds, which 2 is to be placed as the Numerttor of a Frathen; over the Divilor's as a Denominator, To will the Frattion be and the complexe quotient will be 3%, that is three pounds and two fitch parts of a pound for each persons thane. Daniel Late for called . .

Mingle Fraction doth likewise arise, when a bester whole number is given to be divided by a greater, for insuch case the Dividendistro be made the Numerator of a Fraction, and the Division the Denominator, which fraction is their nee quotient, and doth always express certain parts (or at least a part) of an Integer; which hath the same name with the Dividend: so if 3 pounds sterling be given to be divided equally amongst 4 Persons, the share of each, that is, the quotient will be 3, to wit, three fourth parts of a pound; in like manner, if 5 be given to be divided by 8, the quotient is 1, so that the Numerator of a Fraction is alwaysed Dividend, the Denominator is a Divisor; and the Fraction it self is the austient.

W.A Compound Fraction (otherwise called a Fraction of a Fraction) is that which hath more Numerators and

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Denominators than one, and may be discovered by the word [of] which is interpos'd between the parts of fuch compound Fraction: fo of is a Fraction of a Fraction, or compound Fraction, and expresseth two thirds of three fourths of an Interer, viz. a pound sterling being supposed the Inreger, and first divided into four parts, three of those four parts are equal to 15 s. Again, if the faid 15 s. be divided into three parts, two of those three parts are equal to 10 s. therefore the compound Fra-Stion of a of a pound fterling doth express jos. In like manner the compound Fraction of 1 of of a pound sterling, that is, one fourth of three fourths of four fifths of a pound fterling doth exprefs 3 s. as will be farther manifest by the fixteenth and ninth Rules of the seventeenth Chapter.

XI. An improper Fraction is that, whose Numerator is either greater; or Fraction.

at least equal unto the Denominator:

10 this Fraction 15 that is sixteen fourths, is called an Improper Fraction, and so is this 2 for indeed a Fraction of this kind may well be surnamed Improper, because it will not admit the definition of a crue Fraction, since it is always greater than an entire unity, or at least equal unto it; so sixteen Fanthings, or 15 of a penny are equal to 4 entire pence, and 4 Farthings, or 4 of a penny are equal to 1 penny; therefore when the Numerator is greater than the Denominator, such improper Fraction signifiest more then 1 or an Integer, but when the Numerator is equal to the Denominator

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(be it what number foever) fuch improper Fraction is alwayes equal to unity, or I Integer.

XII. A mixt number is that, which a miss besides the Integers or entire unities, of mamber. which it consists, hath also a Fraction annexed: So if you would express in Figures a length of a piece of Timber, that contains 12 foot and half a foot, you are to write it thus 12½ foot. In like manner 7 Miles and three quarters or fourths of a Mile are to be written thus 7½ Miles.

XIII. A mixt number hath two parts, the whole or integral part, and the broken or fractional part; so in this mixt number 12\frac{1}{2}, the number of Integers. 12 is the integeral part, and the Fraction \frac{1}{2}\frac{1}{2}

the Fractional part.

CHAP. XVII.

Reduction of Vulgar Frattions.

I. The same parts of Numeration, as have been wrought in whole Numbers in the preceding Chapters are likewise to be performed in fraction, but first of all Reduction of Fractions in divers kinds must be known, which being the principal skill in the doctrine of Fractions, must be diligently observed by the Learner.

II. A number is said to be a common Measure or Divisor unto two or more numbers given, when it will measure or divide every one of the numbers given, and leave no remainder, so 4 is a common measure unto the numbers 12 and 20; for if 12 be divided by 4, the Quotient will be exactly 3,

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without any remainder or surplusage, also if 20 be divided by the same Divisor 4, the quotient will be precisely 5 without any remainder; in like manner 5 is a common Divisor unto these three numbers 10,25 and 40.

their greatest common Divisor (that is, the greatest number which will measure or divide each of the numbers given without leaving any remainder) may be found in this man-

To finde the greatest common measure unto any two numbers.

ner, viz. Divide the greater number by the lefs, then divide the last Divisor by the remainder, (if there be any) and so continue dividing the last Divisors by the remainders until there be no remainder, (neglecting the quotients) so is the last Divisor the greatest common Divisor unto the numbers given.

Thus, if the greatest common Divisor unto the numbers 91 and 117 be sought, divide the greater

numbers 91 and 117 be lought, number 117 by 91, so the remainder is 26, by which dividing 91, the remainder is 13, by which dividing 26, the remainder is 0; so is 13 the greatest common Divisor unto the numbers 117 and 91, as is manifest in dividing each of them by 13; for 13 is found in 91 precisely 7 times, and in 117 precisely 9 times.

IV. A fingle fraction may be reduced into the least terms, by dividing the Numerator and Denomi) 117 (1 91 26) 91 (3 78 13(26 (2 26

To reduce a Eration into the least terms, viz. 1. By a general Rule.

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nator by their greatest common measure, for the quotients will be the Numerator and Denominator of a fraction equal to the former, and in the least terms.

So if the fraction 91 be given to be reduced in. to the least terms, find the greatest common Divisor unto 91 and 117 by the last Rule, which will be found 13, and then dividing 91 by 13, the quotient will be 7 for a new Numerator ; also dividing 117 by 13, the quotient will be o for a new Deno. minator, fo is the fraction of reduced into the least terms, viz. into the fraction ? : but here you are to observe, that if the greatest common Divisor unto the Numerator and Denominator be 1, fuch Fraction is in its least terms already, so the fraction annot be reduced into lower terms, because the greatest common Divisor will be found 1, (by the third Rule of this Chapter) the like may happen of infinite others: and although the last be a general Rule for the Reduction of Fractions into their leaft terms, yet there are other practical Rules, which in fome cases will be more ready; (especially unto beginners) viz.

V. When the Numerator and De2. By particunominator are even numbers, they
lar Rules. may be measured or divided by 2.
Therefore in such case you may (as is taught in
the Rules of the 6th Chapter) take the half of the
Numerator for a new Numerator, also the half
of the Denominator for a new Denominator. So

if 16 be given, draw at length the line which separates the Numerator from the Denominator, and

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cross the same with a downright stroke near the Fraction, as you may see in the Margent, then take the half of 16, which is 8, for a new Numerator, also the half of 64, which is 32, for a new Denominator; Again, the half of 8 is 4, for a new Numerator, also the half of 32 is 16, for a new Denominator, and proceeding in like manner, there will be found 4, equivalent unto 66.

VI. When the Numerator and Denominator do each of them end with 5, or one of them ending with 5, and the other with a Cypher, they may be both measured or divided by 5: So 225 will be reduced into 3/475 |95 | 19 and 40/425 into 2/17 as by the operation in the Margent is manifest.

in the Margent is manifest.

VII. Whenfoever you can efpy any other number, which will exactly mean

other number, which will exactly measure the Numerator and Denominator, (although it be not the greatest common measure) you may divide the Numerator and Denominator by such number as before: So we may be first 28 7 1 reduced into 1 by 4, and 1 may be reduced into 1 by 7 as by the operation is manifest.

VIII. When the Numerator and Denominator do each of them end with a Cypher or 4100 Cyphers, cut off equal Cyphers in both, fo will the fraction be reduced into leffer terms; So 400 is reduced into 4, and 700 oo 500 into 2.00 into 2.00 into 2.00 into 2.00 oo 500
IX. The value of a single fraction in the known parts of the Integer.

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of the Integer, may be found in this manner, viz. multiply the Numerator of the fraction propounded, by the number of known parts of the next inferiour denomination which are equal to the Integer, and divide that product by the Denominator, so is the quotient the value of the fraction in that inferiour denomination, and if there happen to be any fraction in the quotient, you may find the value thereof in the next inferiour denomination, by the same Rule, and so proceed till you come to the least known parts.

So the value of of a pound ferling will be found 11 s. 3 d. viz. multiply the Numerator 9, by 20 (the number of shillings which are equal to a pound ferling) the product is 180, which being divided by the Denominator 16, the Quotient is 11 -4 shillings. In like manner, the value of of a shilling will be found 3 pence, for multiplying the Numerator 4 by 12, (the number of pence in a shilling) the product is 48, which being divided by the Denominator 16, the quotient is 3 pence.

Also the value of $\frac{3}{7}$ of a pound sterling, will be found 10 s. 9 $\frac{3}{13}$ d. And $\frac{37}{90}$ of a pound Troy will be found equivalent unto 3 ounces 17 penny weight and 12 grains.

X. A mixt number may be redu-To reduce a mixt ced into an improper fraction equinumber into an improper Fradivalent unto the mixt number, in this manner, viz. Multiply the Integral part of the mixt number, by the Denominator of the fraction annexed to the Integers, and unto the Product add the Numerator of the said fraction, fo is the sum the Numerator of an improper fraction, whose Denominator is the same with that of the faid fraction annexed.

So 4 " will be reduced into the improper fra-Cion 39 for 4 being multiplyed by 12, the Product is 48 unto which adding the Numerator 11, the fum is 59 for a new Numerator, which being placed over the Denominator 12, gives the improper fraction 39 which is equivalent unto 411 (as will appear by the 13th Rule of this Chapter.) Inlike

manner 7 will be reduced into 15

To reduce a zoholo XI. A whole number is reduced number into an into an improper fraction, by plaimproper fraction cing the whole number given, as a Numerator, and 1, as a Denominator.

So 14 Integers will be reduced into the improper. fraction 14 and one Integer into the improper fra-

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XII. A whole number is reduced into an improper fraction which shall have any Denominator assigned, in multiplying the whole number given, by the Denominator affigned, and placing the Product as a Numerator, over the faid Denomina. tor.

So if 13 be given to be reduced into an improper fraction whose Denominator shall be 4, multiply 13 by 4, so is the Product 52, which being placed over 4, gives the improper fraction 52 equivalent unto 13, (as will appear by the next Rule) in like manner 13 may be reduced into 91

To reduce an improper fradion into its equivalent whole or mixt number. kIII. An improper fraction may be reduced into its equivalent whole number or mixt number, in this manner, viz. divide the Numerator by the Denominator, so is the quotient the whole number or mixt number sought; So the improper fracti-

on 32 will be reduced into the mixt number 4 1 for if 50 be divided by 12, the quotient is 4 1 Also the improper fraction 32 will be reduced in-

to the whole number 13.

To reduce frallions to a common denominator, viz. I. When two frallions are propounded. XIV. Fractions having unequal Denominators, may be reduced into fractions of the same value which shall have equal Denominators, by this Rule and the next following, viz. when two fractions

having unequal Denominators are propounded, to be reduced into two other fractions of the same value which shall have a common Denominator, multiply the Numerator of the first fraction, (that is, either of them) by the Denominator of the second, so is the Product a new Numerator (correspondent unto the Numerator of that first fraction,) also multiply the Numerator of the fecond fraction by the Denominator of the first, so is the Product a new Numerator (correspondent unto the Numerator of the second fraction) lastly, multiply the Denominators one by the other, so is the Product

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Product a common Denominator to both the new Numerators.

Thus if the fractions $\frac{1}{3}$ and $\frac{4}{5}$ be propounded, multiply 2 by 5, so is the product 10 for 2 new Numerator correspondent unto 2 $\frac{4}{2}$. also multiply 4 by 3, so is the product 12, which is a new Numerator 3 $\frac{5}{3}$ correspondent unto 4: lastly, multiply 10 $\frac{12}{3}$ by 5, so is the product 15, which $\frac{12}{3}$ by 5, so is the product 15, which $\frac{12}{3}$ shall be a common Denominator unto the new Numerators, so the fractions $\frac{12}{3}$ and $\frac{12}{3}$ are found which have equal Denominators and each of these new fractions is equal unto its correspondent fraction first given, viz, $\frac{1}{15}$ is equal unto $\frac{2}{3}$ and $\frac{12}{15}$ is equal unto $\frac{4}{5}$ (as will be manifest by the 4th Rule of this Chapter.)

AV. When three or more fractions which have unequal denominators, are given to be reduced as in the last Rule, multiply the Numerator of each fraction and all the denominators excepting its own continually, so are the several products arising from such continual multi-

2dly. When 3, or more fractions are propounded. See contimulational Multiplication in the 13 Rule of the 5. Chapter.

plication, new Numerators; Lastly, multiply all the denominators continually, so is the Product a common denominator to all the new Numerators.

denominators, are given to be reduced into three other fractions of the same value, which shall have equal denominators, multiply the Numerator 3, into the denominators 5 & 7 continually (according to the 13th Rule of the 5th Chapter;) so is the product

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105; also multiply the Numerator 2, into the denominators 8 and 7 continually, so is the product 112; in like manner multiplying the Numerator 5, into the denominators 8 and 5 continually, the product is 200, which 3 products are 3 new Numerators; Lastly, multiply all the denominators 8, 5, and 7 continually, so is the product 280, which is a common denominator to all the new

Numerators; thus the fractions $\frac{165}{280}$ $\frac{3}{2}$ $\frac{2}{5}$ $\frac{5}{7}$ $\frac{712}{280}$ and $\frac{700}{280}$ are found, which have equal Denominators, and each of these new fractions is equal unto its

correspondent fraction first given, viz. $\frac{105}{2.00}$ is equal unto $\frac{3}{8}$ $\frac{112}{280}$ is equal unto $\frac{2}{3}$ and $\frac{200}{280}$ is equal unto $\frac{3}{4}$ as will be manifest by the fourth Rule of this Chapter.

Note. Sometimes the Work of the two last mentioned Rules may be perform'd more compen-

diously by this following Rule, viz.

When the unequal Denominators of two Fradions have a common Divisor, divide the Denominators severally by their greatest common Divisor, (found out by the fore-going third Rule of this Chapter,) and then multiply cross-wise in this manner, viz. the Numerator of the first Fradion by the latter Quotient, and the Numerator of the latter Fraction by the first Quotient, and reserve the Products for new Numerators; Lastly, multiply the Denominator of the first Fraction by the latter Quotient, (or the Denominator of the latter Fraction by the first Quotient,) so shall the Product be a common Denominator to the said new Numerators: As for example, if \(\frac{1}{212} \) and \(\frac{1}{28} \) kI.

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be proposed to be reduced to a common Denomi. nator, I divide each of the Denominators 12 and 18 by their greatest common Divisor 6, and the Quotients are 2 and 3; then I multiply 5 the Numerator of the first Fraction by 3 the latter Quotient, also 7 the Numerator of the latter Fraction by 2 the first Quotient, and the Pro. 15 ducts 15 and 14 I referve for new 36 . 36 Numerators; Laftly, I multiply 12 the Denominator of the first Fraction by 3 the latter Quotient, (or 18 the Denominator of the latter Fraction by 2 the first Quotient,) and the Product 36 is a Denominator to each of the new Numerators 15 and 14: so 15 and 14 are found out, which have a common Denominator, and are equal to - and 7 the Fractions first proposed.

XVI. A compound fraction (otherwise called a fraction of a fraction) may be reduced into a single fraction in this manner, viz. Multiply all the Numerators continually, fo is the Product a new Numerator, also multiply all the Deno-

To reduce a compound fraction to a jugle fradion. See continual multiplication in the last Rule of the 5th Chapter.

minators continually, fo is the Product a new Denominator.

Thus if the compound fraction - of - be given to be reduced into a fingle fraction, multiply the Numerators 2 and 3, one by the other, fo as the Product 6 for a new Numerator. Also multiplying of 3 of 4 other she materials and 4 one by the other, the product is 12 for a new De- $\frac{3}{6}$ or $\frac{3}{2}$ nominator, fo is $\frac{6}{12}$ (or $\frac{1}{2}$) the lingle fraction

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fraction fought, being equivalent unto $\frac{3}{3}$ of $\frac{3}{4}$ the compound fraction given to be reduced. In like manner the compound fraction $\frac{7}{4}$ of $\frac{3}{2}$ of will be reduced into the fingle fraction $\frac{12}{12}$ or $\frac{3}{12}$ in its leaft terms) $\frac{3}{12}$

By this Rule a fraction or mixt number of a leffer name may be reduced to a fraction of a greater name: so if $3\frac{1}{2}$ pence be propounded to be reduced into an improper fraction of a pound sterling, the operation will be in this manner, viz. $3\frac{1}{2}$ or $-\frac{7}{2}$ of a penny is $-\frac{7}{2}$ of $-\frac{1}{12}$ of a pound sterling, which compound fraction will (by the aforesaid Rule) be reduced to $-\frac{7}{480}$. In like manner $42\frac{3}{16}$ minutes of an hour are equal to $-\frac{615}{42}$ of an hour, for $-\frac{615}{16}$ (that is $-\frac{42}{16}$) of $-\frac{1}{60}$ are equal to $-\frac{615}{960}$ (or in its least terms)

Here you may also observe, that when a compound fraction is one of the given terms in any question, it is first of all to be reduced to a single

fraction by the aforesaid sixteenth Rule.

To find whole numbers, which shall have the same reason as any fractions or mixt numbers given.

XVII. Two or more fractions being given, there may be whole numbers found, which shall have the same reason or proportion as the fractions given, viz. When the fractions given have unequal denomina-

tors, reduce them into equivalent fractions which shall have a common denominator, (by the 14th or 15th Rule of this Chapter) then rejecting the common denominator, the Numerators shall have the same reason or proportion as the fractions sirst given.

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So 3 and 5 being given, will first of all be reduced into their equivalent fractions 24 and then rejecting the common denominator 40, the Numerators 24 and 25 will have the fame reason with 3 and 5 viz. As 3 is to 5 so is 24 to 25: also if the fractions - 1 and - were given, there will be found 8,16, and 32, which are in the same proportion one to the other as the fractions given : In like manner, if mixt numbers be given, there may be whole numbers found which shall have the same reason or proportion, as the mixt numbers, so 52 and 35 being given, will be first reduced into the improper fractions -17 and 29 (by the tenth Rule of this Chapter:) also the said $\frac{17}{3}$ and $\frac{29}{8}$ will be reduced into $\frac{136}{24}$ and $\frac{87}{24}$ then rejecting the common Denominator 24, the Numerators 136 and 87 will have the same reason as $5\frac{2}{3}$ and $3\frac{5}{8}$ viz. As 136 is to 87, fo is $5\frac{2}{3}$ to $3\frac{5}{8}$ also 16 and 18 being given, there will be found 33 and 36, which being divided by their common measure 3 (found by the third Rule of this Chapter) will give 11 and 12 which have the same reason 25 16 - and 18.

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CHAP. XVIII.

Addition of Vulgar Fractions and mixt Numbers.

I. W Hen the numbers given to be added are fingle fractions and have equal Denomi-

To add fingle fractions, viz. 1. When they bave equal denominators

nators, add all the Numerators together, so is the sum the Numerator of a fraction, whose denominator is the same with the common denominator, which new fraction is the sum of the fractions given to be added.

So $\frac{3}{9}$ and $\frac{2}{9}$ being given to be added, their sum will be found $\frac{5}{9}$ viz. the sum of the numerators, 3 and 2, is 5, which being placed over the common denominator 9, gives $\frac{5}{9}$: In like manner the sum of these fractions $\frac{7}{8}$ $\frac{5}{8}$ and $\frac{5}{8}$ will be found $\frac{17}{8}$ which (by the 13th Rule of the seventeenth Chapter) will be found equivalent unto $2\frac{1}{8}$ so that $2\frac{1}{8}$ is the sum of the fractions given to be added.

2. When the fractions given to be added have unequal denominators they are first to be reduced into fractions of the same value, which shall

have a common Denominator (by the fourteenth or fifteenth Rule of the seventeenth Chapter) and then they may be added by the first Rule of this Chapter.

So if $\frac{2}{3}$ and $\frac{3}{5}$ were given to be added, their sum will be found $r\frac{4}{25}$; for (by the fourteenth Rule of

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Chap.XVIII. the feventeenth Chapter) 2 and 3 will be reduced into their equivalent fractions to and p which having equal Denominators may be added according to the first rule of this Chapter, and fo the fum will be found 1 4 : In like manner the fum of thefe fractions 1 3 and will be found 1-5-

III. When any of the fractions given to be added is a compound Fraction, such compound fraction is first of all to be reduced into a fingle fraction (by the fixteenth Rule of the seventeenth

The Addition of compound fra-& ions.

Chapter) and then you may proceed as before. So $\frac{3}{3}$ and $\frac{2}{3}$ of $\frac{7}{4}$ being given to be added,

their fum will be found 23 for the compound fraction 2 of will(by the fixteenth Rule of the 17th Chapter)be reduced to -3 (or in its least terms) -6 which added to the fingle fraction 3 (according to the second rule of this Chapter) gives 23 Here you may observe, that the fractions given to be added in all the former cases, are supposed to be fractions of Integers which have one and the same particular denomination, viz. if one of the fractions given to be added, be a fraction of a pound sterling : all the rest are also to be fractions of a

By denomination is meant the name of any Integer or thing.

pound sterling, and the like is to be understood of other denominations.

IV. When fractions of Integers of different denominations are given to be added, they are first of all to be reduced into fractions of Inte-

To add frattions of Integers which bive d ff. rent deno. 1N199 3 \$16.935.

gers which shall have one and the same particular denomination (by the sixteenth Rule of the seventeenth Chapter) and then they may be added by

the first or fecond Rule of this Chapter.

finde first of all the sum of the fradions (by the first and second Rule of this Chapter) then add the Integer or Integers (if there be any found) in the sum of the fractions, unto the whole numbers, and collect the sum of them as you were taught by the Rules

of the third Chapter.

So if $3\frac{1}{2}$, $4\frac{1}{3}$ and $16\frac{5}{8}$ were given to be added, their sum will be found $24\frac{11}{24}$ viz. the sum of the fractions $\frac{1}{2}$ and $\frac{5}{8}$ will be found (by the second Rule of this Chapter) to be $1\frac{11}{24}$ and the sum of the whole numbers 3, 4, and 16, is 23, unto which adding 1 (the Integer found in the sum of the fractions) the sum is 24; so that $12\frac{11}{24}$ is the sum of the mixt numbers given to be added.

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CHAP. XIX.

Subtraction of Vulgar Fractions and mixt Numbers.

7 Hen the numbers given are both single fractions and have equal denominators, subtract the leffer numerator from the greater, and place the remainder over the common denominator, to is fuch new fraction the diffe-

rence between the fractions gi-

The Subtraction of fingle frattions, VIZ. I.When they have a common denomma-

Thus the difference between the fractions _ and is =; which is found by fubtracting the leffer numerator 7 from the greater denominator 9, and placing the remainder 2 over the common denominator 11, also the difference between the fractions $\frac{\pi}{2\pi}$ and $\frac{17}{21}$ is $\frac{6}{21}$ that is, the fraction $\frac{17}{21}$ exceeds $\frac{\pi}{21}$ by $\frac{6}{21}$.

11. When the numbers given are both fingle fractions and have not a common 2. When they denominator, reduce them into frahave unequal ctions of the same value which shall denominators. have a common Denominator (by

the fourteenth or fifteenth Rule of the seventeenth Chapter) and then find their difference by the last Rule.

So the difference between the fractions and 7 will be found _ viz, reducing the fractions given

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into their equivalent fractions 48 and 49 which have a common denominator, the difference fought will be found 75 by the first Rule of this Chapter.

The fuboraction of mixt numbers, VIZ. 1. By a general Rule. given is a whole number or a mixt number, also when both of them are mixt numbers, reduce such whole, or mixt numbers into an improper

Fraction or Fractions by the tenth or eleventh Rule of the seventeenth Chapter, and then the operation will be according to the first or second Rule of the Chapter.

of this Chapter.

So $7\frac{1}{3}$ being given to be subtracted from 12, the remainder will be found $4\frac{2}{5}$, viz. First $7\frac{3}{3}$ will be reduced into the improper Fraction $\frac{38}{5}$, also 12 will be reduced to $\frac{12}{5}$ then these two improper fractions $\frac{38}{5}$ and $\frac{12}{5}$ will be reduced into their equivalent fractions $\frac{38}{5}$ and $\frac{69}{5}$ (which have a common Denominator.) Lastly, the difference between $\frac{38}{5}$ and $\frac{69}{5}$ is $\frac{22}{5}$ or $4\frac{2}{5}$ In like manner $9\frac{1}{2}$ being given to be subtracted from $12\frac{1}{5}$, the remainder will be found $2\frac{7}{10}$; as by the subsequent operation is manifest.

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Although the three last Rules be sufficient for all cases in subtraction of Fractions, mixt numbers, or whole ok I.

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whole and mixt, nevertheless the following Rules will be more expeditious in the subtraction of mixt numbers, or whole and mixt, especially when the integers confift of many places, as will be manifest by the operation, viz.

IV. When a whole number is given to be fub-

tracted from a mixt number, fubtract the faid whole number from the whole part of the mixt number (as is taught by the Rules of the fourth Chapter) and unto the remainder annex the fractional part of the mixt number given, fo is the mixt number

2. By particular Rules viz. I. A whole number, from a mixt number.

thus found, the remainder or difference fough t.

As if 7 be given to be fubtracted from 24 3, the remainder will be 17-5, as by the operation is manifeft.

V. When a fraction is given to be subtracted from an Integer, fubtract the Numerator from the Denominator, and 2. A Fraction from an Inter place that which remains over the Denominator, which new fraction

thus found, is the remainder or difference fought. So ? being fubtracted from an Integer, or 1, the remainder is 2 : Alfo 13 being subtracted from 1,

the remainder is -10.

VI. When a fraction is given to be subtracted from a whole number greater than 1, 3. A Fraction Subtract the said fraction from one from a whole of the Integers given (by the last number great Rule) fo the remaining fraction beter than 1. ing annexed to the number of Inte- . gers lessened by unity or 1, gives the remainder or difference fought,

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Thus 5 being subtracted from 17, the remainder is 162: also 7 being subtracted from 39, the remainder is 385.

VII. When a mixt number is given to be subtracted from a whole number, subtract first of all (by the fifth Rule of this Chapter) the fractional part of the mixt number, from an Integer borrowed from the whole number

given, and set down the remaining fraction, then adding the Integer borrowed, unto the Integers of the mixt number, subtract the said sum from the whole number given, (as is taught in subtraction of whole numbers) so that which remains, together with the remaining fraction before found, is the remainder or difference sought.

So if 9 1/12 be subtracted from 50, the remainder is 40-5, as by the operation is ma-

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VIII. When a fraction is given to be fubtracted from a mixt number, and the faid fraction is less than the fractional part of the

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mixt number, subtract the lesser fraction from the greater by the sirst or second Rule of this Chapter, so the remaining fraction being annexed to the whole part of the mixt number, gives the remainder or dis-

ference fought.

So $\frac{5}{9}$ being subtracted from 12- $\frac{7}{8}$ the remainder is 12 $\frac{23}{74}$, as by the operation is manifest.

12. When a fraction is given to be sub-

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tracted from a mixt number, and the faid fraction is greater than the fractional part of the mixt number, fubtract the faid greater fraction from an Integer borrowed from the mixt number, (by the fifth Rule of this Chapter) and add the remaining fraction unto the fractional part of the mixt number (by the first or second Rule of the eighteenth Chapter) fo the fraction found by that addition, being annexed to the whole part of the mixt number lessened by an Integer, or 1, gives the remainder or difference fought.

Thus being subtracted from 13 3, the remainder is 12 39, viz. fubtracting 3 from 1, the remainder is 4, which added to 3 gives 59, which being annexed to 12, (the number of Integers in the mixt number leffen-12 59 ed by 1 of unity) gives 12 30 the remain-

der fought.

X. When a mixt number is given to be fubtracted from a mixt number, and the fractional part of the mixt number to be fubrracted, is less than the fractional part of the mixt number from which you are to fubtract, fub. tract the said lesser fraction from

6. A mixt number from a mixt number by this and the wext

the greater, (by the first or second Rule of this Chapter) and fet down the remaining fraction : also subtract the Integers of the lesser mixt number from the Integers of the greater (as in Subtraction of whole numbers) fo is the mixt number thus found, the remainder or difference fought.

So if $17\frac{3}{8}$ be given to be subtracted from $20\frac{5}{7}$, the remainder will be found $17\frac{3}{8}$ $3\frac{19}{36}$, viz. Subtracting $\frac{3}{8}$ from $\frac{5}{7}$, the remainder is $\frac{19}{16}$; also subtracting 17 from mainder is $\frac{19}{16}$; also subtracting 17 from

55 20, the remainder is 3.

XI. When a mixt number is given to be fub. tracted from a mixt number, and the fractional part of the mixt number to be fubtracted, is greater than the fractional part of the mixt number from which you are to fubtract, fubtract the faid greater fraction from an Integer borrowed from the greater mixt number (by the fifth Rule of this Chapter) and add the remaining fraction unto the fractional part of the greater mixt number (by the first or second Rule of the 18th Chapter) fo is the fum to be referved as the fractional part of the remainder fought; then add the Integer borrowed, unto the Integers of the leffer mixt number, and subtract the sum from the Integers of the greater mixt number, (as in subtraction of whole numbers) fo that which remains, together with the fraction before reserved, is the remainder or difference fought.

Thus if $20\frac{7}{8}$ be given to be subtracted from $35\frac{3}{5}$ the remainder will be found $14\frac{29}{40}$, viz. $35\frac{3}{8}$ subtracting $\frac{7}{8}$ from an Integer or 1, the remainder is $\frac{1}{8}$, which added to $\frac{3}{5}$ gives $\frac{20\frac{7}{8}}{14\frac{29}{16}}$, then adding the Integer borrowed, unto

20, it will be 21, which subtracted from 35, the remainder is 14, so that the remainder or difference sought is 14.29.

When you cannot clearly discern which is the greater of two fractions, having unequal denomi-

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nators, reduce them into fractions of the same value which shall have a common Denominator, (by the sourteenth Rule of the seventeenth Chapter) and then it will be apparent which of the two fractions is the greater. As, if it be desired to know which of these two fractions $\frac{6}{7}$ and $\frac{11}{13}$ is the greater, after they are reduced to $\frac{78}{91}$ and $\frac{77}{91}$, it is

CHAP. XX.

evident that the former exceeds the latter by -1.

Multiplication of Vulgar Fractions and mixt numbers.

I. W Hen the numbers given to be multiplyed are both fingle fractions, multiply the Numerators one by the other, so is the product a new numerator: altractions, for multiply the denominators one by the other, so is the product a new denominator,

which new fraction is the product fought.

So $-\frac{7}{12}$ and $\frac{5}{8}$ being given to be multiplied, the product will be found $\frac{35}{96}$, for 7 multiplied by 5 produceth 35 for a new numerator, and 12 multiplied by 8 produceth 96 for a new denominator; also $\frac{5}{7}$ and $-\frac{3}{2}$ being multiplied one by the other, the product will be found $\frac{15}{49}$. Here you may observe that in the multiplication of proper Fractions, the product is always less than either of the terms given, for in multiplication such proportion

as unity or I hath to either of the terms given, the fame proportion hath the other term to the pro-

II. When one of the numbers given is a whole number or a mixt number; also when both of them are mixt numbers, reduce such whole number or mixt number or numbers into an improper fraction or fractions by the tenth or eleventh Rule of the seventeenth Chapter, and then the operation

will be the same as in the last Rule.

So $8\frac{2}{3}$ being given to be multiplied by 5, the product well be found $43\frac{1}{3}$; viz. $8\frac{2}{3}$ being reduced into an improper fraction will be $\frac{26}{3}$: also 5 will be $\frac{3}{4}$, then multiplying 26 by 5, the product is 130 for a new numerator: also multiplying 3 by 1, the product is 3 for a new denominator, which new Fraction $\frac{130}{3}$ being reduced (according to the thirteenth Rule of the seventeenth Chapter) will be $43\frac{2}{3}$ the product sought. In like manner $7\frac{1}{2}$ being multiplied by $5\frac{3}{5}$, the product will be found 42. Here observe, that when either of the terms given is a compound Fraction, it is first of all to be reducted into a single Fraction and then the operation is as before.

Note, Sometimes the work of Multiplication in Fractions may be very usefully contracted by the

following Rule.

1. When two Fractions propos'd to be multiplyed (whether they be proper or improper) are fuch, that the Numerator of the one, and the Denominator of the other, may be feverally divided by some common Divisor without a remainder; you may

take the Quotients instead of the faid Numerator and Denominator, and then multiply as before in the first Rule of this Chapter : As for example, if 6 be to be multiplyed by 5 because 6 the Numerator of the first, and 12 the Denominator of the latter Fraction, being severally divided by their common Divisor 6 give the Quotients 1 and 2, I fet thefe (or imagine them to be fet)in the places of 6 and 12; by which exchange there arise - and these multiplyed one by the other, (according to the first Rule of this Chapter) produce _ the destred Product of 6/7 into 5/12, in the smallest terms.

Again, to multiply 16/48 by 18/16; because the Nume-

rator of the first Fraction and the Denominator of the latter, being each divided by 16 give the Quotients 1 and 1, I fet 1 and 1 in the places of 16 and 16; likewise because 48 the Denominator of the first, and 3 the Numerator of the latter Fraction, being each divided by their common Divisor 3 give 16 and 1, I take 16 and 1 instead of 48 and 3; fo by those exchanges there arise $\frac{x}{16}$ and $\frac{x}{x}$, which multiplyed one by the other produce i, which is the Product in the smallest terms made by the multiplication of $\frac{16}{48}$ into (or by) $\frac{3}{16}$.

2. To take any part or parts of a number propounded, is nothing else but to multiply the faid number by the Fraction which declareth what part is to be taken: fo if you defire to know what is -5 of 320, multiply $\frac{320}{1}$ by $\frac{5}{8}$, or $\frac{40}{1}$ by $\frac{5}{1}$, and the product will be 200. In like manner - of 45 3 is

303. Alfo - of 120 is 30.

3. Sometimes the work of multiplication in mixt numbers

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numbers may be compendiously performed after the manner of these following examples. viz. if it be required to multiply 120 - by 48 - first multiply the whole numbers mutually, to wit, 120 by 48, and place the particular products orderly one un-

der the other as in Multiplication of whole numbers; then multiply the faid whole numbers first given by the Fractions alternately, viz. take in of 48 which is 12, also take in of 120 which is 60, and place the faid 12 and 60 orderly to be added to the former particular products: Lastly, add all together, and to the sum annex the product of the two fracti-

ons, to wit in this example, the product of the multiplication of $\frac{1}{4}$ by $\frac{1}{2}$, which is $\frac{1}{8}$, fo the total product required will be $5832\frac{\pi}{8}$, as you see by the example in the Margent. In like manner, if $18\frac{1}{2}$ be multiplied by $40\frac{1}{3}$, the product will be $746\frac{1}{6}$; and if $29\frac{\pi}{2}$ be multiplied by 50, the product will be 1475, as you see by the examples following.

4. When a fraction is to be multiplyed by its Denominator, take the Numerator for the product; fo if this fraction -3- be propounded to be multiplied by the Denominator 4, the product will be

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be 3, which is the same with the Numerator 3. In like manner if $\frac{3}{8}$ be multiplied by the denominator 8, the product is equal to 5 the Numerator of the said $\frac{3}{8}$.

CHAP. XXI.

Concerning Division by Vulgar Fractions and mixt numbers.

I. When the numbers given are both lingle fractions, multiply the Denominator of the Divisor by the numerator of the Dividend, so is the product a new numerator of the Dividend, fo is the denominator of the Dividend, so is the product a new denominator, which new fraction is the quotient sought.

So if $\frac{4}{9}$ be given to be divided by $\frac{3}{3}$, the quotient will be found $\frac{20}{27}$; viz. multiplying 5 by 4 the product is 20 for a new numerator, also multiplying 3 by 9, the product is $\frac{3}{3}$) $\frac{4}{9}$ ($\frac{20}{27}$) for a new denominator, so is $\frac{20}{27}$ the quotient sought; in like manner if $\frac{5}{8}$ be given to be divided by $\frac{2}{7}$, the quotient will be found to be $\frac{35}{16}$ that is $2\frac{3}{16}$, as you see in the Example: here you may observe, that in $\frac{2}{7}$) $\frac{5}{8}$ ($\frac{35}{16}$) Division by proper fractions, the quotient is alwayes greater than either of the fractions given; for in Division, as the divisor is to 1 or unity, so is the dividend to the quotient.

11. When one of the numbers given is a whole number or a mixt number; also when both are mixt numbers, reduce such whole number or mixt number or numbers into an improper fraction or fractions, by the tenth or eleventh Rule of the seventeenth Chapter, and then the operation will be the same as in the last Rule.

So if 42 be divided by 7-, the quo.

 $(7\frac{v}{2})$ 42 (tient will be found to be $(5\frac{3}{5})$, for $(7\frac{v}{2})$ and 42 will be reduced into these improper fractions $(5\frac{15}{2})$ and $(6\frac{3}{5})$ tiplying 42 by 2, the product is 84 for

a new Numerator, also multiplying 15 by 1, the product is 15 for a new denomina-

tor, fo is 184 the quotient fought, which is equal to 53/5 (as is evident by the thirteenth Rule of the feventeenth Chapter.) In like manner, if 6 1/2 be divided by 3 2/5, the quotient will be 1/34. Also if 5 1/3 be divided by 12 1/2, the quotient will be 32/75.

Note, Sometimes the work of Division in Fractions may be very usefully contracted by this following Rule, viz. When either the two Numerators, or the two Denominators of the Fractions proposed, can be divided severally by some common Divisor without a remainder, you may take the Quotients instead of the said Numerators or Denominators, and then divide by the first Rule of this Chapter: As for example, if \(\frac{12}{17}\) be to be divided by \(\frac{8}{3}\), because the Numerators 12 and 8 being each divided by their common Divisor 4 will give the Quotients 3 and 2, I take these instead of 12 and 8, by which exchange there arise \(\frac{3}{17}\) and \(\frac{2}{3}\), the for-

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mer of which being divided by the latter, (according to the first Rule of this Chapter) gives 15, which is the Quotient in the least terms that ariseth by dividing 13 by 8,

Again, to divide $\frac{25}{8}$ by $\frac{15}{8}$; because the Numerators 25 and 15 being severally divided by their common Divisor 5 give the Quotients 5 and 3, likewise because the Denominators 8 and 8 being each divided by 8 give the Quotients 1 and 1, I set 5 and 3 in the places of the Numerators 25 and 15, also 1 and 1 in the places of the Denominators 8 and 8, whence arise $\frac{5}{2}$ and $\frac{3}{2}$; Lastly, by dividing $\frac{5}{2}$ by $\frac{3}{2}$, that is 5 by 3, there ariseth $\frac{5}{3}$, that is $1\frac{2}{3}$, which is the desired Quotient of $\frac{25}{8}$ divided by $\frac{15}{8}$.

Questions to exercise the Rules of Vulgar Fractions before delivered.

Quest. 1. The difference of two numbers is $1^{\frac{12}{24}}$, the leffer number is $2^{\frac{1}{8}}$, what is the greater? Answ. $3^{\frac{1}{4}}$, (found by Addition.)

gives the sum 8 23 Answ.4 1 (found by Subtraction.)

2 neft. 3. There is in three bags the sum of 121-21, viz. in the first bag 50-11, in the second

40 41, what is in the third hag? Anfw. 30 1.

(found by Addition and Subtraction.)

Quest.

Notation of Book I.

Queft. 5. What is 3 of 1303 ? Anfw. 813

(found by Multiplication.)

160

Quest. 6. What number is that which being multiplied by 3 produceth 25 2 Ans. 42 1 (found by Division.)

Now followeth the doctrine of Decimal Fractions.

The Doctrine of Decimal Fractions.

CHAP. XXII.

Notation of Decimal Fractions.

2. TT is hard to determine, who was the first that brought Decimal Arithmetick to light, though it be a late Invention, but without doubt it hath received much improvement within the compass of a few years, by the industry of Artists, and now feems to be arrived at perfection. The excellency thereof is best known to fuch as can The proper ufe apply it to the practical part of the of Decimal 4-Mathematicks, and to the Construrithmetick. ction of Tables, which depend upon standing or constant proportions, such are Trigonometrical Canons, Tables for computing of Compound Interest, &c. in which cases decimal operations do afford fo great help, that (in my opinion) many ages have not produced a more usefull invention; but it may be objected, that Decimal Arithmetick for the most part gives an imperfect folution to

Chap.XXII.

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a question, this I grant, yet the Answer so given may be as ufefull as that which is exactly true; for in common affairs, the loss of _ part of a grain, or of an inch, &c. to wit, any quantity which cannot be feen is inconsiderable : but I would not be mistaken, for in extolling Decimals I do not cry down Vulgar Fractions, fince experi-Decimal Fra-

ence sheweth that Decimal Fractions are commonly abused, by being applyed to all manner of questions a-

ctions fometimes abufed.

bout money, weight, &c. when indeed many questions may be resolved with much more facility by Vulgar Arithmetick, as may partly appear by this Example, viz. at 9 1.-61.-8 d. the hundred weight of Tobacco, what will 987 hundred weight cost? Answ. 9212 l. which by the common Rule of Practice by Aliquot parts is found out, in a quarter of the time that will necessarily be required to work it by Decimals, which at last will give an imperfect answer ; I might instance the like inconvenience divers ways, were it not for loss of time : fo that the right use of Decimals depends upon the discretion of the Artift.

II. When a fingle Fraction hath for its denominagor a number confifting of 1 or The definition unity in the extream place towards of a Decimal the left hand, and nothing but a Cy-

pher or Cyphers towards the right, it is more particularly called a Decimal: of this kind are thefe that follow, 5, that is five tenths, 5, five hundredth parts; likewise these are decimal fractions, 34, 205, 1023, &c.

III. A Decimal fraction may be exprest without

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out the denominator, by prefixing a point or comma before (to wit, on the left hand of) the Numerator, so to may be written thus, s or thus, s and

25 thus, .25 or thus ,25.

205, thus, .0205, likewife 6, thus, .006.

V. In Decimals thus expreit, the Denominator is discoverable by the places of the Numerator: for if the Numerator consists of one place, the Denominator consists of 1 or unity with one Cypher, if of two places, the Denominator consists of 1 with two Cyphers annexed: if of three, the Denominator consists of 1 or unity with three Cyphers annexed: fo the Denominator of 25 is 100, the Denominator of .050 is 1000, and the Denominator of .096 is 1000.

VI. Cyphers at the end of a Decimal do neither augment or diminish the value thereof: so.2,.20,.200,.2000 are decimals, which have one and the same value, for 20 being abreviated by the eighth Rule of the seventeenth Chapter, will be made 2 and

10 will 1000 or 10000.

VII. Wherefore Decimal fractions are easily reduced to a common Denominator, (which is a trouble some work in Vulgar Fractions) for if all the Numerators of as many decimal fractions as are given, be made to consist of the same number of places, by annexing a Cypher or Cyphers at the end

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end (that is on the right hand) of such Numerators as are desective, they will all be reduced to a common Denominator, so these Decimals .2, .03, .027 (which signific \(\frac{2}{10}\), \(\frac{37}{1000}\)) may be reduced into these, .200, .030, .027, which have 1000 for a common Denominator.

VIII. The order of places in any Decimal proceedeth from the left hand to the right, contrary to the order of places in the Integers, which is from the right hand to the left: so in this Decimal 247, the figure 2 standeth in the first place, (being the outermost towards the left hand, and next to the point,) the figure 4 standeth in the second place, and 7 in the third. Also in this Decimal .0245,

a Cypher stands in the first place, 2 in the second, 4 in the third, and 5 in the fourth.

IX. Every place in the Numerator of a Decimal Fraction hath a peculiar Denominator or proper value, viz. the Denominator of the first place is 10; of the second, 100; of the third, 1000, &c. so that the first place of a Decimal signifies tenth parts of an unit or Integer; the second place, hundredth parts of an Integer; the third place, thousandth parts of an Integer; the third place, thousandth parts of an Integer, &c. Hence it is manifest, that this Decimal .3254 (every place thereof being considered apart by it self) consists of .3, .02, .005, .0004, (viz. 3, 2, 100, 1000), which being reduced to a common denominator (by the seventh Rule of this Chapter) will give these, .3000, .0200, .0050, .0004, (to wit, 3000, 1000), 10000, 1000

X. In whole numbers, the first place above (that is on the left hand of) the place of unities signi-

fies

fies Tens of unities; but the first place beneath, (that is on the right hand of) the place of unities fignifies tenth parts of 1 or unity, and is called the first place of Decimal parts or place of Primes; likewife the second place above the place of Unities, signifies hundreds of Unities, but the second place beneath the place of Unities signifieth hundredth parts of 1 or unity, and is called the second place of Decimals, or place of seconds, so that as the values of the places in Integers do ascend in a decuple proportion from the place of Units towards the left band, so the values of the places of Decimals do descend in a subdecuple proportion beneath the place of units towards the right hand; all which will be evident by the following Table.

A Table for the Notation of Integers and Decimals.

oof Unites.	ı or y.
بنّ	of r unity.
Fifth place of Tenthon ands Fourth place of Tenthon ands Third place of Hundreds Scond place of Tens Fift place of Tens	First place of Tenth parts Second place of Hundredth parts Third place of Thongandth parts Fourth place of Tenthous and the parts R.C.
7 3 2 8 5	. 8.237
Sec. Fifth place 2 Ten thon and Fourth place 2 Thou and and second place 2 Hundreds Second place 2 Tens First place 2 Onices (11)	First place Second place Third place Fourth place

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In the foregoing Table, you may observe that the places of Integers or whole numbers are feparated from the places of Decimal parts of 1 (or unitie) by a point; fo the number on the left hand of the point expresent 73285 Integers or unities, but the number on the right hand or the point expreffeth only 8237 parts of 1 (or an Integer) Suppofed to be divided into 10000 equal parts. In like manner this number 3 . 8 fignifies 5 Integers and eight tenth parts of an Integer, and this number 185. 82 fignifies 285 Integers (or Unities) and 82 parts of an Integer.

CHAP. XXIII.

Concerning the Reduction of Vulgar Fractions to Decimal Fractions.

. IF the greatest integer of money, as also of weight; Imeasure, & c. were subdivided decimally, to wit, pound of English money into ten equal pieces of oyn, and every one of these into ten other equal pieces, &c. and weights, measures, &c. after the same manner; the doctrine of Arithmetick would be taught with much more ease and expedition than now it is; but it being improbable that fuch a refornation will ever be brought to pass, I shall proceed n directing a course to the studious for obtaining he frugal use of fuch Decimal fractions as are in his power.

II. Forasmuch as in Arithmetical questions, some of the given numbers do for the most part happen to be fractions, a way must be shewn how to reduce a Vulgar Fraction to a Decimal Fraction ; yet in

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fome cases there is no need of this Reduction ; for example, a foot in length is vulgarly subdivided into 12 inches, an inch into 4 quarters, and each quarter into 2 half quarters; but a foot may as eafily, and a great deal more commodioully be divided, first into ten equal parts, and then each of those into ten other equal parts, and each of these into ten other equal parts ; (or at leaft fuch divifion must be supposed or imagined when it cannot actually be made) this foot in length fo divided, being applyed to the fides of superficial figures, or of folid bodies , will at first fight give the quantities of lines in feet and decimal parts of a foot; (as readily as a foot vulgarly divided will fhew you how many feet inches, quarters, and half quarters are contained in any line) from whence the Superficial or felia content may be found in feet by multiplication only ; and how much this excels the valear way. I shall partly manifest in the fifth Rule of the 26th Chap. ter. The like subdivision I would have to be made of a Tard. Perch. &c.

III. A single fraction which is no decimal fraction may be reduced into a de
How to reduce cimal of the same value, or infinitely near, (for all vulgar fractions cannot be exactly reduced to decimals) by

the Rule of Three direct; for as the Denominator of any single fraction whasoever, is to the Numerator thereof, so is any other Denominator to his correspondent Numerator: Example, let it be required to reduce sinto a Decimal, whose Denominator is affigned to be 1000, say by the Rule of three, if the Denominator 8 hath 5 for a Numerator, what will the Denominator 1000 require for a Nu-

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a Numerator ? Multiply and divide as the Rule of Three direct doth require, fo will the fourth properrienal be found to be 625, which is the Numerator foughe; therefore to or .625, is a decimal fraction equal in value to . Another Example, let it be required to reduce 27 into a decimal fraction, whole Denominator shall be 100000, say by the Rule of three, if 240 the Denominator give 7 for a Numerator, what will the Denominator 100000 require for a Numerator & Anto. 2916 and Somewhat more, but that which the faid 2916 wants of being a true Numerator is less than _____ part of an Integer, therefore the decimal fraction 1000 or .01916 is almost equal to which 240 cannot be exactly reduced into 2 Decimal Fraction, the like will happen in the reduction of most vulyar Fractions to decimals in which case, the Denominator of the decimal must be affigned to be fo great, that what is wanting in the Numerator may be an inconfiderable value.

IV. Upon the aforefaid ground, the known or accustomary parts of Money, Weight, Measure, Time. &c. may be reduced to decimals: for if you defire to know what desimal fraction of a pound ferling is equal in value to one Milling, confider first that a pound is the Integer, and that 20 Millings are equal to that Integer, therefore I shilling is of a pound; now if we conceive one pound to be divided into 100000 parts, ziz. if we affign 100000 for the Denominator of a decimal fraction, the Numerator will be found by the last Rule to be 5000, fo that 1000 or logooo or. og (for cyphers at the end of a decimal are of no-ule, as hath been shewn in the 6th Rule of the 22 Chapter) is a decimal fraction of a pound, and is exactiv

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actly equal to 1's. or 1 part of a pound ferling.

In like manner forafmuch as 240 pence are equal to a pound of English money, 7 pence are 2 parts of a pound, which fraction will be reduced into this decimal. 029161. Which is very near equal to 171. for it wants not 100000 part of a pound. Moreover fince 960 farthings are equal to a pound English, one farthing is 1 part of a pound, which will be reduced into the decimal. 00104 l. very near ; but if you please to proceed nearer the truth; you will find this decimal .00104166 to answer a farthing, and so by augmenting the Denominator with cyphers, you may proceed infinitely near, when you cannot attain unto the truth it felf. After the fame method may the vulgar Sexagenary fractions used in Aftronomy be reduced to decimals, for fince a degree is ufually subdivided into fixty parts called minutes or primes; a prime or minute into fixty parts called feconds; a second into fixty thirds; a third into fixty fourths, &c. and consequently a degree is equal unto 60 minutes (or Primes) or unto 3600 seconds, or 216000 thirds or 12960000 fourths, &c. It is evident that 7 minutes (or Primes) are -7 parts of a degree, which by the third Rule of this Chapter may be reduced into the Decimal .1166, &c. Alfo 29 thirds are 20 parts of a degree which may be reduced into the decimal .000134, &c. Moreover,

58:33:14:12, that is, 58 Primes, 33 feconds, 14 thirds, and 12 fourths may be reduced to a decimal in this manner, viz. reduce them all into fourths (according to the fixth Rule of the feventh Chapter) fo will you find 12647652 fourths, which

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to th ch are 11500000 parts of a degree, which vulgar fraction may be reduced into this decimal of a degree, to wit, .975899, &c. (by the third Rule of this Chapter.)

This to the ingenious will be a sufficient light for the finding of the Decimals congruent to the shillings, pence, and farthings which are under a pound sterling; also the decimals of the known parts of Weight, Measure, Time, &c. as they are express in the sollowing Table, wherein you may observe; that most of the decimals consist of 7 or 8 figures, yet in ordinary practice, you shall have occasion to use only the first five, and sometimes sewer.

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THE TABLE OF REDUCTION.

DF Engli	ET I.	pence with	Decimals of a pound
	er being	salidade yas salidade yas	.0489583
Shillings	Decimals of a pound.	11	.046875
19	95		.0447916
17 16	.85	10	.0427082 .041 6 666 .040625
14	.75		.0395833
13 12.	.65 .6	9	.0304583
10	·5 ·45	8	.0354166
8 7 6	.4 35 .3		'0322916 '03125
HT 5	.25	7	.0302083 .0291666 .028125
3 2 1	.15		.0270833
			5 .025

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Om Postilla	Contract Space on the Part of the Contract of	and the same of th	Management Suggest 1980 E-607-100-100
1 0002142	10239583	14 /	.7
\$281680. H	:0229166	30013	.65
14550807	.021875	12	.6
5823-160 R	.0208333	11	.55
4 Srgo. 1	.0197916	10	.5
\$1725500 C	.01875	9	.45
84,000	.0177708	8	.4.
	.0166666	7	-35
7584900	.015625	6	.3
THE ESTA	10145833	5	.25
\$820800.	.0135416	Parl amound	.2
de il maisola 3.	.0125	3	112
A Bushes.	.0114583	. 2	·I
2078600.	.0104166	1	.05
54:8700.	.009375	328	Decimals
\$ 0072542	.0083333	Grains	of an ounce.
1.0000000	.0072916	23	10479166
1,0061383	.00625	22	-0458333
I pen, & I far.	0052083	21	-04375
Penny 1	0041666	20	.0416666
3, Farth.	*003125	19	.0395833
1. Farth.	.0020833	18	.0375
Carrie - 1	.0010416	17	.0354166
TABL	ET II.	16	,0333333
Of Troy weigh	tht, the In-	15	.03125
teger being an	Ounce.	14	.0291666
Danne	Desired 6	.13	.0270833
weights.	Decimals of	. 12	.025
-	an Ounce.	11	.0229166
19		10	.0208333
18		9	01875
17		8	
16		7	.0145833
15	175	- 6	0125

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- day	1.0114166	Legor 11	10982142	7
4		10.	.0892857	
3		* T. I.SG. 9	.0803571	
2	.0041666	8	.0714285	
I	.0020833	8:00010.7	.0625	
TABL	many the same named	6	.0535714	
of Averd		200000.5	.0446428	
	Integer being	2.3	.0357142	
an hundred	weight to	3	.0267857	
mit, 112 pos		2	.0178571	
	decimals of	01427 O I	.0089285	
1 hundred.	I hundred.	5 3110	decimals of	
1 managem		Ounces.	1 hundred.	
1	.75	00140195	.0083705	
encommonds and	35	77 14	.0078125	
1	.25	. 22 200 13	.0072544	
2 mais his Con	decimals of	0:05 12	.0066964	
Pounds.	I hundred.	11	.0061383	
27	.2410714	Tosporo io	.0055803	
26	-2321428	- 001400	.0050223	
25	.2232142	8001114	.0044642	2
24	2142857	1	.0039062	
23	.2053571	0110106	.0033482	
22	.1964285	5	.0027901	
21	.1875	1	.0022321	
20	.1785714		.0016741	
19	.1696428	2	.0011160	
18	.1607142	20 Plexity	.0005580	
17	.1517857	The state of the state of	-	
16	1428571	quarters of	decimals of	
15	.1339285	1 Ounce.	1 hundred.	
14	.125	3	.0004185	
13	1160714	2	.0002790	
12	1071428	1.	.0001395	L

TABLET

ok I.

TABL	ET IV.	6	.0234375
Of Auera	upois little	5	.01953125
	Integer being	4	.015625
a pound.		198 min. 3	.01171875
to cantaryen	decimals of	S. Links	.0073125
Qunces.	а ронна.	1.6.1	.00390625
15	9375	quarters of	decimals of
14	.875	a dram.	I pound.
.13	8125	3	,0029296
43	75	7.62	.0019531
to theme to	.6875	(1	.0009765
10	.625	TABL	ET V.
9.	.5625	Of liquid m	eafures, the
8	25	Integer ber	ng a gallon.
7.007	4375	\$4.60	decimals of
6	375	Pints.	1 gallon.
this is no tary 5	.3125	. 7	-875
1 2000 A	.25	Malana 6	-75
3	.1875	-1-5	.625
0.507102	.125	1 028 226.4	.5
1	.0625	2 202 10 3	-375
Laure of morth	decimals of	- 28500 2	.25
Drams.	a pound.	I de la companya i	.125
15	.05859375	quarters of	decimals of
. 14	.0546875	a pint.	agallon.
13	.05078115	300 F00 3	1.09375
12	.046875	250 100 2	.0625
Axana II	.04296875	1	.03125
10	.0390625		
9	.03515625		
	.03125		1. 12 11
71	.02734375		

TABLET

ABLI	TVI	TABLI	TVIL
	es, the In-	Of long mea	
er being a	quarter.	Tard or one	Ell being the
	decimals of	Integer.	201
Bufbels,	a quarter.	quarters of	decimals of
	:875	1 yard or 1	1 yard or 1
7	.75	ell.	ell.
AU 160 Z 5	.625	2275	.75
excep 4	.5	2	.5
intim 3	.375	1	.25
2	28	Agen	decimals of
I.	1,125	Nails.	1 ya.or 1 ell
-	decimals of	1.73	1875
ks.	a quarter.	: 72	
3		17543	1
2		quarters of	decimals of
1		1 nail.	1 ya.or 1 ell
erters of	decimals of	-3	1.046875
Peck.	a quarter.	2	.03125
7 3	.0234375	7 1	.015625
2	.015625	TABL	ET VIII.
I	1.0078125	Of the Rea	luction of in-
7.	decimals of	ches,&c.to	decimals, the
Pints.	a guarter.	Integer bei	ng a foot in
3	.005859	length.	44
. 2	.003906	37250	decimals of
1	.001953	Inches.	a foot.
757	. 4	11	1 -2 -0000
		10	.8333333
		9	1.75

k 1.	Chap.XXIII	of1	Reduction.	2175
one		.6666666	parts of a	decimals of
the	4.02560. b	5833333	dozen	a grofs.
106	56665720. 8		14301000	.076388
44	5505 FEU 25	4166666	017	.069944
of	1110 30 4	23 333333	6 3063333	.0625
1	9916220. 38		8.1669999	.055555
-	21111110. 23	\$ 166666B	4.125	
	11 .02 3277	10833333	4.0833333	.04166 6
15	guarters of	decimals of	4. October	.034722
	an inch.	a foot.	Adecimais of	.027777
of	*+++6:0:	-0625	taday.	020833
11	77880.17	.0416666	5270010 E	.013888
	5550010.	.0208333	T : 0102777	1.006944
	half a quan	.0104166	TABL	ET X.
	ter of an inch.	2	OFTIMES 40	day being the
of	TABLI	TIX.	Melget .	2
ell	Of dozens, the	integer be-	£750.	decimals of
	ing a gross.	-	Honris to.	day.
	MOISTO	decimals of	F11102023	(9583333
	dozens.	a grofs.	001471022	9166666
	Mostingii.	9166666	14 C347222	4875
· ·	11111110	8333333	775015030	.8333333
be	6 0101165	.75	OL OFFICE	
in	8 . 100 222	6666666	81,03000	
*"	7	,5833333	441016017	1
-	sassen 6	.5	91 OSTET 10 1P	
of	28 100000 \$.4166666	St. Of old 12	.625
_	4.0000:44		1100000 14	
6	71000.30	.25	0001000 13	
3	24 74 200 29	1666666	12	.5
	1102.00.30	0833333	Tr	.4583333
	de 3 1 0 1 2		10	4166666
81	200 000 4			. 0

Minutes. a day. .0409722 59 58 .0402777 .0395833 57 .0388888 56 .0381944 55 .0375 54 .0368055 53 52 .0361111

.0354166

.0305555

51

44

18 50 .0347222 17 49-1-0340277 16 48 .0333333 15 .0326388 47 14 46 .0319444 13 .0312500 45 12

.0076388 II .0298611 43 .0069444 10 .0291666 42 .00625 .0284722 41 8 .0034722 .0277777 40 .0270833 39

.0048611 .0041666 .0034722

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Book

.0263888

.0256944

.0249999

.0243055

.0236111

.0229166

.0223222

.0215277

.0208333

.0201388

.0194444

.0180555

.0173611

.0166666

.0159722

.0152777

.0145833

.0138888

.0131944

.0118055

IIIIIIO.

.0104166

.0097222

.0090277

.0083333

.0125

.01875

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3

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2

6

4	.0027777
3	.0027777
2	.0013888
1	.0006944

Fablets, of which the first (intituled English money) contains in the first of Zaglish motor the particular Fractions (viz. the shillings, pence, and

withings) of a pound sterling; and in the other coumn the decimals, unto which they may be respetively reduced: So in the same Tablet .65 is the secimal, answerable to 13 s. .0208333 to 5 d. and 003125 to 3 f. Likewise. 0489583 is the decimal of 11 d. together with 3 farthings; Also. 03125 s the decimal of 7 pence half penny.

VI. The next Tablet (intituled Troy weight)con-

ains in the first column thereof the

particular Fractions, (viz. the Penny 2. of trey weights, and Grains) of an ounce Trey, weight.

and in the other their respective deci-

mals: fo .6 is the correspondent decimal of 12 penny weight, and .0020833 of 1 grain. Likewise 025 is the decimal of 12 grains.

VII. The third Tablet (intituled Averdupous rest weight) contains in the first coumn thereof the Fractions, (viz. the suppose great Quarters, Pounds, Ounces, and the weight.

Quarters of Ounces) of an Hundred according to Averdupois weight, and in the other their proper decimals: so.5 is the decimal of two quarters or half a hundred, .1517857 of 17 pounds: .0033482

Reduction of Vulgar Fractions Book 1 178 :0033482 of 6 Quices, and. 0004185 the decimal of 3 quarters of an Ounce. VIII. The fourth (intituled Averdupois little weight) theweth you the Fractions (viz. 4. Of Averthe Ounces, drains, and quarters of drams dupois little of a pound Averdupois, together with

ggeight. their respective decimals : so the dais mal of 3 Ounces is . 1875, the decimal of 9 Drams if .03515625, and the decimal of one quarter of t Dram is .0009765.

IX. The fifth (intituled Liquid measures) had the fractions (viz.the Pints and quarten of pints) of a Gallon, and likewift 4.0f Liquid mea fures. their several decimals : fo the decimal of & Pints is .625, and the decimal of

two quarters or half a pint is .0625.

X. The fixth (intituled Dry measures) gives you the fractions (viz. the Bufbels, Pecks, quarters of Pecks and pints) of a quar-6. Of Dry ter, together with their peculiar demeg sures. cimals: 10 .375 is the decimal of three Bushels, .03125 of one Peck, 0234375 of 3 of 1 peck, and .003906 of two pints.

X 1. The seventh (intituled Tards and Ells) offers you the fractions (viz. the Quar. ters, Nails, and quarters of Nails) of 7. Of Long meafures. Yards or Ells, and their respective decimals: fo .25 is the decimal of one quarter of a Yard or Ell, .125 of two Nails, and

.046875 of three quarters of a Nail.

X II. The eighth (intituled Reduction of inches, &c. to decimals of a foot) presents unto you the fractions (to wit, the Inches, quarters of Inches and half quarters of an Inch) of a foot, together with

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with their correspondent decimals : fo .4166666 is the decimal of & Inches, .0625 of 3 of an Inch. and o104166 of - or half a quarter of an Inch.

X 1 1 1. The ninth Tablet (intituled Dozens) yields you the Fractions (viz. the 8. Of things Dozens and particulars) of a Gros, accompand by as also their respective decimals : so the Dozen. 25 is the decimal of 3 Dozen, and .048611 of 7 particulars.

XIV. The tenth and last Tablet (intituled Time)

gives you the Fractions (viz. the Hours

and Minutes) of a Day: fo .625 is the decimal of 15 hours, .0375 of 54 mi-

outes, and .0006044 of one minute.

XV. When a fingle Fraction of any of the premised Tablets is propounded to be reduced to a decimal, find it in the first Column of the Tablet, unto which it belongs; this done, just against that Fraction so found, you shall have the decimal required : so 13 s. being propounded, taking the

The ufe of the Same Table for the Reduction. Of fingle fractions to decimals.

first premised Tablet, I find 13 s. in the first Column of the Tablet of money, and just against the same thirteen hillings, I observe . 65, before which having prefixed a point, and by that means ligned it for a decimal (according to the third Rule of the 22 Chapter of this Book) I conclude the same .65 fo ordered, to be the correspondent decimal of thirteen shillings the fraction propounded : In like manner .0229166 is the decimal of 11 Grains in the Tablet of Troy weight; and .0357142 the decimal of 416. in the Tablet of Averdupois great weight, &c.

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pounded, and it is required to find a decimal equivalent unto the sum of them, find the decimal of each of the Fractions given according to the last Rule; then adding together the decimals so found that intire sum is the decimal sought: so 13 s. 3d being reduced to a decimal sought: so 13 s. 3d being reduced to a decimal, is .670833; for the decimal of 13 s. is .65, and the decimal of 3d .020833, which being added together (by the second Rule of the 24th Chapter of this Book) amount to .670833, viz. the decimal which represents 13 s. 3d. the Fraction propounded: In like manner the decimal of 9 penny weight, and 13 Grains is .4770833, and the decimal of \(\frac{1}{2} \) C. 19 lb. 7 Ounces is .67354, &c.

13 s. 5 d.	.020833
	.670833
9 p. w. 13 gr.	·45 .027083
	.477083
10 lb. 7 ounc.	.5 .16964 .00390
. Sometimes	.67354

And here as you see meer Fractions reduced, so likewise may the Fractions of mixt numbers be reduced to decimals: for example, these numbers 97 ok I

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97 lb. 181

16. 7 ounces 13 4 drams. Item of 67 Gallons, 54 pints. Item 28 Quarters,0, Bushels,2 4 Pecks, and 3 Pints after reduction are 97, .4891, .67, .71875, and 28.0781

97:4375 67.625 28.0625 .0507 .0937 .0156 .0009 67.7187 28.0781

Again 22 1 yards, 3 Nails; Item 36 Gross, 3 Dozen and 5 particulars, being reduced, are 22 7031, 36.2847.

> 22.5 .0156 .0156 .0347 22.7031 36.2847

what Fraction it represents, search he same decimal in the second Coumn of the Tablet, unto which it beongs, where if you find it expressly,

the number just against it in the first Column is the fraction you look for: so.65 (representing the fraction of a pound sterling) being given. I find it in the second Column of the Tablet of Mozney, and over against it in the first Column I find 3 s. which is the fraction represented by .65, the decimal propounded. In like manner 3.025 (respecienting 3 ounces and .025 of an ounce Troy) being propounded, the number represented by it, is 3 Ounces, 0 p.m. 12 grains.

XVIII. When in the second Column of the

Tablet, unto which you are directed, you cannot precifely find the decimal propounded, fearch that, which being lefs, comes nearest unto it, and take the number that answers unto it in the first Column for the greatest fraction of the number required: then deducting the decimal so found out of the decimal given, find likewise the remainder, as another decimal, and take his correspondent number for the next fraction of the number required: and so proceed in that order, till you have discovered the intire number represented by the

decimal propounded.

Example: .6739 being propounded, I demand the fraction of a pound fterling represented by it; the decimal in the Tablet of money, which being less comes nearest to .6739 is .65, whose correfoondent number in that Tablet is 13, which are the shillings of the number required; then subtracting (by the I Rule of the 25 Chapter of this Book) .65 out of .6739, the remainder is .0239. and the nearest decimal in the same Tablet to .0230 is .0208, whose correspondent number is s. which are the pence of the number required : last of all deducting .0208 out of .0239, the remainder is .0031, which gives you in the first Column 3, being the farthings of the number required : So that I conclude the intire fraction represented by the decimal. .6739, is 13 s. 5 d. 3 f.

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Subtract 13 s.	65
Subtract 5 d.	.0239
3 f	0031

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In like manner 7.359 C. being reduced by the Tablet of Averdupois great weight is 74 C. 12 lb. 4 ounc. And 94.58 lb. reduced by the Tablet of Averdupois little weight; is 94 lb. 9 ounces and 6 drams.

	7.359 C.
Subtract I quarter	25
	.109
Subtract 12 lb.	107
4 02.	002
	94.58 16.
Subtract 9 oz.	56
6 Drams.	oz

CHAP. XXIV.

Addition of Decimal Fractions.

I. To fuch as well understand the Notation of Decimal fractions, all the varieties of their Numeration, to wit, Addition, Subtraction, &c., will be as easier as the operations by whole numbers; therefore he that would be a good Proficient in Decimal Arithmetick, must throughly understand the 22 and 23 Chapters aforegoing.

II. When divers decimal fractions are given to be added together, they must first of all be orderly placed one under another according to the doctrine of their Notation. So if these decimal fractions, to wit, 125, 39 and 7 were given to be added, they must be written down thus

.125 .39 .7 N

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or if you will have the fame number of places to be in all the decimals given, without altering their values, they may be written thus.

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12 1125 .390 .700 Not thus. .125 . 39 7

For the Figures or Cyphers, which are of like degrees or places must be subscribed directly one under another, viz. tenth parts or primes must be written down directly underneath tenths; also bundredth parts or feconds must be placed under hundredth parts, as you fee in the first Example, where.3 or three tenth parts in the fecond decimal stands directly under . I or one tenth part in the first decimal; likewise. 7 or seven tenths in the third decimal stands directly under the tenths in the former, and fo of the reft.

In like manner, when mixt numbers, which confift of Integers and decimal parts are given to be added, due respect must be had of their subscription one under another : fo if these mixt numbers, to wit, 32.056, 7.07, and 1 .9 were given to be ad-

ded, they must be written down thus.

32.056 7.07 I .Q

III. Having placed the decimals and drawn a line underneath in manner aforesaid, add them together,

gether, beginning with the outermost rank towards the right hand (as hath been taught in Addition of whole numbers of one denomination in the third Chapter :) fo if the decimals in the first Example of the second Rule of this Chapter were given to be added, I first subscribe 5, which is all that stands in the first rank towards the right hand, then proceeding to the fecond rank, I fay o and 2 make 11, wherefore I write down I .39 which is the excess of 11 above 10, and for the 10 I carry 1 in mind to the 1,215 next rank, faying I in mind added to 7 makes 8, which added to 3 and 1 make 12, wherefore I write 2 which is the excess of 12 above 10 under the line, referving 1 in mind for the 10, then I prefix a point before 2, which fands in the first place of decimals; and on the left hand of the point, to wit in the place of Units or first place of Integers, I write down 1 (being the 1 in mind) which done, I find that the fum of the Decimals given is 1.215, that is, one Integer (whether it be a Perch, Yard, Foot, &c.) and 215 parts of an Integer, as you fee in the Example. In like manner thefe mixt numbers 32.056;7.07 and 1.9 being given to be added, their fum will be found to be 32.056 41.026, that is, 41 Integers and 26 parts 7.07 of an Integer, as you fee in the Margent; 1 .9 more Examples for the learners exercise 41 .026

.65	34.7	503.75
.025	0.35	0.32
.03	5.26	0.12
.705	30.31	504.19
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CHAP. XXV.

Subtraction of Decimal Fractions.

Aving first written down the greater of the two numbers given, (whether it be a whole number, mixt number, or decimal) and the lesser underneath the greater, according to the directions in the second Rule of the 24th Chapter. Proceed as you are taught in Subtraction of whole numbers: (by the Rules of the 4th Chapter) so if this decimal fraction. 784 were given to be subtracted from this decimal .837, the remainder will be.053, that is, 1800 parts of an Inte-

295.094 ger, in like manner it this mixt number 78.919 were given to be subtracted from 295.094, the remainder will be

may observe that 10 is borrowed as often as need requires, according to the Rules of Subtraction of whole numbers of one denomination: Note also, when the decimals in both the numbers given consist not of the same number of places, that decimal which is defective in places towards the right hand, must have the void places filled up with cyphers, or at least cyphers must be supposed to be annexed: so if this decimal .04338 be given to be subtracted

from this .65, the remainder will be found to be .60662, and the Work will frand as in the Margent, where you see the three void places are supplied with

cyphers, and then the operation is as in whole numbers, by borrowing to as often as the lower fi-

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gure cannot be subtracted from the upper. More examples of Subtraction of Decimals are these following.

24.04338	37.	.394
.65	0.104	-35
23.39338	36,896	.044

CHAP. XXVI.

Multiplication of Decimal Fractions.

7. TT Hen two numbers are given to be multiplied, and are both mixt numbers, or both decimal fractions, or one of them a whole number, and the other a decimal or mixt number, (which are all the cases that can happen) there is no neceffity of writing them down precifely one under the other as in Addition and Subtraction, for the product or number sought in Multiplication depends not upon any regular placing of the two numbers given: fo if this mixt number 56.3 were given to be added to this mixt number 1.30526 1.30526, they ought to be written one under the other, as you fee (ac- 56.3 cording to the second Rule of the 24th Chapter) but if they are to be multiplied one by the other. they may be written thus,

> 1.30526 55.3

II. In any of the Cases which may happen in Multiplication of Decimals, multiply the numbers given as if they were whole numbers, then cut off alwayes from the product by a point, comma, or N 4 line,

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line, fo many places towards the right hand, a there are places of decimal parts in both the num. bers given to be multiplied, that done, the figure or figures (if any happen to be) on the left hand of the faid point or line of feparation doth declare the Integer or Integers in the product, and thole on the right hand of the point are decimal part of an Integer: fo if this mixt number 56.3 (that is, 56 Integers and 2 of an Integer) be given to be multiplied by this mixt number 1 .30526, the product will be found to be 73.486138, that is, 71 Integers and 486138 parts of an Integer; for ha ving chosen that to be the Multiplicator, which will cause least work, and subscribed it under the Multiplicand ; (to wit, 56.3 underneath 1.30526) De I proceed according to the Rules of Multiplication of whole numbers, viz. having drawn a line underneath the numbers given, I multiply all the Multiplicand, to wit, 1.30526, as if it were a whole number, by 3 the first multiplying figure, and sub-

scribe the product thereof, which is 1.30526 391578 underneath the line, and 56.3 proceeding in like manner with the 391578 other multiplying figures 6 and 5, at 783156 last I find the total of the particular 652630 products to be 73486138; and because 73 486138 there are 6 places of decimal parts in both the numbers given, (to wit, 5 places of parts in the multiplicand, and 1 place in the multiplicator)I cut off o places to the right hand from the total before produced, so will it stand thus 73 486138 : wherefore I conclude that the true product is 73 486138, that is, 73 Integers and almolt . of an Integer, In

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In like manner, if this mixt number 246.27 (that is 246 193) were given to be multiplied by 35 Integers, the true product will be found to be 8618: aum. 75, that is 8618 Integers and 75 parts of an Integer, as you fee by the operation in the Margent, where you may observe that 246.25 two places are cut off from the total 35 number produced of the multiplication, towards the right hand, because 123125 here are two places of decimals in the 73875 multiplicand, (the multiplicator con-8618 75 lifting of Integers only) but if there had been decimal parts also in the multiplicator, fo many more places should have been cut off, as was shewed in the first Example.

Again, if thefe two decimals . 87 and 9 (to wit

and 2) were given to be multiplied one by the other, the true product will be found to e.783 that is 783 parts of an Integer, as you fee in the Example, where you may observe that the product is a fraaion only; for after 3 places (being the number of places of decimals in both the

numbers given to be multiplied) are cut off to the right hand, there remains no Integer on the left hand.

III. When the Multiplication is finisht, if there arise not so many places in all as ought to be cut off by the second Rule of this Chapter (which may often happen when the product is a fraction) in fuch case, as many places as are wanting, so many cyphers must be prefixed to the product on the left hand thereof, and then a point must be prefixt

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5.525

.0143650

ing given to be multiplied one by the other, I multiply 375 by 5, and there arifeth 1875, now ac. cording to the fecond Rule of this Chapter, I should cut off 6 places to the right hand, and here are but 4 in all, wherefore I prefix two Cyphers, to wit, as many as there are places wanting, and then prefixing a point, the true product will be .001875 1875; iq like manner if this mixt number 5 .525 be multiplied by this decimal .0026, the true product will be found to be .0143650 (or 143550) as you

may fee by the operation in the Margent, where one cypher is prefixed to the numbers ariling from the total Multiplication to discover the true pro-

duct.

IV. Decimal parts of an Integer may be reduced to the known or accustomed parts of fuch Integer by Multiplica-To reduce decition only, for if the decimal fraction known parts of given be multiplied by that number, the Integer. which declareth how many known

parts are equal to the Integer, the Product gives the number of known parts required : So this decimal fraction of a pound sterling, to wit, 8687 1. being propounded, I multiply it first by 20 (the number of shillings contained in a pound) and the product gives 17 shillings and .3740 parts of a

fhilling;

hear in value to another arthing, fo it appears that 8687 parts of a pound stering are 17 1. 4d 2f. very After the fame manhear. ner, a decimal fraction of any

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integer whatfoever may be reduced into the nown or accustomed parts of such Integer.

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A brief way to find

the value of any

decimal fraction of

a pound of English

A briefer way to value any decimal part of a pound of English money, without ofs of a farthing may be this, viz. the figure (if any happen) in the first place of the decimal being doubled gives thillings, also if

moneys. there be 5, or a figure greater than s in the fecond place, one thilling more is to be ad-

ded to the former ; lastly, when ; is taken from the figure in the fecond place, if every unit in the remainder be accounted as ten, and the figure in the third place as unities, thefe tens and units taken as one number and lessened by I give the number of farthings, which with the shillings before found declare the value of the decimal propounded; likewise if the figure in the second place (when

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(when any happens) be less than 5, every unit in fuch figure is to be accounted ten as before ; fo is the decimal before mentioned, to wit, .8687 1. the figure 8 in the first place being doubled gives shillings, also because s is contained in 6 which stands in the fecond place, one shilling more is to be added to the aforefaid 16 shillings, which will now be made 17 s. that done, the remainder of the faid 6 after 5 is fubtracted, to wit, 1 being efteemel as 10, and added to 8 (which ftands in the third place, and to be esteemed as units) gives 18, from which abating 1, the remainder is 17 farthings of 4 pence and a farthing; fo that the value of the faid decimal. 8687 1. is found as before to be in shillings 4 pence 1 farthing. After the same manne this decimal of a pound of English money, to wit 319 1. will be reduced to 6 shillings and 18 far things or 6 shillings 4 pence 2 farthings, which wants less than a farthing of the exact value of the decimal .319 /.

V. Having explained all the cases in Multiplica tion of Decimals; I shall here give See the questithe learner a tafte of their excellent ons from 49 to use, by some familiar questions 73 in the 10th whereby it will be evident, that what Chapter of the

is oftentimes performed by many Appendix. tedious Multiplications and Division Wa in the vulgar way, is effected for the most part by

one or two Multiplications in Decimals.

The first Example may be this, suppose there is the certain piece of Wainscor in form a rectangled parale nun logram commonly called a long square, whose breadth is 3 yards 3 of a yard, 1 nail and - of a nail; and the length 6 yards, and of a yard, the question is to fon

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chap.XXVI. Desimal Fractions. it in now how many fquare yards are contained in that lo in iece of Wainfcot; here because it is defired that . the he Superficial content may be given in yards, the parts f a yard as well in the breadth as in the length of he Wainfoor which are before exprest by the accuomed parts of quarters, nails, &c. must be reduced will nto decimal parts of a yard, which are as easie to e found by a yard fubdivided decimally, as the ommon parts of quarters and nails are found by hird yard vulgarly subdivided : but for want of a fron ard subdivided decimally, this Reduction may be gs of erformed by the seventh Tables of the precedent f the able of Reduction, viz. looking into the faid Tae in let, right against 3 of a yard, I find L nner his decimalfar-

Alfo the decimal correspondent to 2.0625 nail is-

And the decimal of - of a nail 2.015625

The fum of those three decimals (, 828124

Wherefore the breadth of the Wainfcot in yards and decimal parts 3.828125

Again, the decimal of half a yard .5, wherefore the length of the 6.5 Wainscot is

rt by The length and breadth being nultiplyed one by the other produce e is a he superficial content, therefore the > 24.8828125 rale. number of fquare yards required adth

Wherefore I conclude that 24 fquare yards and omewhat more are contained in that piece of Wainfcot.

Wainscot, and it is evident by the first place of the decimal that what is above 24 yards is more then but less then of of a square yard, or more strictly, it is more then but less than of a square yard, but by taking all the places in the decimal you have the exact answer to this question, because the common parts of quarters, nails, and quarters nails may be always exactly reduced into decimal but that seldom happens in other things; never theses, albeit by decimal operations you cannot alwayes hit the mark, yet you may come as near as is possibly to be imagined, and that with mus more ease then by vulgar computations in questions of this nature, as will appear by com

7. q. n. q. n. 3-3-1-1 4 12 add 3 15 4 60 add 1 61 4 244 add 1

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245 qua of nails.

paring the precedento peration with the con mon way of workin here subjected, viz. the syards, 3 quarters of a yard, 1 mail, and of a mail, (which express the breadth beformentioned) must all breduced into quarters mails by the sixh Rules the seventh Chapter, states will be found 24 quarters of Nails, as you see by the operation.

Again the 6 yards and half which express the length aforesaid, must likewise be reduced into quarters of Nails by the

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foresaid Rale, so there will be found 416 quarters of nails of a yard, as you fee by the operation.



quarters of nails.

Then multiplying the breadth and length one by the other, to wit, 245 by 416, the product will give 101920 for the superficial content of the piece of Wainscot in square quarters of nails of a yard ; now these square quarters of nails of a yard must be reduced to square yards, and the readiest way to perform that is to find first of all how many quarters of nails of a yard are contained in one yard in length, viz. fince there are 16 nails in a yard, there are confequently 4 times 16 quarters of nails, to wit, 64 quarters of nails in a yard in length, therefore 64 multiplied by 64 produceth 4096 fquare quarters of nails in a yard fquare ; mul laftly, I fay by the Rule of three, if 4096 fquare quarters of nails of a yard give 1 yard square, how many

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many yards fquare will 101920 fquare quarters of nails give: So will the Answer be found 24.366 vards, which is the same with 24 .8828125 before found by the decimal operation (for 3516 is equal to the decimal .8828125, as will appear by reducing them to a common denominator by the four. teenth Rule of the feventeenth Chapter.) Now! leave it to the Reader to judge which of these two wayes is the more expeditious, and fo let him take which liketh him best.

Example 2. There is a squared piece of Timber terminated at both ends with equal long squares, viz. the breadth of the piece of Timber is 1 foot inches, 3 of an inch, and thalf quarter of an inch; the depth or thickness is 1 foot 3 inches, - of an inch, and or half a quarter of an inch, and the length of the piece is 11 feet 10 inches, and 3 quarters, the question is how many folid or cubical feet are contained in that piece of Timber? The Anfwer may be found by decimal Multiplication in manner following, viz. Forasmuch as it is desired that the folid content may be given in feet, the parts of a foot as well in the breadth, depth, and length, which are before exprest by the accustomed parts of inches, quarters and half quarters must be reduced into the decimal parts of a foot, which are as easie to be found by a foot subdivided decimally, as the other common parts by a foot vulgarly subdivided; but for want of a foot subdivided decimally, this Reduction may be performed by the eighth Tables of the precedent Table of Reduction, viz.

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Chap XXVI	Decimal Fractions.	197
The decimal c	orrespondent to 3 in 3	.416
The decimal o	of an inch is	.062
The fum of the	ofe 3 decimals is———————————————————————————————————	488
In like manner of the depth or to will be reduced by	the common parts of inch hickness of the piece of the said Tables, into the	Timber
The decimal cor	respondent to 3 inches	525
The decimal of	half a quarter of an inch	is01
The fum of thefe	e 3 decimals is	28
Wherefore the	depth or thickness is	-1.28
Again, the accus	fromed parts of inches, or	. in the
ngth of the piece	e of Timber will be redu	iced to
nese decimals, wiz	Ano	
The decimal of	10 inches is-	833
The decimal of-	of an inch is	063
	2 decimals is-	
Wherefore the l	ength of the piece is-	11.895
Now if the brea	dth depth and length be	multi-
ted continually,	the last product is the foli	d con-
nt required, viz.	1.488 multiplied by 1.28	produ-
th 1 .90464, whi	ich multiplied by 11 .895	produ-
ta 22.65, &c. wh	erefore I conclude that 2	2 10114
eet, half a foot,	and fomewhat more than	nair a

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Example 3. How many Equinottial degrees are orrespondent unto 136 dayes, 21 hours, and 40 minutes?

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nutes? The Answer is found by multiplying the time given by 360, for as 1 day is to 360 degrees; so 136 dayes; 21 hours, and 40 minutes, to the Equinodical degrees required; but first the 21 hours and 40 minutes must be reduced to decimal parts of a day, by the tenth Tablet, thus

The decimal of 21 hours is _______.875
The decimal of 40 minutes is _______.02777
The fum of these 2 decimals is _______.90277
Therefore the time propounded is ______.136.90277

Which being multiplied by 360 49284 .99 &c

Wherefore I conclude that 49284.99 or very near 49285 Equinottial degrees are correspondent unto 136 dayes, 21 hours, and 40 minutes, which was required by the question.

CHAP. XXVII.

Concerning Division by Decimal Fractions.

I. In any of the Cases which may happen in Division, if the Dividend be greater than the Divisor, the quotient will be either a whole number or else a mixt number, but when the Dividend is less than the Divisor, the quotient must necessarily be a fraction; for a lesser number is contained in a greater once at the least, but a greater is not contained once in a lesser.

II. Sometimes the Dividend, whether it bes whole number, mixt number, or decimal fraction

Chap. XXVII. Decimal Fractions.

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is to be prepared by annexing a competent number of typhers thereunto, to make room for the Divisor: for is of 32.5 were given to be divided by 17.323 the Dividend 32.5 must be increased with cyphers at pleasure after this manner 32.30000, &c. Likewise if i were given to be divided by 360, the Division cannot be made till the Dividend i be increased with cyphers, which being annexed, the Dividend will stand thus 1.000000, &c. Here note, that the cyphers annexed in manner aforesaid do supply places of decimal parts, and will be ulefull in discovering the quality of the quotient accor-

199

ding to the fourth Rule of this Chapter.

III. After the Dividend is prepared by annexing cyphers, when occasion requires; (as in the last Rule) all the places thereof must be esteemed as one whole number (to wit confifting of unities or Integers) and fo is the Divisor to be esteemed whether it be a decimal fraction or mixt number for in all tases the Division must be performed in every respect according to the Rules of Division of whole numbers in the fixth Chapter. So if this mixt number 326.25 were given to be divided by this mixt number 12.3, you must divide in the same manner, as when you divide 32625 Integers by 123 Integers, also if this decimal , 8356 were given to be divided by this decimal .og, you are to divide in the fame manner, as when you divide 83 96 Integers by 5 Integers; and after the quotient is found, the degree or place of the first figure which ariseth in the quotient muft be inquired after ; viz. you must know how far such first figure is distant from the place of units, to the end that the point or line which is used to separate between the place 0 2

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place of unites (or first place of Integers) and the Ch first place of decimals may be duly placed .. This Di is the only knot in decimal Division, and may be or resolved by the following Rule, viz.

IV. In any of the Cases which may happen in Di-A general Rule to difcover the

quality of the quetient in all cafes of Divifion by decimal

vision of decimals, the first figure which arifeth in the Quotient, wil be alwayes of the same place or do gree with that figure or cypher of the Dividend, which at the first que stion standeth over, or at least be longeth unto the place of units is

the Divisor. To illustrate this Rule I shall give Es amples in all cases, and first let a mixt number b given to be divided by a mixt number, viz. Let it be required to divide 172 .5 by 3 .746, here (accor ding to the fecond Rule of this Chapter) the Di vidend must be increased with cyphers at pleasure fo will it stand thus 172.500000,&c. then Division being made according to the Rules of Division of whole numbers in Chapter 6, the Quotient arifing will be 46049.

3.746) 172,500000 (46049, &c.

Now it remaineth to separate the Integers in this quotient from the decimal parts to perform which, I subscribe the Divisor 3 .746 orderly underneath

> 3.746) 172.500000 (46,049 3.746

the first Dividual 172.50 (being that part of the Dividend

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This Dividend whereof the first question must be asked) ay be pratleast I imagine the Divisor to be so subscribed, and fo I find that the figure 3 which stands in the place of Units in the Divisor will be placed under 7, which is the place of tens, (or fecond place of Integers) in the Dividend, wherefore by the fourth Rule before given, I conclude that the first er of igure arising in the quotient must likewise stand que in the place of tens (or fecond place of Integers) and confequently the next place on the right hand must be the place of Units; so it is evident that the separating point or line must be placed between the figure 6 and o in the quotient, that done, the true quotient is found to be 46 .049, &c. to wit, 46 Integers and 49 parts of an Integer, and some. what more, for 46 42 is less than the true quotient, but 46 50 is greater than it, and therefore albeit, after the aforefaid Division of 172, 500000 by 3.746 is ended, there will be a remainder, to wit 446 which feems to be great, yet here it is lefs in #2lue than i part of an Unit or Integer, and if to that remainder you annex another cypher and continue the Division, you will proceed nearer the truth and not miss part of an unit of the true quotient, and in that order you may proceed infinitely near, when you cannot obtain the quotient exactly by Division of Decimals.

Example 2. Suppose this mixt number 2.34 be given to be divided by this mixt number 52 .125; (where you may observe that the Dividend is less than the Divisor) first (as before) annex cyphers at pleasure to the Dividend, to make room for the Divisor, then the division being prosecuted as in

whole

whole numbers, at length these figures will arise in

52.125) 2.3400000 (.0448,&c. 52.125

the quotfent, to wit, 448; and to the end the degree or quality of the first figure 4 may be disco. vered, Ysubscribe the Divisor 52.125 under the hift dividual 2.34000 (for fo far the first question did extend in the Division and thereby I find that the figure 2 which stands in the place of units in the divisor will be feared under 4, which is in the fecond place of decimals, wherefore I conclude that the first figure arising in the quotient must al to ftand in the second place of decimals, and consequently the first place of decimals (which is new on the left hand to the fecond) must be supplied with a cypher ; fo that if a cypher be prefixed on the left hand of 4, and then a point placed before that cypher, the quotient will at length be difco vered to be.0448,&c. or 448 and somewhat more that is to fay, 448 is less than the true quotient but da is greater than it, and if you will proceed mearer the truth, you may continue the divition, is directed in the first Example of this Rule.

Example 3. Where a whole number is divided by a decimal fraction, viz. suppole 82 Integers were given to be divided by this decimal .050; After cyphers are annexed to the dividend at pleafure, and

.056) 82.00000 (1464 28,85.

ok I.

the division profecuted as in whole numbers (to wit. 8200000 being divided by 56) thefe figures 146428 will arife in the quotient, now to the end the degree or fest of 1, the first figure in the quotient may be known, I subscribe the divisor .056 under the first dividual &z (for fo far did the first question in the division extend) and because the divisor is less than unity, I supply the place of units by a cypher or o prefixed on the left hand of the point of separation in the divisor; also I pre-

.056) 0082.00000 (1464.28,&c.

0.056

fix cyphers before, (to wit on the left hand of) the Integers in the dividend to represent a succession of places of Integers, (for the order of places in Integers is from the right hand towards the left. then I find that the cypher or o which represents the place of units in the divilor, doth sand under that cypher, which, represents the fourth place of Integers in the dividend (as you fee by the Example in the Margent) wherefore I conclude that the first figure arising in the quotient must also be seated in the fourth place of Integers, and consequently the 4 first places in the quotient will be Integers, and the rest a decimal, so that the true quotient is 1464 Integers, and 28 parts of an Integer, and fomewhat more, wie, 1464 .28 is less than the true quotient, but 1464 .29 is greater than it.

Example 4. Suppose this decimal .0129 be given to be divided by this decimal .5 : after division is finished accor- .5) .0125 (25

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Division of Book I 264 whole numbers, (to wit after 123 B divided by 7) thefe figures 25 will arife in the paocient; now to difcover the degree or feat of 21the firlt figure in the quotient, I Jubleribe the divilor .5 under the first dividual of2, and having .0125 (.025 (as in the laft Example) prefix ed a cypher on the left hand of 0.5 the point of feparation in the divifor, to denote or reprefent the place of units, I find that fuch cypher or place of units doth fand under the figure i, which is feared in the fecond place of decimals in the dividend wherefore I conclude by the Rule that the first fi gure which ariseth in the quotient must also be in the fecond place of decimals, and therefore prefix. ing a cypher to supply the first place of decidals and putting a point before that expher, the quen-Example 5. Suppole this decimal .8564 be given to be divided by this .008, first Tannex cyphers to the dividend at preasure, then profecuting the divilion as in whole numbers to wit dividing 850400 by 8 the quoticos) .856400 (107.050 ene ariting is 107050. now to difcover the degree or place of 1, the first figure in the quotienr, I hibicribe the divitor :008 under the first di-vidual .8, then I prefix 008)000.85640(107.05 a cypher to fet forth no rigo best . i decimal or 1890. of divior. : Z. lemano it prefix cyphers to represent places of Integers in the dividend, that done, I find that the typher or o which air plieth

Decimal Fractions. Chap XXVII. by 7) might the place of imiles in the divisor, doct need on to bride that cypher which is Rested in the third lace of Integers in the dividend, wherefore Itonia lude by the Rule, that the little figure arthing in he quotient must be also in the third place of the egers, and confessiontly the third lift places in he quotient will be thregers, and the relt a decihal, fo that the true quotient is 167 of or 169

Example 6. Let it be required to divide this des lea. simal fraction .73012 by this .32, first dividing dend 3952 by 32 as if they were whole numbers, the first fill ures arising in the quotient will be 2311. Now to be is iscover the quality or value of the said figures I subscribe the Divisor . 32 under the first dividual 73, then prefixing a cy-

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iven the divisor so subscribed (or 0.32

magined to be subscribed) s aforesaid, to represent the place of units in each di-s aforesaid, to represent the place of units in each ding of them, I find the cypher or o which supplyeth the lace of units in the divisor to stand under the o which represents the place of units in the dividend, wherefore I conclude by the preceding fourth Ehe Rule, that the first figure ariling in the quotient will tand in the place of units, and consequently the ollowing places of the quotient will be a decimal raction, fo that the true quotient is 2 .311 or 2 311 The reason of the foregoing fourth Rule will appear from the following Confidentionson

1. If the divisor be multiplied by the quotient, the product is equal to the dividend.

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2. If the divisor be multiplied by the first figure which ariseth in the quotient, the product is the first number to be fubrracted in the division, and confe. quently every particular place of that product is of the same degree with that figure or cypher of the dividend, which stands over such particular place when the fubtraction is to be made, for numbers of unlike denominations cannot be fubtracted one from the other.

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enumbers bezgii. T the faid fi the E	7175 10 045 114 80	up and a yalah	grafile s a ner forc and refer	
14.35)	269 .0625 143 5	(18.75	ing sodd Now ar Nog lod Notesticil	50
e inu Ass geb A	125 56	o findite sarpado liberty	glokelerek Ocesl e le go Swell fine	
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3.So that to find the degree or feat of the first figure in the quotient, is nothing else but to find what degree or feat that figure must have, which multiok I.

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multiplying the figure or cypher in any particular place of the divisor, will produce the same degree as that figure or cypher of the dividend hath, which stands over or at least belongs to such particular place of the divisor at the first question.

4. And because if a figure standing or supposed to fland in the place of unities in the divilor, be multiplied by a figure of the Tame place or degree. as that figure or cypher of the dividend hath, which at the firft quellion flandeth over, or at leaft belongeth unto the faid place of unities, the first place arising in that product will be of the samedegree or place with the faid figure or cypher of the dividend; (whether it be a place of Integers or decimal parts) therefore the truth of the faid fourth Rule of this Chapter is manifest, namely, look what degree or place that figure or cypher of the dividend hath, which stands over or at least belongs to the place of unities in the divisor at the first question in Division, the same degree or place hatt the first figure in the quotient

Now that the benefit of Division by decimal fractions may partly appear, I hall add two questions,

and fo conclude this Chapter.

Quest, 1. A Merchant bought of gold Place, 356 ounces, 13 penny weight, and 15 grains for 1160 pounds sterling, the question is what he paid for an ounce? Answer 3 1.—5 s.——4 divery near. The operation by decimals may be after this manner, viz.

By the second Tablet of Reduction 3.65

The decimal of 15 grains is _____.03125

The sum of these 2 decimals is ____.68125

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Then by the Rule of three 1 say, if 396.68125 ounces cost 1160 polleds, what 1 ounce? Here 'tis evident that if I divide 1160 by 356.68125, the quotient mill give the value of an ounce, to wit, 3.252 pounds for 3 pounds, 5 billings and - d. very near.

1356.68125) 1,169,000000 (3,252,&c.

Quest 2. Suppose the length of the Tropical year (or the space of time wherein the Sun running through the whole Beliptiek circle, confisting of 360 degrees is returned to the same Equinostial or Solfting point from whence he departed) to consist of 363 dayes, 5 hours, and 40 minutes, the question is to know the Suns mean or equal motion for day, to wit, what part of 360 degrees the Sun moved in a whole day? The operation by decimals, thus,

By the tenth Tablet of Reduction the decimal correspondent to 5 bours 2.2083333

The decimal of 49 minares is ____ 0340277

The sum of those decimals is -. 2423010

Cowherefore the rune given, in days

365.2423610

Then by the Rule of three, if 365, 242361 days give 360 degrees, (or a total circumference) what will 1 day give? Here if I divide 360 by 365, 242361, the gnoriens will give the diurnal motion required, which will be found very near .98564, &c. or 9566 parts of a degree, which decimal being reduced into the common Sexagenary parts (by the fourth

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fourth Rule of the 26 Chapter) will give 79-8. &c. and fuch is the Suns diarnal motion very near. according to the aforefald Supposition of the length of the Tropical year.

I shall here add the vulgar Sexagenary resolution of this question, that by comparing both wayes together, the excellency of decimal Arithmetick in calculations of this nature may be the more perspicuous.

The aforefaid question being stated according to the Rate of three will stand thus,

hours dayes degrees

5: 49-360-If 365 :

The first term in the Rule must be reduced into minutes (by the fixth Rule of the feventh Chapter) fo there will be found 525949 minutes.

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Likewise the third term I day must be reduced into minutes, which will be found to be 1440, as you to fee by the following operation.

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Then multiplying the third term by the fecond to wit 1440 by 360, the product is \$ 18400, which of being divided by the first term 525949 (according to the note in the ninth Rule of the 16th Chapter the quotient will give \$18400 parts of a degree which fraction being reduced into the accustomed Sexagenary parts (by the ninth Rule of the feven

teenth Chapter) will give as before 59: 8, &c. for the Suns mean diurnal motion; now which of these two wayes is the more expeditious I leave to him who is verft in both to determine.

CHAP. XXVIII.

The Rule of Three Direct in Fractions.

1. TO repeat fuch things as have already been declared in reference to the definition of this Rule, and also the due placing of the 3 given numbers would be superfluous; and if respect be had to the Rules of Multiplication and Division of fractions delivered in the 20 and 21 Chapters, the working

uced working of the Rule of three direct in fractions is you the same with that in whole numbers, to wit, muliply the fecond number by the third, (or the third y the fecond) and divide the product by the first umber, so the quotient is the fourth number ought: to wit, the answer of the question.

Otherwife thus,

Multiply the Denominator of the first number y the Numerator of the fecond, also multiply that broduct by the Numerator of the third number. and referve this last product for a new Numeraor, again multiply the Numerator of the first number by the Denominator of the second, also multiply this product by the Denominator of the hird number, so shall this last product be a new Denominator; lastly, the new fraction (whose Numerator and Denominator is found as aforelaid) is the fourth number fought, which, if it be a proper fraction, may (if occasion require) be reduced into the known parts of the Integer: (by the ninth Rule of the seventeenth Chapter) if an improper fraction, it is to be reduced into its equivalent whole number or mixt number, by the thirteenth Rule of the feventeenth Chapter.

Example, If 3 of a yard of Velvet be fold for 3 of a pound sterling, what shall - of a yard cost? Anfiver 40 1. Or 14 5.9 7 d. For according to the Rule I multiply the Denominator 4, by the Numerator 2, and the product is 8; this 8 I a-

gain multiply by the Numerator 5, and the product 3gives 40 for a new Nume-

rator: moreover I multiply the Numerator 3 by

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again multiply by the Denominator 6, so the last preduct is 34 for alnew Denominator; wherefore I conclude that 4 is the fourth number sought, which if it be reduced (according to the ninth Rule of the sewencement Thapter) gives 14 1. 24 defor

97 d.) for the Answer of the question.

II. When any of the three given numbers is a a hole number or mixe number, fuch number muft fert of all be reduced into an improper fraction (by the tench or eleventh Role of the feventeenth Chapter) to the end that all the 3 given numbers may be a fractions i moreover if after fuch Reduction, the first and third numbers be not fractions of Integers of the same particular denomination, fuch of the faid numbers which is of the leffer de. nomination, mult be reduced to a fraction of the greater (by the fixteenth Rule of the feventeenth Chapter) which preparations being performed, the reft of the Work is to be profecured according to the first Rule of this Chapter. An Example of this fecond Rule here followeth. If a quantity of Ambergreece weighing 1- 16 Troy be fold for 601. fterling, what are 19 grains worth at that rate? An-Swer 65 942 1. Or 2 5. 4 119 d.

This question being stated according to the 7 Rule of the 16. 1. gr. 8 Chapter will stand thus, 12 60 19 which 3 numbers will be reduced (by the tenth and eleventh Rules of the feventeenth Chapter) into these improper fractions

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But fince the third number 15% grains Twoy is not a fraction of an Integer of the same name with the first, (which is a fraction of a pound Troy,) it must be reduced into a fraction of a pound Troy, thus, 15% gr. is 15% of 10 of 10 of a pound Troy, which compound fraction will be reduced (by the 16 Rule of the 17 Chapter) into this single fraction, to wit, 15% lb. Troy, and so the 3 numbers will at length stand thus in the Rule.

Then working as in the first example of this chapur, the Answer will be found 51206 t. which being reduced (according to the 9 and 4 Rules of the 17 Chapter) is found equal unto 2 s. 4 119 d.

Another Example. When the 2 of 3 of 2 Ship is valued at 147 l.—11 s.—3 d. how much is the whole Ship worth? Answ.491 l.—17 s.—6 d.

Note, when in any question whatsoever a compound fraction, to wit, a fraction of a fraction, is one of the given numbers, such compound fraction must first of all be reduced to a single fraction; (by the 16 Rule of the 17 Chapter) so here, the compound fraction? of 3 being reduced into a single fraction gives 5 or 3 then say, if 3 be worth 147 l. 11 s. 3 d. what is t or the whole Ship worth? Ship l. s. d. Ship After due reduction 3 147: 11: 3 1 is made by converting the 147 l. 11s. 3 d. into pence, and that number of pence, as also the third number 1, into improper

By the 2. Tables in the Table of Reduction in the 23 Chapter, the decimal fraction correspondent to 3 penny meight is

The sum of those 2 decimals is _____.160416 Wherefore the first number in the 2 oz.

Also the decimal of 6 pence is ____.025

The sum of these two decimals is ---.525

the rule of three is _______ 62.525

Moreover by the faid Tablet 2. the

decimal of 1/2 of an ounce or 10 penny oz. weight is 5, wherefore the third number in the Rule of three is

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So that after the faid reduction is finisht, the 3 given numbers will stand in the Rule thus,

19.160416—62.525—1.5

Lastly, multiplying the second number by the third, and dividing the product by the first number (according to the Rules of Multiplication and Division of Decimals delivered in the 26 and 27 Chapters) the fourth number will be this, to wit, 4894, &c. that is four pounds ferling and 1894 parts of a pound, which decimal being reduced (according to the fourth Rule of the 26 Chapter) gives 175.—10 d.—3 far every near.

The proof of the Rule of three direct in Fractivons is the fame as in whole numbers, respect being had to the Rules of Multiplication in Fractions.

CHAP. XXIX.

The Inverse Rule of Three in Fractions.

I. A Fter a question belonging to this rule is due by stated (according to the seventh Rule of the eighth Chapter) and prepared if need require, according to the second Rule of the 28 Chapter. The operation will be the same as in the Rule of three Inverse in whole numbers, respect being had to the Rules of Multiplication and Division in Fractions, viz. multiply the first number by the second, and divide the product by the third; the quotient is the fourth number sought, to wit, the answer of the question.

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Or thes, 2 shit ye

Multiply the Denominator of the third fraction by the Numerator of the fecond, also multiply that product by the Numerator of the first fraction, and referve the last product for a new Numerator: again multiply the numerator of the third fraction by the denominator of the second, also multiply this product by the denominator of the first fraction, so is the last product a new denominator; lastly, this new fraction is the fourth number sought, or answer of the question.

Example, If of cloth, which is 1-3-yard in breadth, 3-1-yards in length will make a Cloak, how much in length of that stuff which is -8-yard in breadth will make a Cloak of the same bigness with the former?

Answer 9 yards.

Then, (after the first and fecond numbers are reduced into improper fractions) the three numbers will stand

Lastly, 8, 7 and 7 being multiplied continually give 392 for a numerator; also 5, 2 and 4 being multiplied continually give 40 for a denominator, whereby this improper fraction 392 ariseth, which (by the thirteenth rule of the seventeenth Chapter) will be found to be 9 32, or (the fraction being reduced into its least terms) 9 4 which is the Answer of the question.

Ex.2. Suppose when Wheat is at 2 1.-00 s.-6 d. the Quarter, the penny white loaf ought to weigh

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8 ounces and 1 penny weight of Troy weight; what ought it to weigh when Wheat is at 36 fhil. lings the Quarter? Answer 9 ounces and 1 11 penny weight.

The 3 given numbers being pence p.w. pence duly placed in the rule and re- 2000 : duced will ftand thus,-

And if the operation be profecuted according to the rule before given, the Answer will be found 181 3996 penny weight, or 9 ounces, 1-37 penny weight.

CHAP. XXX.

The Double Rule of Three in Fractions.

I. The Double Rule of Three is fo called, because it is composed of two fingle Rules, and may either be resolved at one Work by the Rule compound of s numbers, brelfe by two distinct fingle Rules of three, which latter way to fuch as understand the Rule of three in fractions is (as I conceive) less troublesome in the stating, and (in the method whereby I intend to profecute it) the same in operation with the former. This I shall manifest first in whole numbers, then in fractions.

Example 1. If I pay 28 thillings for the carriage of 3 C. weight for 50 miles, how much ought I to pay for the carriage of 17 C. for 84 miles? Answer 13 L.-61.-6d. 18

Of the 5 given numbers I make choice of three fuch which will make a fingle rule of three, and fay,

Which

Which rule I find (by the third rule of the ninth Chapter) to be direct, and therefore I multiply the third number 17 by the second 28, and the product which is 476 I place as a numerator over the divifor as denominator. Then with this fraction (whe-

ther it happen to be a proper or improper fraction) and the remaining two numbers in the question, which have not yet been used, I form a second rule of Three, and fay,

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Which being a rule of three direct, I work as a rule of three in fractions, according to the first rule of the 28 chapter, and fo find the fourth number to be 20084 s. or 13/.-63.-618 d.

Or the first lingle rule being varied, the operation will be thus, ano Wene as baviolar ed radi

sign to file owy of all miles, co. miles to C. no 1. By a rule inverse, 50 -- 3 -- 84 -- (150) -ngo lar) at sno from Comb Buon C. shipping 3. By a rule direct, 110 : 28: 17: (35984

fielinamilad I all Otherwise thus,

speiste en vollegelen ich ile Cyalm. 1. By a rule inverse, 3 -50m. 2. By a rule direct, 150 : 28

Thus you fee the two fingle rules to be varied be three manner of wayes in resolving the question

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propounded, and each way produceth the same Answer; the like diversity may be found in all questions resolvable by the doubte rule of three, or rule compound of 5 numbers.

Example 2. if 40 1 lin 2 of a year gain 21 l. what will 100 % gain after that rate in 7 of a year? Anfw. 5.1. -7 s. -9 d.

By 2 Single rules of three, thus,

1. By a rule direct, 203: 1: 100

2. By a rule direct, 2: 2500: 12:

Or by these two single rules,

year La year 1. By a rule direct, 2: 15 : 12: (105) Lita Hong by bas ladeuch

2. By a rule direct, 203: 105: 100 (32500)

Otherwise thus ,.

197. 1200 1. Ry a rule inverse,

year 2. By a rule direct; 406/ 2 1

Thus by 2 single rules of three varied three feveral ways, you fee the Answer of the question to be \$2500 1. to wit, 41. -7 s. - 9 1 d.

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CHAP. XXXI.

The Rule of False in Fractions.

J. W Hen a question propounded cannot readily be applyed to the Rule of three, or any of the vulgar Rules in Arithmetick; the best refuge for such as are not acquainted with Algebra is the Rule of two false Positions, which, for that it hath already been handled in whole numbers, I shall the more briefly touch upon in Fractions.

II. When a number is fought by a question, you are to feign or suppose some number taken by guess to be the number sought, and to make tryal whether that feigned number will answer the conditions in the question or not, by comparing the number resulting at the end of the Work, with the given number refulting from the true number fought; and if you find both those results to be the same, then is the number which you first took by guess the true number or answer of the question, but if the number resulting from the suppofititious number be either greater or less than the given refult, with which it ought to be compared (to fee whether you have hit the mark or not) fuch excess or defect must be noted for the Error of the first Polition, to wit, an excess must be fignified by this note t, and a defect by this -................

feigned, and after tryal is made therewith, to see valued whether it will perform the conditions prescribed I. I in the question, by comparing the results as afore and the

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faid the error of this fecond Polition, if too much, is not be moted by the if noo little by he fore-

IV. After the errors of both Politions are difcovered, the two numbers before supposed or seigned to be the number fought, must be multiplied by the sitern errors, that is, the first Polition by the feognderror, and the fecond Polition by the first error ; then if the notes of the errors are unlike, to wit, one of them t, and the other the fum of the faid products is to be taken for a dividend, and the fum of the errors for a divitor; but if the notes of the errors are both slike, to wit, both of them to or both the difference of the faid products is to be taken for a dividend, and the difference of the errors for a divident; laftly, the quotient ariling from the di-vition made by the faid dividend and divilor, gives the true number fought, or answer of the quettion, if it be forwable by the Pouls of Fulls. Thefe Roles are the fame im lubitance with those delines ed in the 15 Chapter, and may be funther illuffraed in the 15 Chapter, and may led by the following Questions.

Queft. . A Gentleman hired a fervant for a year for o pounds feeling, and a livery Cloak valued at a certain rate, but it happened that 2 of the year heing expired they fell at variance, and the or Geotleman put away his Tervant, giving him the g. Clock together with so shillings in money, which was the servants full due for the time of his fervice, the question is to find what the Cloak was be ee valued at? Answ. 21. 83. - od.

1. I suppose the Cloak to be valued at 3 pounds, ed and then feek how much thereof was due to the fervant.

222

3. For as much as the Cloak together with the by money which the fervant received ought to be e- first qual to the part of the Cloak, together with the white part of the oppoinds wages due to him at the end fred of 12 of the year, therefore 3 1. (the supposed are 1 all 10 together with 2 1. (the money which the fervant received) should be equal received in the close (bec due to the fervant at the end of _ of the year Divi together with & 4 (the wages due for the fame i Di time that is to lay, "L (the fum of 3 1. and 2 1) fo m flould be equafico 2 L (the fum of -7 1, and 7 1.) will but it is greater by wherefore the first Politi the f on for the value of the Cloak being 3 pounds, the

4. I make a second Supposition guessing the value of the Cloak to be 2 pounds, and proceeding the in every respect as with the first supposition I find as he the error to be to little; so that the two Post please tions with their errors will be as you fee :

error is found to be too much.

to their errors will be as you see:

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Chap XXXI. in Fractions Now in regard the wrors are fractions I may take in their stead, whole numbers in the same propor-tion, to wire, multiplying the Numerator of the fift fraction (or first error) by the Denominator of the seconds take the prode duch which is 6 in ftead of ng ga ar the firsterror to , likewise leavel W multiplying the Nameraof the fecond fraction, orni 150 6 he by the Denominator of the fift, I take the product viis) 12 (22 pounds the which is 4 instead of the ferond error 1 Or innd flead of the faid o and 4 I may take 3 and 2 which are in the fame proportion with 6 and 4, (or with and in Then multiplying the Positions and new ual more crosswife, and adding the products together out (because the lights are unlike) the sum is 12 for a are) Dividend, and the sum of the errors 3 and 2 is 5 for me Divifor, fo the quotient will be found to be 2 2/. (1) fo much therefore was the value of the Cloak, as 1) will easily appear if tryal be made with 2 1/2. in the fame manner as with the first feigned number.

Quest. 2. Virtualia (in lib. 9. cap. 3.) reporteth that King Hiero having given commandment for the making of a Crown of pure Gold, was in-value formed that the Workman had detained part of ling the Gold, and mixt the rest with as much Silver, find as he had stole of Gold; The King being much dis-post pleased at the deceit, recommended the examina-

fracule, who without defacing the Crown discovered the cheat in this manner viz. Experience telling him that a quantity of Gold would posses Jon els room or space than the same quantity of Sil-

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ver, and confequently that a mixt mais of Gold and Silver of the fame quantity, would take up fome mean fpace between the two former, he made a muse of pure Gold of the same weight with the Crown, likewise another mass of Silver of the same weight, then having put the Crown as also the other two Maffes feverally into a yeffel filled up to the brim with water, he diligently referved the water flowing over into another vessel, and from those 3 several quantities of water so expeld, he found out the quantity of Gald and of Silver in the 54. Crown: But forasmuch as Viermin delivers no Silv the practical operation, I shall here shew the same Will after the manner of Cardanus, Gemma, Frifius, and 911 other Arithmeticians.

be no Let us therefore suppose the weight of the Crom error as allo of the two feveral Maffes to have been 54 tien 2 Support alfo that by putting of the mass of Got the into the veffel, 3 lof water was expeld; by putting in of the Crown, 3 1 land by putting in of the mal minat of Silver, 4 1 l. The question therefore is to know Num. how much Gold and how much Silver the Grow infter was composed of. This may be resolved after the then

manner. Suppose 3 l, of Gold to be in the Crown wise, then there remained 217 the of Silver, now say be mer P

5-3-3-(1-4) of Silver, now say be mer P

5-4-2-(1-4) the Rule of 3, if 5 L 0 25 for how much 3 l. of Gold? Answer 1 4 l. Also if 5425 by of Silver expel 4 1/2 of water, how much 2 1, o fore w Silver, Answer, 141. of water, add therefore the the we water of the Silver and of the Gold together, to Silver wit, 1 4 and 1 5, fo there will arife 3 1/2 of water Gold, this ought to have been 3 1. (for so much over Ansme)

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flowed by pusting in of the Crown) but it is soo much by -2, wherefore - is to be noted with + for up de the error of the firft Position 3 L. Again, feign andhe ther quantity of Gold to have been in the Crown, to wit, 2 /. therefore there remained 3 /: of Silver, ne 0then fay if \$1. of Gold to

expel 3 %. of water, how much 2 1. of Gold? Anfw.

mc he 1 1 1. of water : Alfo if

he si of Silver expel 4 1 is of water, how much 3 4 of Silver? Answer; 24 then add 1 4 unto 2-7, the sum me will be 3 2 1, of water, this ought to have been nd 34 A but it is too much by 13, wherefore 13 is to be noted with + for the

om error of the second Postin 2 l. Here because the errors are fractions having a common Denoon instead of the errors,

Pos. 13 13 39 6)25 (4 7 lb. of Gold.

this then multiplying crof-

wife, to wit, 3 by 13 the product is 39, alfo 2 by 21 7 the product is 14 which subtracted from the tor-be mer Product 39 (because the errers are like) leave 10 25 for a Dividend, also the difference between the ate errors 7 and 13 is 6 for a Divisor; Lastly, dividing 5,25 by 6, the quotient is 41, fo much Gold thereof fore was in the Crown, and confequently (because the the weight of the Crown was 5 !,) there was 3 !. of to Silver which may be proved thus; Say if 5 1. of ter Gold, expel 3 l. of water, how much 41 l. of Gold ? ven Answer, 2-1. of water, again if 5 1. of Silver ex-W pel

pel 4 of water, how much of Silben ? Anfwer, I, of water, which being added to 2-1. the fum is 3 = 1. of water, to wit as much as flowed over, when the Crown was put into the vellel.

Here note, that in making a tryal of this na. ture, there is no necessity that the mass of Gold or of Silver be of the fame weight with the Crown I or whatfoever thing is to be examined, but of

what notable part of weight you pleafe.

Note alfo, that for the more cafe discovering prod of the Dividend and Divisor bysthe notes of + and ____ according to the fourth Rule of this Chapter, the following verse may be a help, to wit.

Addito dissimiles, Subtrabitoque pares.

Or thus,

Notes being unlike, Addition make; If like, leffer from greater take.

The Reader may fee more questions to exercise numb the Rule of Falle in the tenth Chapter of the Ap- fquar pendix, and the demonstration thereof in the ninth fquar Chapter of the fame. lquar of tha

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it felf, the product mail be equal to the found and tent first riven: JUXXX . A.H.D. ot of 27 for

before rise if it be fangered ther is, multiplied by

The Extraction of the Square cong and (or Quadrate) Root.

He Extraction of the Square-root is that by which having a number given, we find out mother number, which being multiplied by it felf roduceth the number given.



11. In the Extraction of the Square-root, the number propounded is alwayes conceived to be a square number; that is, a certain number of little squares comprehended within one intire great square, and the root or number required is the side of that great square, as will readily appear by this Diagram, where you see 25 little squares contained within one great square; now if the said content 25 be given, and the side or root of the square containing the said 25 little squares is required, the invention of such side or root is called the extraction of the square root; which root must

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be such, that if it be squared, that is, multiplied by it felf.the product must be equal to the square content firft given : So s is the fquare root of 25, for s times 5 is 25. Likewise this square number 49 being propounded his root is 70 100

III. Square numbers are either fingle or com-

pound.

TANA fingle fquare number is that, which be ding produced by the multiplication of extr A finds one fingle figure by it felf, is alwayes lefs on t then 100: fo an is a fingle fquare number procuproduced by 5, likewife 4 is a square num cond ber produced by 2.

V. All the lingle fquare numbers together with ther their respective roots are expressed in the Table mans next

following.

Squares. 1 4 9 78 25 36 40 64 81 2 3 4 5 6

Here in the uppermot rank of the Table are o ma placed the fingle fquare numbers of every particulaced lar figure, and in the other their respective roots; and therefore if it were demanded what is the IX. square root of 36, the answer will be 6. So the my so fquare root of 16 is 4, the fquare root of o is 3, quare &c. And contrarily the square of the root 6 is 36. quare umbe Also the square of 3 is 9.

When a square number is given that exceeds a, aft not 100, and yet is none of the square numbers othe mentioned in the Table, for his root you are to quare yet comes nearest unto it: so 45 being given, the and of root that belongs unto it is 6, and 10 being given. on to ven; his correspondent root is 3.

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VII. A compound square-number is that, which being produced by a number (that conlists of more places then one) mul- A compound quare-wumtiplied by it felf, is never lefs then ber. 100: fo 1024 is a compound square

number produced by the multiplication of 32 mul-

tiplied by it felf.

el VIII. To prepare any square number given for of extraction, put a point over the first place thereof is on the right hand (being the place of Units) then er proceeding towards the left hand, pass over the fen. Rond place, and put another point over the third place; also passing over the fourth place put anotheher point over the fifth, and fo forward in fuch le manner that between every two points which are ext one to the other, one place will be intermited: fo if the square root of 1024 be re-

mired, the first point is to be placed over , and the second over o as you see, and are o many points as are in that manner

blaced, of fo many figures the root demanded will tonfift.

the IX. Having thus prepared your number, you the may see it distributed by the points into several 3, quares: fo in the last Example, 10 is the first 36. quare and 24 the fecond, likewise if this umber 144 were propounded for extracti.

eds in, after points are duly placed according ers o the last Rule, you will fee I to be the first

to quare and 44 the fecond.

fs. X. Having drawn a crooked line on the right the and of the number propounded for extraction, gi. after the fame manner as is usually done in Divion to denote the place of the quotient) find the T. A

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of hand of the Resolvend 124, the work will stand syou see.

XV. Let the whole Resolvend except the first place thereof on the right hand (being the place of mits) be alwayes esteemed as a Dividend, then de-minding how often the Divisor before found, is contained in the said Dividend, and observing in that behalf the Rules before taught in Division, write the answer in the quotient, and also on the right hand of the

of Divisor, to wit, between the Dias for and the crooked line : fo if ou ask how often the Divisor 6
found in the Dividend i2, the 62) 124
in liver is 2, wherefore I write 2
in the quotient, and also after the
ivisor 6, as you see in the Margent.

WI. Multiply all the number which standers

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the left hand of the Refolvend, (to wit, before the crooked line) by the figure last placed in the tis otient, and write the product orderly under-

th the Resolvend (to wit, u-

der the faid product, subtract it independent the Resolvend, and subindependent the remainder under the set so 62 being multiplied by the product is 124, which if I the product is 124, which if I

62) 124 124

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hat the remainder is o; and thus whole Work being finished, the square root bei 1024 (the number propounded) is found to be

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Note 1. When the product before mentioneder uneat roneous, and then you are to reform it by placin 3. a leffer figure in the quotient, and no logged and Then

Note 2. For every one of the particular square (distinguished by the points) except the first onth 6, and colvena left hand, a Reforvend is to be fet apart, by bringin down to the remainder the congruent particula lotient fquare, as is directed in the 13 Rale; and as often 14. ule) wl a Resolvend is set apart, so often a new divisor ist be found by doubling or multiplying by 2 all ten the root in the quotient (confifting of what number the de g it c places foever.) ioslysti bda nasio en ice oi

Note 3. The Work of the 10,11, and 12 Rules fe finding of the first figure in the root, is but once cause t fed in the extraction of the root of a number co fifting of what number of places foever; but t Work of the 13,14,15, and 16 Rules is to be rept ted for the finding of every place in the roote faid p ne with cept the first.

The practice of these 3 Notes will be seen in the ne following Examples.

Example 2. Let it be required to extract whole

square root of 43623.

or the Shive Con as Having distributed the number propounded i to feveral squares by points, as isd ined) rected in the eighth Rule of the (to) Chapter, I demand the square root of the 4 the first square, which I find by t 5 rule of this Chapter to be 2, when list one placing 2 in the quotient a discont 43623 (2

the square thereof, which is 4, und 36, & the first square 4, I draw a line, and subtracting shell the from 4 the remainder is 0, which I subscribe und tal

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rneath the line. This is alwayes the first Work, hich is no more repeated in the whole Extractias was intimated in the third Note aforego-

Then bringing down the next square which is 6, and placing it next after the remainder o, the folvend is 36, and doubling the root 2 in the otient, the product is 4 for a Divifor (by the 13 d 14 Rules) and the Dividend will be 3 (by the 15

ule) wherefore I demand how ien the divisor 4 is contained the dividend 3, and not findg it once contained in it. L ace oin the quotient, and alnext after the Divisor 4, and cause the product of 40 mul-

lied by o, (the fast Character

the quotient) is Q, the resolvend 36 from which esaid product ought to be deducted remains the ne without alteration, therefore I bring down the next square, and place it after the remainder , fo will 3623 be a new refolvend, then doubling whole root in the quotient, which is 20, the

ifor will be 40 (according the fecond Note before menoned) and the dividend will be

2 (to wit, all the resolvend exnd by Rule 15.) wherefore I 40)03623

mand how often the divider is contained in the dividend 362, or how often 4 36, & though it be 6 times in it, yet (according to first Note aforegoing) I can take but 8, (for if I fuld take 9, and proceed according to the 15

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and 16 Rules, a number would arife greater than the refolvend, from which fuch number ariling ough to be subtracted) wherefore I write 8 in the quotient, and also after the divisor, 40; this done,

multiply 408 (the number of the left hand of the refolvend by 8 the figure last placed in the quotient, and the product to wit, 3 264 I subscribe under and subtract from the refolvent
ber of unities contained in the root fought; a because after the extraction is ended there happe to be a remainder, to wit 359, I conclude that root sought is greater then the said 208, but then 209, yet how much it is greater then 208, rules of Art hitherto known will exactly disconalthough we may proceed infinitely near, as in

next Rule will be manifest.

XVII. To find the fractional part of the rovery near, a competent number of pairs of phers, to wit, co, 0000,000000, or 00000000, are to be annexed to the number first propounded with cyphers annexed to be but one entire number, extraction is to be made according to the predent Rules, and look how many points were plat over the number first given, so many places of tegers will be in the root, the rest of the roots wards the right hand will be the Numerator of decimal fraction, which Numerator consists of so many places as there were points over

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exphers annexed : fo if 43623 were given as before; to find the root thereof (according to this rule) annex cyphers in this manner, and then if you extract it according to the Rules aforegoing, you

43623.000000 (208.861, &c.

will find the root arising in the quotient to be 208 .861, that is 208 Bei ; and because after the extraction is finisht there happens to be a remainder, I conclude that 208 461 is less than the true or exact root, but 208 100 is greater than it; fo that by annexing three pairs of cyphers to the number propounded, you will not mils _ part of an unit of the true row; also by annexing 4 pairs of cyphers, you will not miss part of an unit, and in that order you may proceed infinitely near, when you cannot obtain the true root. The whole operation of the faid Example here followeth:

> 43623.000000 (208 861, &c. The root. 408) 03623 3264 4168) 35900 33344 41766) 255600 250596 417721) 500400 417721 82679

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And then the root thereof 3, 1621776, &c. being extracted will be ______ \$3,1622776,&c. which (according to the third Rule of the 22Chapter) may be 3,1622776,&c. written thus

See here part of the Work in the extraction of the root of 10, which may give you a light and un-

derstanding of the rest. To some souls be isome

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XVIII. The extraction of the The Proof. fquare root is proved by multiplying the root by it felf, for that done, the product (in fuch cafe when there is no remainder after the extraction is finished) will be equal to the number whose square root was enquired; so in the first Example of this Chapter, the root 32 being multiplyed by it felf produceth 1024 the number propounded : but when after the extraction is finithed there happeneth to be a remainder, and that the root is found as near as you please in a mixt number of integers and decimal parts (by annexing cyphers as in the 17. Rule) then fuch mixt number being multiplyed by it felf must produce a mixt number less than the number first propounded for extraction, yet so near unto it, that if the figure standing in the last place of the Numerator of the decimal fraction in the root be made greater by 1, and then the mixt number fo increased be multiplyed by it felf, the product must be greater than the number first propounded ; fo in the Example of the 17. Rule, if 208. 861 be multiplyed by it felf, it produceth 43622. 917, &c. which is less than the propounded number 43623, but if 208. 862 be multiplyed by it felf, the product will be 43623. 335,&c. which is greater than 43623.

AIX. The square root of a Fraction is found in this manner, viz. To extract the extract the root of the Numerator (by the precedent Rules of this

Chapter) which root shall be a new Numerator. Also the root of the denominator is to be taken for a new denominator, so the new Fraction shall be the square root of the Fraction first propounded:

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ded: thus the fquare root of 16 is 1, viz the root of 9 is 3 for a new numerator, also the root of 16 is 4 for a new denominator. In like manner the fquare root of is is But here note diligently, that if the Fra-Elion whose square root is required be not in its leaft terms, it must first of all be reduced by the 4. Rale of the 17. Chapter before any extraction be made; for oftentimes it happens that the Fraction first given hath not a perfect root, but when fuch Frathion is reduced into its least terms, the root thereof may be extracted : fo in this Fraction 3, each term is incommensurable to its square root, but the faid being reduced to its leaft terms -, the root of this may be extracted, for the root of 4 is 2 for a new Numerator; also the root of 9 is 3 for a new Denominator; fo that 2 is found to be the fquare ran of 4 (equivalent unto -8.)

XX. When either the Numerator or Deno. minator of a Fraction hath not a perfect square root, fuch root is usually exprest by prefixing this Character, Jor Jq. before the Fraction given: To the squareroot of 13 is fignified thus / 13, or thus Jq. 13, because the root of 13 cannot be exprest by any true or rational number whatfoever, yet it may be found very near as in the next Rule.

To outralt the fquare root mear, of a fraction incommensurable to its quare root.

XXI. The square root of a Fraction which is incommensurable to its root may be found near, in this manner, viz. reduce the fraction proposed into a decimal by the third Rule of the 23. Chapter: the more places are in the decimal, the nearer will the root be

found, but the decimal must consist of an even number

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number of places, viz. either of two, four, fix, eight or ten, &c. places; then extract the fquare rost of that decimal as if it were a whole number according to the Rules aforegoing, which root found shall be a decimal expressing near the fquare roor of the fraction proposed.

So if the square root of 13 be required near, reduce the faid 13 into a decimal (by the 3d. Rule of the 23. Chapter) which will be found .81250000, &c. Then extracting the fgnare root thereof as if it were a whole number, it will be found .9013 very

XXII. The fquare root of a mixt number commensurable to its root, fquare root of is found in the fame manner as in a mixt the 19. Rule of this Chapter, the mixt number being first reduced into an improper fraction by the 10. Rule of the 17

Chapter.

So the fquare root of 34 33 will be found 5 7, viz. 34 22 being reduced into the improper Fraction 2209 the square root of the Numerator 2209 will be 47 for a new Numerator; also the fquare roct of the Denominator 64 is 8, for a new Denominator, fo is found 47 which (by the 13. Rule of the 17. Chapter) is 5 7 the square root sought. And here the fame caution is to be observed as in the 19. Rule of this Chapter; viz. the fractional part of the mixt number, or the improper fraction equivalent unto the mixt number, must be in the least terms before any extraction be made.

XXIII. When the mixt number To find the given is incommensurable to its fquare root Iquare root, prefix this Character bemear, of a mixt fore it, viz. Jor Jq. So the fquare mumber incomroot of 7 - will be thus expressed: 17mensurable to its root. or /q. 73 : but if you defire to find

the square root near, of a mixt number incommensurable to its root, reduce the fractional part of the mixt number into a Decimal of an even number of places, as in the 21. Rule of this Chapter, and annex the Decimal fo found unto the whole part of the mixt number; then esteeming the faid whole number and Decimal as one entire number, extract the Iquare root thereof according to the aforegoing Rules of this Chapter, and from the root found, cut off alwayes to the right hand, fo many places as there are points over the Decimal annexed, which number so cut off shall be a Decimal, shewing the fractional part of the root, and that on the left hand shall be the whole part of the root; so the square root of 72 will be found 2. 7688 yery near.

CHAP. XXXIII.

The Extraction of the Cube Root.

I. THE Extraction of the Cube Root is that, by which having a number given, we find another number, which being first multiplyed by it felf, and then by the product, produceth the number given.

II.

II. In the Extraction of the Cube A Cubical root, the number propounded is al- number. wayes conceived to be a Cube num-

ber, that is a certain number of little Cubes comprehended within one entire great Cube, and the root or number required is the fide of that great Cube: what a Cube is may be well exprest by a Die, which indeed is a little Cube it felf; wherefore if you place four Dice in a square form, that is, laying two and two in a rank, you shall have a square containing four Dice, upon which if you yet erect fuch another square of Dice you shall have a great entire Cube comprehending two times 4 that is 8 Dice or little Cubes ; and here 8 is the Cube number given, and two is the root, or number required : In like manner if you rank 25 Dice in a square form, viz. laying 5 in a rank, you have a square containing 25 Dice, now upon this square of Dice if you erect fuch another square, you shall have a great entire Cube comprehending 5 times 25, that is 125 little Cubes, and in this cafe 125 is the Cube number propounded, and 5 the root or number required.

111. A Cube number is either fingle or com-

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IV. A fingle Cube number is that, A fingle Cube which being produced by the Multi-

plication of one fingle figure first

by it felf, and then by the product, is alwayes less than 1000. So 225 is a fingle Cube number produced by 5 multiplyed first by it felf, and then by 25 the product; for 5 times 5 is 25, and 5 times 25 is 125.

V. All the fingle Cube numbers, and fquare num.

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bers, together with their respective roots, are expressed in the Table following.

Cabes	I	8	27	64	125	216	343	\$12	729
Squares							49		
Roots							7		

Here, in the uppermost rank of the Table are placed the single Cube numbers of the particular singures 1,2,3,4,5,6,7,8,9. in the next the squares of those singures, and in the lowest rank the squares themselves being the respective roots of the Cubes and squares in the uppermost ranks; and therefore the Cube root of 125 being demanded the answer is 5, and the Cube root of 216 being required, the Table will give you 6, and so of the rest.

VI. When a Cube number is given that exceeds not 1000, and yet is none of the Cube numbers mentioned in the Table; for his root you are to take the root of the Cube number, that being less comes nearest unto it. So 157 being given, the

Foot that belongs unto it is 5.

A compound Cube number is that, which being produced by a number (that confilts of more places than one) first multiplyed by it self, and then by the product is never less then 1000. So 157464 is a compound Cube number, being produced by 54 multiplyed first by it self, and then by 2916 the product, for 54 times 54 is 2916, and then 54 times 2916 is 157464, the compound Cube number propounded.

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VIII. To prepare a Cube number for extraction, out a point over the first place thereof towards the right hand, (to wit the place of units) then paffing over the fecond and third places, put another point over the fourth, and passing over the fifth and fixth put another point over the feventh, and in that order (to wit two places being intermitted between every two adjacent points) place as many points as the number will permit : fo 157464 being given, you are to place the points as in the Margent, and fo 157464 many points as are in that manner placed, of fo many figures, the root demanded will confift.

1X. Having thus prepared your number, you may fee it distributed by the points into feveral Cubes: so in the same example 197 is the first Cube, and 464 the second. 7464 In like manner if this number 7464 were propounded for extraction, after points are duly placed as before, you will fee 7 to be the first Cube, and 464 the second.

X. Having drawn a crooked line on the right hand of the number propounded to fignifie a quotient, find the Cube root of the first Cube and place it in the quotient : fo 157464 (5 I finding (by the fixth Rule of this Chapter) 5 to be the correspondent

coot of 157, I write 5 in the quotient, and then the work will stand as you fee in the Margent.

XI. Subscribe the Cube of the root placed in the quotient, under the firth 157464 (5 Cube of the number given: fo 125 125 being the Cube of 5 the root, (by the

fifth

stand as you fee. XIII. To the faid remainder bring down the next the Cube of the number propounded, (to wit the final

15746+ (5 125

the 3 next places) placing the fain faid Cube next after, to wit, on feat the right hand of the remainder, refo fo the next Cube 464 being placed land will be found this number 32464, which may be ripl

gures or cyphers that stand in in the

32464 refelv.

called the Resolvend.

XIV. Having drawn a line underneath the Refolvend, square the root in the quotient, that is, multiply it by it self and subscribe the triple of the tern said square or product, under the her

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32464 refolu. 75

whereof is 75, which I subscribe under the Resol-

resolvend in such manner, that the leate first place (to wit, the place of u- teen nits) of the said triple square less may stand directly under the am third place (or place of hundreds) ethe in the Resolvend : so the square wor of the root 5 is 25, the triple Di

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Chap.XXXIII. The Cube Root. vend in fuch manner, that the figure ; which is in the first place (to wit the place of units) in the triple product 75, may ftand under 4 which is feated in the third place of the refolvend, as you fee in the Margent. XV. Triple the Root or number in the quotient, and subscribe this triple number in such manner that the first place thereof, (to wit the place of units) may frand directly under the fecond of place (to wit the place of tens) in the Refolvend : fo the triple will of the root 5 is 15, which I subscribe in such manner, that 157464 125 next the figure ; which is in the first e findace(to wit the place of units)
in in the faid triple number, doth
the fand directly under 6, which is 32464 Refolv. on leated in the fecond place of the 15 der, esolvend, and the Work will aced hand as in the Margent.
here XVI. The triple square of the root, and the be riple of the root being placed me under the other as is di-Re- ected in the 14. and 15. Rules nul- foregoing, draw a line un-157464 (3 125 the lerneath and add them togethe her in fuch order as they are 32464 Refolve

the eated, and let the fum be e-if u- teemed as a divisor : so the tri-nage le square 75; and the triple the umber 15, being added toeds) ether as they are ranked in the nare work, the fum will be 765 for iple Divisor. fol-

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XVII.Let

fee in the Example.

XVIII. Having drawn another line under 157464 (:54 125 32464 Refolv. 75 IS 765 Divifor. 300

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the Work, multiply the tripl fquare before subscribed (asi directed in the 14. Rule) by the figure last placed in the quenent, and fubfcribe this product under the faid triple fquare; (to wit units under units, ten under tens, &c.) fo 75 being multiplyed by 4, the produc is 300 which I subscribe under 75, (the triple fquare) and th work will frand as you fee in the 1366 Margent.

XIX. Multiply

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XIX: Multiply the Agure laft placed in the quotient firft by it felf, and then the product by the triple number before fubfcribed, (as is directed in the 15. Rule of this Chapter) this done, fubferibe the laft product under the faid triple number, (to wit, units under units, tens under tens, &c.) fo 4 being fquared or multiplyed by it felf, the product is to, which being multiplyed by the triple number 15, the product is 240, this therefore I fubferibe under the aforefaid triple number 15, and the Work will stand as you see.

XX. Subscribe the Cube of the figure last placed in the quotient, under the resolvend, in such manner that the first place of this 125 Cube, (to wit the place of units,) may stand under the place of units in the refolvend : So 64 being the Cube of A. I write it under the refolvend 32464, in fuch manper that the figure 4, which 765 Divifor. is in the place of units in the

1157464 (54 ad 32464 Resolvend

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Cute 641 may fland under the be spo by fgure 4 which is feated in the imos 40 monds the place of units of the refol. the Margent. tiply to A

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XXI. Drawing yet another line under the work add the three laft numbers together in the fame order as they are feated, and fubtract the fum of them from the resolvend, placing the remainder orderly underneath ; fo the fum of the three last numbers as they are ranked in the Work is 32464, which if you fubtract out of the relolvend 32464, the remainder is o. Thus the whole Work being finished the Cube root of 157464 , (the number propounded) is found to be 54. he figure

Note I. When the fum of the three laft num. bers before mentioned is greater than the refolvend, the Work is erroneous, and then you are to reform it by placing a leffer figure in the quotient. 32461

Note 2. For every one of the particular Cubes (diftinguished by the points) except the hift Cube on the left hand, a resolvend is to be fet apart, by bringing down to the remainder the next Cube (as is directed in the 13. Rule.) And as often ast resolvend is set apart, so often is a new Divisor to be found, by adding the triple of all the root in the quotient f confifting of what number of places soever) to the triple of the square of such root, after they are orderly placed according to the 14. and 15. Rules.

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Note 3. The Work of the 10, 11, and 12. Rules for finding of the first figure in the root is but once used in the extraction of the root of any number what soever, but the Work of all the following Rates, is to be used for the finding of every place in the root except the first.

The practice of thele 3 Notes will be feen in

the following Examples.

Example 2. Let it be required to extract the

Cube root of 8302348.

Having distributed the number given into febe. Rule of this Chapter. I demand the Cube root of 8 (the first Cube on the left hand) which I find by

(the first Cube on the left hand) which I find by the fifth Rule of this Chapter to be 2, wherefore placing 2 in the quotient, 2nd 8 the Cube thereof under 8 the first Cube, I draw a line, and subtracting 8 out of 8 the remainder is 0, which I subtracting 8 out of 8 the remainder is 0, which I subtraction which I subtraction (as was intimated in the 3 Note aforegough the first work, and is no more repeated in the whole exacts the first work, and is no more repeated in the whole exacts the first work, and is no more repeated in the whole exacts the first work, and is no more repeated in the 3 Note aforegotraction (as was intimated in the 3 Note aforegointimated in the 3 Note aforegoing) then bringing down the next Cube, (to wit,
the figures standing in the three following places
of the number propounded) which is 302, I
place it after the remainder 0, so is 302 the refolthe refolvend, I feek for the triple of the square of the root, vizi the root in the quotient is 2, which multiplyed by it self produceth the square 4, the triple whereof is 12, this I subscribe un-Not der the refolvend, in fuch manner that the figure 2

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in the units place of this triple fquane 12, may stand directly under the figure 3, which is seated

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	. Resolvend.
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126	Divisor.

in the third place of the resolvend, (to wit, the place of hundreds) according to the 14. Rule aforegoing; Again I triple the root 2, which produceth 6, and fubfcribe this triple number 6 under the fecond place (or place of tens) in the refolvend, to wit, under o, (according to the is. Rule of this Chapter) then drawing a line under the Work, and

adding together the faid two numbers laft fabferibed, as they are ranked, the fum of them is 126 for a divisor, (according to the 16. Rule afore-

going.)

That done, esteeming 30, to wit, all the plat ces except the first or place of units in the refolwend, as a Dividend, I demand how often the divifor 126 is contained in 30, and not finding it once contained therein, I write o in the quotient, and now because the sum of the three numbers which ought to have been produced (according to the 18, 19, and 20. Aules of this Chapter) by the multiplication of o (which was last placed in the quotient) amounts to o, the refelvend 302 out of which the faid fum should have been subtrasted, remains the same without alteration, wherefore having drawn a line under the Work, I write down anew the old refolvend 302, and bringing down the next Cabe 348, I annex it to the faid

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302; fo there will be a new resolvend, to wit, 302348.

Then fquaring the root 20, (that is, multiplying of it by it felf) the product is 400, which I

triple or multiply by 3, and fubscribe the product 1200 underneath the new refolvend, in fuch manner. that the place of units in this triple quadrate 1200, may fland under the place of hundreds or third place of the resolvend 302348, to wit, under 3 (according to the 14. Rule.)

b-19 Again I fubscribe the etriple of the root 20. which is 60, in fuch a= manner that the place

ok of units in this triple di. root 60 may fland unit der the place of tens nt, or second place of the ers resolvend then to

ding together the two numbers last subscribed, to wit, 1200 and 60, in fuch order as

they are ranked in the Work , the fum is 12060 for a Divi-

for.

8 302348 (202

0302) Refolvend

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302348 Resolvend

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Again, esteeming the whole resolvend except the first place, (or place of units) as a dividend to wit, 30234, I demand how often i (the first figure of the divisor towards the left hand) is contained in 3. the correspondent part of the Dividend, and though it be three times contained in it, yet (according to the first Non at the end of the 21. Rule of this Chapter) I dare take but 2. for if I should take 3 and proceed according to the 18, 19, 20, and 21 Rules of this Chapter) a number would arise greater than the resolvend, (from which such number arising ought to be fubtracted,) wherefore I write 2 in the quotient.

Then multiplying the triple square 1200 before Subscribed, by 2, (the figure last placed in the most quotient) the product is 2400, which I subscribe nition under the said 1200, (to wit, units under units, rest and tens under tens, &c.) Alfo multiplying the as th triple root 60 before subscribed, by 4 (the quadrate of 2 the figure last placed in the quotient) were the product is 240, which I subscribe under the \$302 faid triple root 60, last of all I subscribe 8 the wort Cube of the said new root 2, under the ohersplace of units or first place of the resolvend, to wit, under 8, and having added together those three numbers last subscribed, to wit 2400, 240 and 8 as they stand in ranks in the Work, the sum of them is 242408, which being subducted from the resolvend 302348, there will remain 59940. Wherefore the Work being finished, I find 202 to be the number of unities contained in the Cube root of 8:02348 the number propounded : and because after the extraction is ended there happens

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to be a remainder, to wit \$9940. I conclude that the Cube root fought is greater then the faid 202 but les then 203, yet how much it is greater then 202. no Rules of Art hitherto known will exactly discover, although we may proceed infinitely

near as by the next Rale will be manifest.

XXII. To find the fractional part of the root very near, ternaries of cyphers, to wit, ooo, oocooo, or oooooooo, &c. are to be annexed to the number first propounded, then esteeming the number propounded with the cyphers annexed to be but one entire number, the Extraction is to be made according to the preceding Rules of this Chapter, and look how many points were placed over the number first given, fo many of the forore the most places in the Quotient are the Integers or uibe inities contained in the Cube root fought, and the ts, rest of the places in the quotient are to be esteem'd the as the Numerator of a Decimal fraction, which na. Numerator consisteth of so many places as there t) were points over the cyphers first annexed : so if the \$302348 were given as before, to find the Cube the worthereof, (according to this Rule) annex cyphers in this manner,

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And then if you profecute the extraction acording to the Rules aforegoing, you shall find he Cube root fought to be 202. 48, &c. that is, 02 48 and more, wherefore you may conclude hat 202 48 is less than the true root, but 202 40 is greater

areater than it, fo that by annexing two ternaries of cyphers, to wit, 6 cyphers, to the number propounded, you will not mils part of an unit of the true rose, alfo by annexing 3 ternaries of cyphers, to wit o cyphers, you will not mifs part of an unit of the true root, and in that order you may proceed infinitely near, when you cannot obtain the true root. The whole operation of the faid Example here followeth, where you may observe, that for the more certain and ease placing, as well of the numbers which conflitute the several Divisors, as of those which constitute the Ablatitious numbers to be subtracted from the feveral and respective resolvends, down-right lines are drawn between the particular Cubes of the number propounded, first distinguished by points as before.

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In like manner the Cube roost of 2 will be found to be near equal to 1, 25992, &c. that is, 1 25991 and more.

XXIII. The extraction of the Cube root is pro. ved by multiplying the root cubically, to wit, the root being first multiplied by The Froof. it felf, and then the product multiplied by the root, the number ariling or last product (in cafe there be no remainder after the extraction is finished) will be equal to the number propounded : fo in the first Example of this Chapter, the Cube rost 54 being multiplied firft by it felf produceth 2916, ten which being multiplied again by 54 produceth hat 157464, to wit, the number whose Cube root was in- red quired. But when after the Extraction is finished, Extr there happeneth to be a remainder, and that the tor root is found as near as you please in Integers and faid decimal parts, (by annexing cyphers as in the 22 Rule four of this Chapter) then such mixt number expressing the root, being multiplied cubically, must produce a mixt number less than the number first propoun-

ded, yet so near unto it that if the figure standing to in the last place of the decimal fraction in the root be made greater by 1, and the mixt number fo increafed be multiplied cubically, the product muft be not fed be multiplied cubically, the propounded : fo in many greater than the number first propounded : fo the Example of the 22 rule of this Chapter, if 202.48 be multiplied cubically it produceth 8301305. 49, ter,

&c. which is less than the propounded number 8302348, but if 202. 49 be multiplied cubically, there will arife 8302535. 49, &c. which is greater oot than the faid given number.

XXIV. The Cube root of a Fraction is found in were this manner, vie. extract the Cube root of the

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Numerator, (according to the aforegoing Rules) which root reserve for a new Nume-To extrall the rator; also the Cube root of the Denominator shall be a new Denomina-

Cube root of a fration.

tor : laftly this new Fraction shall be by the Cube root of $\frac{8}{27}$ is $\frac{2}{3}$, for the cube root of 8 is 2 the Cube root of the Fraction first propounded. in for a new Denominator. In like manner the cube is root of is is is. But here note diligently that the d: fraction whose cube root is required must be in its least terms before any Extraction be made, for of-tentimes it happens that the fraction first given that not a perfect root, albeit, when such fraction is in- reduced into its least terms, the root thereof may be ed, extracted: To in this fraction 16 neither the numerathe for nor denominator hath a perfect cube root, yet the and faid 16 being reduced to its least terms - 0, by the Rule fourth Rule of the 17 Chapter) the cube root of this unce the second of the second of this may be extracted, for the suberoot of 8 is 2 for a new numerator, also the suberoot of 27 is 3 for a new unce new numerator, so that the suberoot of 27 is 3 for a new senominator, so that the suberoot of \$\frac{8}{27}\$ (which is equal to \$\frac{16}{34}\$) is found to be \$\frac{2}{3}\$.

ea. XXV. The Cube root of a fraction which hath the not a perfect Cube root may be found near in this anner, viz. reduce the Fraction given into a De-imal fraction, by the third Rule of the 2; Chap-ter, the more places are in the Decimal, the nearer will the root be found, but the decimal mult con-lift of ternaries of places, to wit, either of three, six, atternoot of the Numerator of that Decimal, as if it d in were a whole number, (according to the Rules bethe ore given which root found shall be a Decimal

expressing

expressing year the Cube root of the Praction propounded.

So if the cuberoot of were required, I reduce the faid a lato a decimal whose numerator may consist of ternaries of places, to wit, into this . 66666666666666 &c. then extrading the cube root thereof, I find .8735, which is very near the cube root of

XXVI. The Cube root of a mixt number commenfurable to its root may be found in the fime manner as in the 24 Rule of this Chapter, the mixt number being first reduced into an improper fra-

ction (by the 10 Rule of the 17 Chapter)

So the cube root of 12.19 will be found to be 2.1 viz. reducing 12 into this improper fraction the cube root of 343 will be found 7 or 2 And here the fame caution is to be observed as in the 24 Rule of this Chapter, viz. the fractional part of the mixt number, or the improper fraction equivalent unto the mixt number, must be expressed by a Numerator and Denominator in the least terms be-

fore any extraction be made.

XXVII. When the mixt number whose Cube root is required hath not a perfeet cube root, this charaeter Je is ufually prefixed before fuch mixt number for the cube root of zel is thus expressed, Jc. 2-3 Likewife Jc. denotes the cube root of which is fraction, whose cube root is inexpressible by any true or rational number; but if you defite to know the cube root near of a mixt number which hath not a perfect cube root, reduce the fractional part of the hath mixt number into a decimal, (as in the 25 Rule of this gaste Chapter) and annex the decimal fo found unto the whole parroor Integers) of the mixt number ; then find i esteeming the faid Integers with the decimal fo an- decin nexed

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nexed as one entire number, extract the cube root thereof, and from the root found cut off alwayes to the right hand fo many places as there were points over the faid decimal annexed, which places fo cut off shall be the fractional part of the root, and those remaining on the left hand shall be the Integral part of the root: fo the cube root of 23 will be found 1. 334, and more.

XXVIII.I might here proceed to shew the extradion of the roots of the Biquadrate, (or fourth Powmy the fifth Power, &c. but their operations being exceeding tedious, and hardly intelligible without the knowledge of Algebra; I shall only in this place touch upon the Extraction of the Bignadrate-root, because it may be extracted by the Rules delivered in the 32C bapten, and refer the more curious Arichmetician for further fatisfaction in this matter, to my Trentile of the Elements of Algebra.

XXIX. A quadrate or fquare number multiplied

by it felf produceth a Biquadrace number So 4 multiplied by it felf produ- To sutraff the cath the Bignadrate 16. Therefore if a number be propounded and the Bique

Bignadrate

drate root thereof be required, first extract the quamdrate or fquare root of the number propounded, and then extract the fquare root of that root for the Biquadrate root fought. Thus if 20736 be a number 5 propounded, the Biquadrate root thereof will be uc found 12: for the fquare root of 20736 is 144, and the fanare root of 144 is 12. When the number given ot hath not a perfect Riquadrate xoot, you are to annex be gastennaries of cyphers, to wit, either 4,8,12, or 16, his the &c.eyphers, and then proceed as before; fo will you ed find the root near, whole fractional part will be z in- decimal, Thus the Biquadrate root of 7 will be found red near 1,62. CHAP.

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CHAP. XXXIV.

The Relation of Numbers in quantity.

1. THus far fingle Arithmetick, comparative A. rithmetick infues, which is wrought by numbers, as they are considered to have Relation one to another. The hard and in 20 20 18 180 10

II. This Relation confifts in quan-Bostius Arith Licaper al Stiry, or quality: ad var stollan

III. Relation in quantity is the reference or refpect, that the numbers themfelves have one unto qua another: As when the comparison is made between 6 and 2, or 2 and 6 : 5 and 3; or 3 and 5.

IV. Here the Terms or Numbers propounded are alwayes two, whereof the first is called the Antecedent, and the other the Confequent : So in the moc first example, 6 is the Antecedent, and 2 the Con. led h fequent : and in the fecond, 2 is the Antecedent, and 6 the Consequent. qual.

V. Relation in Quantity consists either in the ther : difference, or elfe in the rate or reason that is ton so

found betwixt the Terms propounded.

VI. The difference of two numbers is the remainder, which is left after subtraction of two propounded.

Difference. the less out of the greater: so 6 and 2 02, being the Terms propounded, 4 is the difference betwirt them : for if you fubtract 2 out ided of 6, the remainder is 4. remainder is 4.

VII. The rate or reason betwist two numbers is the quotient of the Antecedent divided by the Consequent : So if it be Rate or reason. demanded what rate or reason 6 hath to 2, Lanfwer, Triple reason : for if you divide 6 the Anrecedent, by 2 the Confequench the quorient is 3, 2 being contained just 7 times in 6. In like manner is there subtriple reason betwixt 2 and 6, for if you divide 2 by 6, the quotient is dor (which is all one) ; because 6 being not once found in 2, there remains 2 for the Numerator, 6 the Divifor being the Denominate tor of the Fraction given you in the Quotient, according to the o Rule of the 16 Chapter aforego ing.

te. Will. This rate or reason of numbers is either iefs is weather laupanu so leaps on

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I. L. Equal reason is the Relation that equal pumbers have unto one another:

Equal Leafon.

Equal Leafon.

E. Here the one being divided by the orbits the

he mocient is alwayes an Unit : for if it berdemans n. led how often 5 is in 5, the answer is a mol s of 8 wil numbers have one unto ano- od vd bebiv

he her and this is sither of the great wagant was is ten to the left, on of the lefs to the fon!

asserte and at believe a reason of the greater to the telescore when the greater Term is Antequal reason of 202, 5 to 3, and the like.

he Kill. Here the quotient of the Antecedent diandfritte So o divided by 2 the Quotiented

guent

The Relation of WIX Book I. 262 Cha 3. and 5 divided by 3 the quotient is 12. quen XIV. Unequal reason of the less to the greater, ifth is when the leffer Term is Autecedent : as of 2 to to. 6, 3 to 5, &c. antagr 10 sats 164w by 2, W M. Here the quotient of the Antecedent divithe q ded by the confequent is alwayes less than an unit : . th So z divided by o, the quotiene is or it and 3 divided by 5; the quotiene is 3. tient tonft XVI. Each of thefe kinds of unequal reason! (012 again fubdivided into five other kinds or varieties. XX whereof the three first are simple, and the other rided umerator, o'the Divisor being therrim eratows hole . Draw. The simple kinds of unequal reason an nnex 1.0 Manifold 201 Superparticulari 013, 11 Super heex partient. XX MIII. Manifold reason of the greater to the his k less is, when the Confequent is con 03. rained in the Antecedent divers Monifold Ros-X-X Equal Reason. times without any part remaining onta 25 4 to 2, & to 4, 16 to 8, which if efide called Double realon, because the less is contained uent ewicesinsthe greater of fo 6 to zels triple reafon to S 8 to 2 fourfold realong tac? Hi ti ? hat fo the - DODAN Herethe quorient of the Antecedentdivided by the confequent is alwayes a whole num nee, berg: 160 & divided by 2, the quotient is 4. cor XX. The opposite of this kind, viz. of the les XX to the greater, is caneu inumantion.

Stores in a Bramples hereof are 2 to 4, 4 to 8 findle of 10 es : 100 & 500 fo; &c. Likewife 2 to 6, 2 to 8 findle of 10 es : 100 & 500 fo; &c. Likewife 2 to 6, 2 to 8 from the 1 es of 100 es : 100 es to the greater, is called fubmanifold ided - XX T. Superparticular is, when the Anteceden trene designation of the conference quent

Chap. XXXIV. Numbers in Quantity.

quent; that is, an half, a third, a fourth, or a fifth part, &c. of the confequent, as 3 to 2, 4 to 3, sto 4, 6 to 5, and the like; here three divided by 2, the quotient is it and 4 being divided by 3. he quotient is 1 . In like manner & divided by , the quotient is it, and 6 divided by 5 the quotient is 1 wherefore I fay 2 and half 2 (that is 1) constitute 3: So likewise 3 and one third part of (viz.1.) conflicute 4, and fo of the reft.

ided by the Consequent is a mixt number; whose the hole part; as also the numerator of the fraction he examples last mentioned.

N.

nt

he XXIII. The opposite reason of subsuperparts his kind is Subsuperparticular, as 2 salar.

X-X IV. Superpartient is when the Antecedent

XXIV. Superpartient is when the ontains the Confequent once, and

tides divers parts of the confe- superpartient.

to 5, 9 to 5, 11 to 7, &c. here 5 divided by the quotient is 12, and therefore 5 contains \$ ne, and 2 of 3 , for 3 and two thirds of 3 (viz) conflitute 5.

AXV. Here the quotient of the Antecedent di-ided by the confequent is a mixt number, whole time part being an unit hath alwayes for the merator of the fraction annexed unto it a numer composed of more units than one : so the con-en reflect being made betwire ; and ; and ; the in interedent being divided by 3 the consequent, the solution is 1-2.

XXVI.The

Book I. Cha The Relation of XXVI. The opposite of this reason is Sub. X superpartient : Examples hereofant Supe 3 to 5, 5 to 7, 4 to 7, 5 to 8, 5 to 8, 3 Sub sperparti-9, 7 to 11, and the like. A XXVII. The mixt kinds of unequal reason are he] Manifold Superparticular, and manifold super-Num partient. an i XXVIII. Manifold Superparticular reason hem when the Antecedent contains the inds Manifold Saconfequent divers times; and belide perparticular. an aliquot part of the confequent as 5 to 2, 10 to 3, 17 to 4,21 to 5, and the like. XXIX. Here the quotient of the Anteceder divided by the confequent is a mixt number, who whole part confifting of more units than on hath alwayes an unit for the Numerator of the Fraction annexed unto it ; fo s divided by 2, the he quotient is 2 and 21 divided by 5, the quotien 1541. XXX. The opposite of this Reason Subman fold is Submanifold Superparticular; a Superparticu-2 to 5, 2 to 7, 7 to 7, 4 to 9, &c. XXX 1. Manitold Superpartient is, when the antecedent contains the confequen ence Manifold Suof the confequent; as 8 to 3 1.17 to le w perpartient. ave o 5, 19 to 4, 28 to 5, &c. XXXII. Here the quotient of the Anteceden II. divided by the Consequent is a mix night Submanifold Number, whose whole part as also herw superpartures. the Numerator of the Fraction and one of nexed unto it, is alwayes a Number III. composed of more units than one : so 8 divide Geom by 3, the quotient is 22, and 28 divided by 5, the XXXIII.Th quotient is 5-3

kl. Chap. XXXV. Numbers in Quality.

XXXIII. The Opposite here, is Submanifold att superpartient : as 3 to 8, 5 to 17, 4 to 19, 5 to

to 8, and the like.

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And these are the several kinds or varieties of are the Rates or Reasons that are found amongst Numbers, so that no two Numbers whatsoever hem is comprehended under one of these five hem is comprehended under one of these five inds.

CHAP. XXXV.

he Relation of Numbers in Quality, where; of Arithmetical and Geometrical Proportion.

D Elation in quality (otherwise called Prothe portion) is either the refeence or respect that the Reasons of Vide Euclid. L. S. & S. & S. & A. 3. d. 5. 8 A. Welfe which the differences of numbers ave one to another.

len II. Therefore here the Terms propounded his night alwayes to be more than two, for o-alle herwise there cannot be a comparison of Reaan ons or differences in the Plural number.

be III. This proportion is either Arithmetical, or

de Geometrical. th

Th

IV. Arlthmetical proportion is, when divers differ according to an equal difference, as 2, 4, 6, 8, 13, &c. here 2 is the common difference betwixt 2 and 4, 4 and 6, 6 and 8, 8 and 10, &c. So 1, 2, 3; 4, 5, 6, 7, &c. differ by Arubmetical Proportion, I being the common difference betwixt them.

V. Arithmetical Proportion is either continu-

ed or interrupted.

when divers Numbers are linked to when divers Numbers are linked to gether by a continual progression of equal differences. Such are the examples last propounded, as also these 1, 3, 5, 7, 2, 11, 13, &c. And 100000, 200000, 300000

400000, &cc.

will. In a rank of numbers that differ by Arithmetical Proportion continued, the fum of the first and last Terms being multiplyed by half the number of the Terms, the Product is the total fum of all the Terms: so it being demanded, how many strokes the Clock strikes between midnight and noon; the Terms of the Progression in this qualtion are Twelve, viz. 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12. for in that order the Clock strikes, wherefore if I multiply 13 the sum of 12, and 16 the first and last Terms) by 6 (being half the number of the Terms) the Product is 78, which is the total sum of all the Terms propounded being added together.

Terms by the half sum of the first and last Werms, & then likewise the Product will give you the total

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of all the Terms to 13, 11,947,5, 3 being given, their total is 48, for 8 the half sum of 13 and 3, the first and last Terms being multiplyed by 6, the number of the terms, the product is 48,

Arithmetical proportion continued, the mean being doubled, is equal to the fum of the extreams: 60,5,6,7, being given, 6 being doubled is equal to the fum of 5 and 7 the two extreams.

continued either upwards or down - Opwards wards, roup and man and and a state of the wards are state of the wards

XI. Upwards, when the Terms of the Progreffion increase, as these, 2, 4, 6, 8, 10, 12, &c. or these, 1, 2, 3, 4, 5, 6, &c. And this last rank is more particularly termed Natural Progref.

XII. Here when the first term is also the common difference of the terms, the last term being divided by the number of the terms, the quotient will give you the first term of the rank: again in this case the first term multiplyed by the number of the terms produceth the last term: so this rank 3,6,9, 12, 15, 18, 21, being propounded, wherein 3 is both the first term as also the common difference of the terms; I say 21 the last term being divided by 7 the Number of the terms the quotient is 3 the first term; contrariwise 3 the first term multiplyed by 7, produceth 21, the last term.

downwards is, when the terms of the progression decrease: such as are 35, Downwords. 32, 29, 26, 23, 20: And 40, 35, 30,

25,20,15,10,5.

XIV. Here when the last term is also the com-This Rale is in mon difference of the terms, he firt the moving of term being divided by the Number aforegoing. von the laft term : Again, the laft term multiplyed by the Number of the terms, produceth the first term of the rank.

For example, this rank 40, 35, 30, 25, 20, 15, 10, 5 being propounded, in which 5 is both the laft term, and likewife the common difference of the terms, I fav, 40 the first term being divided by 8 the number of the terms, the quotient is; the laft term : on the other fide 5 the laft term being multiplyed by 8, the product is 40 the first term.

XV. Arithmetical Proportion interrupted is, when the Progression is discontinu. 2. Interrupted. ed : as in thefe numbers 2,4, 8, 10;

here 2 and 4 being compared with 8 period mas and to differ according to Arithmetical proportion, but fo do not 4 and 8 differ, for 2 is the common difference betwixt 2 and 4, 8 and 10; whereas the difference betwixt 4 and 8 is 4. In like manner 8, 14, 17, 23. differ by Arithmetical

proportion interrupted.

X V I. Four numbers being given, that differ by Arithmetical proportion either continued or interrupted, the fum of the two means is equal to the fum of the two extreams: fo 5, 6, 7, 8, being given, the fum of 6 and 7, the two mean numbers is equal to the fum of g and 8, the two extreams : and 8, 14, 17, and 23, being propounded, the fum of 14 and 17 being added together is equal to the fum of 8 and 23.

XVII. Geo.

XV vers no reston number are equ one fro differ b 2.600

Chap.

XVI either c XIX

when d continu firt is t 15 2 to 4 wife the by Geome ple reale times in

XX.J i, the fi ower, he third biquadra er, the Gi of numb he root, rate, 24 kc.

XXI. roducetl gain mu eth the c nal being X VII. Geometrical proportion is, when divers numbers differ according to like resion : that is, when the reafons of Geometrical numbers, being compared together, proporsion. re equal. So 1, 2, 4, 8, 16, 32, &c. which differ one from another by double reafon, are faid to differ by Geometrical proportion, for as one is half 2, fo a is half 4, 4 half 8, 8 half 76, 16 half 32, &c.

XVIII. Geometrical proportion is L. Continued.

either continued or interrupted.

XIX. Geometrical proportion continued is, when divers numbers are linked tagether by a continued progression of the like reason: of this firt is the example last given : for as I is to 2, fo 1 2 to 4, 4 to 8, 8 to 16, 16 to 32, &c. So likewife the numbers 3,9,27, 81, 243, 729, &c. differ by Geometrical proportion continued, viz. by triple reason, each of them being contained three

imes in the next number that follows it.

XX. In Numbers continually proportional from , the first number from 1, is the root or first ower, the second is the square or second power. he third the cube or third power, the fourth the iquadrate or fourth power, the fifth the fifth powr, the fixeh the fixth power, &c. So in this rank of numbers, 1, 3, 9, 27, 81, 243, 729, &c. 3 is he root, othe fquare, 27 the cube, 81 the biquarate, 243 the fifth power, 729 the fixth power, kc.

XXI. The root being multiplyed by it felf roduceth the fquare, which being Menn 970gain multiplyed by the root produpertienals.

eth the cube, and fo each proporti-

nal being multiplyed by the root produceth the proportional

proportional next above it, and then the number comprehended betwixt 1, and the last number produced are called mean proportionals: so in this rapk of proportional numbers, 1, 2, 4, 8, 16, 32, &c., 2 the root being multiplyed by it self produceth 4 the square, which being again multiplyed by 2, produceth 8 the cube, then 8 being multiplyed by 2, the product is 16 the biquadrate, and so of the rest in their order, and here 2, 4, 8, and 16 are the mean proportionals in the rank propounded.

Continual bers by themselves, the numbers inmeans,
Briggius Arith Log. c.c. last produced may not unfitly be

given for the root, multiplyed by it felf, the product is 4, which being again multiplyed by it felf produceth 16, then 16 in like manner squard produceth 256, which likewise multiplyed by it felf produceth 65536, I say then that 2, 4, 16, and

256 are continual means betwirt and 65536.

XXIII. The continual means comprehended be twirt any number given, and 1, are discovered by a continued extraction of the square roots; for example 65536 being given, the root thereof extracted is 256, whose root is 16, then the root of 16 is 4, and the root of 4 is 2; so that at last find 256, 16, 4, and 2 to be continual means intercepted betwirt 65536 and 1, as before.

XXIV. In numbers that increase by Geometrical proportion continued, if you multiply the last term by the quotient of any one of the term

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Chap. XXXV. Numbers in Quality.

divided by another term; which being lels is next unto it, and then deducting the first term out of that product, divide the remainder by a number that is an unit lefs than the quotient, the laft quotient will give you the total of all the terms propounded in the progression, fo this rank 2 6, 18, 194, 162, 486, 1498; being propounded wherein the proportionals differ by Suboriple proportion, I firft take z and 6 the two firft terms. and dividing 6 by 2, I find the quotient 3, wherefore multiplying 1418 the laftterm, by 3 the quosient, the product is 4374, our of which if I dedudt 2 the firft term, the remainder is 4372, which being divided by 2 (vis. a number which is ahlunit less than g the quotient) the last quotient gives me 2186; which is the coral fum of the proportionals propounded, smal add wordes or small

XXV. Three proportionals being given, the square of the mean is equal to the product of the extreams; so 4, 8, and 16 being propounded, 8 times 8 being 64, is equal to 4 times 16, which is

likewise 64.

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XXVI. Geometrical proportion interrupted is, when the progression of like reason is discontinued; in such fort 2. Interrupted.

that four numbers being given, the

exlike reason is not found betwixt the second and t of third, that is betwixt the first and second, and the R1 third and fourth; of this fort are these numbers in-2, 4, 16, 32. here as 2 is to 4, fo is 16 to 32, for they differ by double reason; but as 2 is to 4, so tri is not 4 to 16, for 4 and 16 differ by fourfold reathe fon, 4 being contained 4 times in 16: so likewise rm 4, 8, 8, 16, differ according to Geometrical proded XXVII. portion interrupted.

XXVII. The numbers of Multiplication and Division are proportional; for in Multiplication, as I is to the Multiplicator, so is the Multiplicand to the product, or as I is to the Multiplicand, so is the Multiplicator to the product: Again, in Division as the Divisor is to I, so is the Dividend to the Quotient: or as the Divisor is to the Dividend, so is I to the Quotient.

XXVIII. Four proportional Numbers what sever being given, the product of the two means is equal to the product of the two extreams: So 2, 4, 16, 32, being propounded, 4 times 16 (which is 64) is equal to 2 times 32, which is likewise 64.

is 64) is equal to 2 times 32, which is likewise 64. Here endeth the first Book, which containeth all that is absolutely necessary, for the full understanding of common or practical Arithmetick. Such as desire to see how the same is performed by artificial, or borrowed numbers, called Logarithmes, may peruse Mr. Wingates Second Book, being a diffinit Treatise of artificial Arithmetick.

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APPENDIX,

CONTAINING

Choice knowledge in Arithmetick, both Practical and Theoretical; the Contents whereof are exprest in the following Page.

Composed by John Kersey.

Teacher of the

MATHEMATICKS.

At the Sign of the Globe in Shandois-Street in Covent-Garden.

Vox audita perit, litera Scripta manet.

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APPENDIX.

CHAP.

Appendix

F Contractions in the Rule of Three:

2. Of Rules of Practice by aliques pared.

3. Of Exchanges of Coins, Weights, and Mean

4. Practical queltions about Tare, Tret, Loss, Gain, Barter, Fasterfbin, and measuring of Tapeftry.

5. Of Interest of Money, and the construction of Tables to value Annuicies, &c.

6. A demonstration of the Rule of Three.

7. A demonstration of the Double Rule of Fellowsbig. 8. A demonstration of the Rule of Aligarien:

where also of the composition of Madicines.

9. A demonstration of the Rule of False.
10. A collection of choise questions to exercise all the parts of unigar Arithmetick, to which also are added various practical Questions, about the Mensuration of Superficial Figures and Salids, with the Gaping of Vessels.

to be multiplyed by 8. Sometimes last 10 mins lign hath reference to escribed but 11 mg colling or following numbers as have a little time placed over them, 103 × 2 t 6 or 2 t 0 × 3 fignification as sist to be multiplyed by the fam of 2 and 6. Like-

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An Explication of Such Notes or Characters which for brevity sake are used in this APPENDIX.

His t is a note of Addition, lignifying that the number which followeth fuch fign is to be added to the number preceding it, fo 3 + 4 im. plyeth that 4 is to be added to 3 !- femerimes alfo when no number is placed next after the faid note, it implyeth that the number prepeding is not exactly exprest; fo the fquare root of 2 is 1.414 tor This - is a light of Subtration, tignifying that

the number which followeth fuch fign is to be fab. tracted from the number preceding it; fo 6 2 fignifieth the difference between 6 and 2, or 2 to

be fubrracted from 6

"This x is a fight of Multiplication, fignifying that the number which precedeth fach figh is to be mul riplyed into, or by the number following the ligh : to 3 * 4 implyeth that 3 is to be multiplyed by 4; likewife by 3, 24 . 8 is understood the combine the M onals. matriplication of the numbers 3. 4 and 8'y oiz. 3 is to be multiplyed by 4, and the product is place to be multiplyed by 8. Sometimes also the frie fign hath reference to as many of the preceding +4= or following numbers as have a little line placed equal over them; fo 3 x 2 t 6 or 2 t 6 x 3 fignifieth that fignifi Like- qual c 3 is to be multiplyed by the fum of 2 and 6. wife

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wife 8-5 x 3, or 3 x 8-5 implieth that 3 is to be multiplied by the difference between 8 and 3 : Moreover if A and B represent two numbers, then AzB or A B implieth the product of the multiplication of those numbers: Likewise B-C x A figniffeth the product arising from the multiplication of the excess of the number B above the number C, by (or into) the number A. Again, if A Band A Crepresent two lines, then A B x A Cimphieth a rectangular Figure or long square made of the lines A B and A C.

Numbers placed as you fee in the 3) 18 (6

Margent denote a Divisor, a Dividend

and a Quotient, to wit, 3 the Divisor, 18 the Divid and 6 the Quorient; the like is to be underflood of other numbers fo placed.

Numbers placed after the manner of a fraction denote a quotient, which ariseth from dividing the

2×5×6 Numerator by the Denominator; so -- is equal

to the Quotient, which ariseth from dividing the the product of 3 multiplied by 4.

Four numbers placed as you fee in 2.4:: 6.12

the Margent are Geometrical proporti-

mals, viz. As 2 is to 4; fo is 6 to 12: or if 2 give 4, then 6 will give 12. Sometimes also they are placed thus, 2...4...6...12.

This = is a note of equality or equation; so by 3

ng +4=5+2 is signified that the sum of 3 and 4 is ed equal to the sum of 5 and 2: also 7-3 = 9-5
nat fignifieth that the difference between 7 and 3 is ece-qual to the difference between 9 and 5; that is, 7 ife leffened fened by s. Alfo 4 x 3 = 12 implieth that the prodoll of the multiplication of 4 by 3 is equal to 12.

> This is a fign of majority, light fying that the number on the left hand of fuch fign is greater than the number on the right hand thereof; fo 5 > 1 implieth that 5 is greater than 3.

This is a ligo of minerity, lignifying that the number on the left hand of fuch ligh is lefs than the number on the right hand thereof i fo ; < im. plieth that 3 is left then 5.

This Character J or J q. lignifies the fquan root of the number which follows it, fo / 144 in

plies the fquare root of 144, to wit 14.

Alfo this Jc, fignifies the cube root of the num. ber which follows it, fo Jc. 1728 fignifies the cube root of 1728, which cube root will be found to be se a gariour, which artech from dividing is

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the Princes, which wilch from dividing the

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APPENDIX

CHAP. I.

Of Contractions in the Rule of Three.



Uch as are well verst in the parts of Arithmetick, which have been fully laid open in the precedent Book, and are mindfull of the Norse or Symbols before explained, will find no difficulty in the 1, 2, 3, 4, 5.

id to Chapters of this Appendix, wherein divers impendious operations no less delightfull than fefull are methodically handled, and the rest will as easie to such as are but meanly acquainted ith Geometrical demonstration.

11. To repeat the brief wayes of Mulsiplication fet eth in the 10,11, and 12 Rules of the fifth Chapter, those of Division, in the 11, 15, and 16 Rules of

the fixth Chapter aforegoing, would be a superflu or a ous work, and therefore I shall presuppose the Res fant der to be throughly acquainted with them, as all wind with competent knowledge, in the operations of the fractions both vulgar and decimal.

III.It will be no fmall advantage to the Practice Arithmetician, to have by heart not only the com

mon Table of Multiplication 24 but this also in the Margen rthi 36 to the end that when a nun 48 ber is given to be multiplie 60 or divided by 12, (whi 72 happens in the Reduction 84 Shillings to pence and the con 96 verse) the product or quotie uced 108 may be written down in of 240, line only, as in the Example qu following,

4736 12) 56832(4736 hich 12) 41664 (3472

IV. When a whole number is given to be divid he far by a Divisor, which is equal to the product of ivide Multiplication of two fingle figures, inftead of viding by that Divifor you may first divide by o ed in of those fingle figures, and then divide the quotie wide by the other, so will the last quotient be the same Divide if the Division had been finisht by the Divisor and 86 given: thus if 3466 farthings be given to be reduced. to shillings, because 8 x 6 = 48 I first divide 3466

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l'ix fo there will arise 433 flu or a new Dividend, and Rea farthings remain, then I alforivide the faid 433 by 6,

8) 3466 6) 433 (72 . . 25

othere will arise 721, or

othere will arise $72\frac{1}{6}$, or 2/hillings 2 pence, which with the 2 farthings relation in the first Division make in all 72s.: $2\frac{1}{4}d$.

om which is the very quotient, when 3466 farthings are ivided by 48. Note that you are to reserve a trhing for every unit remaining of the first Division by 8, and two pence for every unit remaining of the second Division by 6. The reason of the operation is evident, for $\frac{1}{6}$ of $\frac{1}{8} = \frac{1}{48}$.

In like manner, if 7136 pence are given to be record into pounds, because 240 d = 1?. also 6 × 40 and 240, therefore if 7136 pence be first divided by 6, the quotient will give 1189 six pences, and 2 pence that is, then if 1189 be divided by 40, (that is by a feer 9 the last place of the Dividend towards the right hand is cut off)

he right hand is cut off)

ne quotient will be 29 1. 6) 7136

and there will remain 29 . 6) 7136 . s. d. x pences or 14 s. 6 d. 40) 1189) 29:14:8

56

pence remaining of the first Division, and the aid 29 1, makes in all 29 1. : 14 s. : 8 d. which is be same with the quotient, when 7136 pence are of ivided by 240, for 30 of 1 = 140.

Again, suppose 3463 pence are given to be reduited.

Again, suppose 3463 pence are given to be redu-your dinto shillings; for asmuch as 4 × 3 = 12, I first vide 3463 by 4, so there will arise 865 for a new medividend and 3 pence remain: then I divide the chaid 865 by 3 so there will arise 288 in or 288 x.

ehipun:

Appendix.

4), 3463 3) 864 (288 .. 7

a d. which with the : pence before remaining make 288 s. 7 d. which is the same with the quotient, when 346;

pence are divided by 12, for - of - = -1

V. In the Rule of Three as well direct as inverte. when the Divisor with either of the other two given numbers may be feverally divided by fone common measure, without leaving any remainder, the quotients may be taken for new terms and proceeding in like manner as often as is possible the operation according to the venth Rule of the eighth Chapter, or the fecond Rule of the nint Chapter, will be much contraded ; fo if it be de manded what 52 yards of Cloath will cost as the rate of 21 1. for 14 yards; the Answer will be found 78 pounds, in manner following.

> 14 . . 21 . . 52 2 ... 3 ... 52 1 ... 3 ... 26 .. (78

In the first rank you may observe that the Divifor 14 and the fecond terman, being feverally di- their wided by their common measure 7, (the three new be de terms in the fecond rank) will be 2,3,52. Again to 4 of the fecond rank the Divifor 2 and the third tern foun sabeing severally divided by their common mea- see. fure 2, the three new terms (in the third rank) will be 13,26, Laffly, working with these according to the Rule of Three direct, the Answer to the question (or fourth term) will be found to be 78.

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Another Example, If 21 men will finish a work in 16 dayes, what time must be allowed to 12 men for the finishing of fuch a work? Answer : 28 dayes.

> dayes men 21 ... 16 ... 12 7 ... 16 ... 4 7 ... 4 ... 1 (28 dayes

In the first rank you may observe, that the Divifor 12(for the rule isinverfe) and the first term 21 being severally divided by their common measure 3, the three new terms (in the fecond rank) will be 7,16,4. Again, in the second rank, the Divisor 4. and the second term 16, being severally divided by their common measure 4, the three new terms in the third rank will be 7.4.1. Laftly, working with thefe as the Rule of three inverfe requires, the Answer to the question (or fourth term) will be found 28.

VI.In the Rule of three, as well direct as inverse. when the Divisor and either of the other two terms are fractions having a common denominator, the faid denominators may be rejected, and their numerators retained as new terms : fo if it be demanded what is the value of 7 of an Ell, when nin 1 of an Ell are worth 66 pence, the Answer will be found 154 pence, and the Work will stand as you ca- fee

> 3 .. 66 .. 7 3 .. 66 .. 7 1 .. 22 .. 7 (154

Another

Another Example. If 3 3 yards of Scarlet cloath cost 81: 15 3. what is the price of one yard at that rate? Answer 21: 63.8 d.

$$\begin{array}{c} \frac{17}{4} \cdots \frac{25}{4} \cdots 1 \\ 15 \cdots 35 \cdots 1 \\ 3 \cdots 7 \cdots 1 \cdots \left(2\frac{1}{3}l\right). \end{array}$$

V11. In the Rule of three as well direct as inverse, when the Divisor only is a fraction, either of the other two terms may be reduced to a fraction of the same Denominator, and then the Denominators may be rejected as before in the sixth Rule; also when one of the three given terms is a fraction, and is not the Divisor, the Divisor may be reduced to a fraction of the same Denominator with the fraction sirst given, and then the common Denominators may be likewise cancelled.

An Example of the first Case may be this, if - of a yard cost 14 s. what is the price of 1 yard? Answer

16 Billings.

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An Example of the second Case; if of stuff which is 3 of a yard in breadth, 7 yards in length will make a Garment; how much of that stuff which is one yardin breadth will be sufficient for the same purpose? Answer 5 yards.

Rules

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Chap. II. Rules of Practice by Aliquot parts. 289

Rules of 3 \\ \frac{1}{4} \cdots 7 \cdots \frac{1}{4} \cdo

CHAP. II.

Rules of Practice by Aliquet parts.

1. A N Aliquot part takes its name from the Latine word aliquaties, for (according to Enclid) an aliquot part is of a greater number, fuch a part which being taken (aliquoties or) certain times doth precisely constitute that greater number, so 3 is an aliquot part of 12, for 3 taken four times doth exactly make 12, without any excess or defect; in like manner 4 is an aliquet part of 20, because 4 taken 5 times doth precisely make 20; but 7 is not an aliquot part of 20, for 7 taken twice doth want of 20. and being taken thrice doth exceed 20; this kind of part last mentioned is by Euclid called pars aliquanta, of which there will be no use in this place.

II. When the Rule of Three direct hath I or an Integer for the first term, it is commonly called a Rule of Practice, either from the great ufe and pradice thereof in common affairs, or else for that me questions of this nature, may be resolved by operations more speedy and practical than those of the

Rule of Three.

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III. The

200 2112 Balls of Prestice 21 Appendix

III. The choicest of these Rules of Practice may be reduced to 5 Cases, viz.

When the price 2. Of pounds and failings.

2. Of pounds and failings.

3. Of pence under 12.

4. Of skillings and pence.

5. Of pounds, skillings, pence,

with parts of a penny.

All which cases with others of the like nature

are handled in their order.

IV. Any even number of shillings is either $\frac{1}{10}$ of a pound, (that is 2 shillings) or else is composed of $\frac{1}{10}$ l. (to wit 2 s.) taken certain times: so 8 s. is composed of $\frac{1}{10}$ l. (or 2 shillings) taken four times, in like manner 18 s. is composed of $\frac{1}{10}$ l. taken nine times.

V. When the price of 1 or an integer of what name foever is 2 shillings, the price of as many Integers as one will of that name is discoverable at first sight, to wit by accounting the double of the figure which stands in the first place (towards the right hand) of the said number of Integers, as shillings and the rest of the said number as pounds: so 345

yard sat two shillings the yard shillings the yard shill. yards yard will cost 34 l. 10 s. for the double of 5 is 10, which I write down apart as shillings, then esteeming the re-

maining figures towards the left hand, to wit 34, as an entire number of pounds, the Answer will be 34 l. 10 s. This contraction is nothing else, but dividing the num-

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Chap. El. be Alian is required by 10.

M	Molog gai	ir	Bill.	20	7	ot st te isl
		90rds . 436	Anfw.	1.	. s.	1
	yar	d 708	Shill.		yards 120	
		yards 230	Austra	1.	5.	

VI. When the given price of 1 or an Integer is any even number of hillings greater than two shillings, multiply the number of Integers, whose price is required, by half the given number of hillings, with this caution, that the double of the figure which ariseth, in the first place of the product he written apart as shillings, and the rest of the product as pounds: so if it be demanded what 218 yards at 8 shillings the yard will amount unto,

the Answer will be found 87 l. 4 s. for I multiply 218 by 4, (which is half 8 the given number of shillings) saying, 4 times 8 is 32, here the double of 2 (to wit, of that figure

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which is to possess the first place in the product)
is 4, which I set apart as shillings, keeping 3 in
mind for the three tens, again 4 times 1 is 4, which
with

with three in mind man. Practice Appendix.

8, fo I conclude that the Answer to file year rais.

87 1.4 s. The reason of this contraction is evident from the fourth and fifth Rules aforegoing. More examples of this Rule are these following.

yard s.	yards
I . 14	436
Anj	/: s.

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yard I.	• •	18		yards 230
		(w:	l. 207	s.

VII. Any odd number of shillings is either compos'd of $\frac{1}{10}l$. (or 2 s.) and of $\frac{1}{20}l$. (or 1 s.) or else it is compos'd of $\frac{1}{10}l$. (or 2 s.) taken certain times, and of $\frac{1}{20}l$. (or 1 s.) So 3 s. is compos'd of 2 s. and 1 s. Also 7 s. is compos'd of 2 s. taken three times and of 1 s. Likewise 13 s. is compos'd of 2 s. taken six times and of 1 s.

VIII. When the given price of 1 or an Integer is an odd number of shillings, work for the greatest even number of shillings contained in that odd number, according to the fifth or sixth Rule aforegoing, then for the odd shilling remaining, take — of the number of Integers, whose price is required (by the 16 Rule of the sixth Chapter of the preceding Book.) These two results added together give the Answer to the question:

question : fo if it be demanded what 2344 ounces at 13 s. the ounce will cost, the answer will be found 1523 1. 12 s. For if (according to the fixth Rule of this Chapter)

I multiply 2344 by 6, oz. (to wit, by half the I .. 13 .. 2344 remainder, when one is abated from 13 the given number of shillings) there will arise

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1406 .. 8 14061. 8 .. Then ta- 11 navig sale and W117. 4 king of 2344 there that bar shoung to shino rumber af Integers whole pricality gravilia Aliw which being added to di manin 13230 12

Still.

the former product as fouborq elle gives 1923 1215. for the las wer to the queltion! Note, When & fhillings is the given price of or an Integer, the briefest way will be to rake Wof the number of Integers, whose value is required. for fuch quotient will give the pounds and hil-

lings, which answer the question ! 10 2347 offices at 3 s. the ounce amount unto 586 1. 15% for E of 2347 is 5861 or 5861. 15 . But when the given price of 1 is any other odd number of shillings, this eighth Rule will be as compendious as any other whatfoever.

More examples of this Rule are these following:

yard	Sill.	yards
I	19	739
10.		l. s.
43	- 1 1	665 2
0		3619
	Anfro.	702 I

8. b. c. m.

at is a the overshmy coil, field and sail a st in found it 23 L. 12 1. 2481. is fallording to the line

· Bill.

I moleigly 2384 by & 276 (.wloyd . iv or) remain er, Bben Vae

Rule of this

Anfw.

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I.K. When the given price of at pr an Integer confilts of pounds and shillings, first multiply the number of Integers whole price is required, by the number of pounds in the faid giten price, and subscribe the product as pounds a then proceed with the skillings in the said given price, according to the fixth or eighth Rule of this Chapter, and haying subscribed that which ariseth under the seforefaid product of pounds, add them all together for the answer of the question : fo if it be demanded what 3 28 hundred weight wall amount unto at 21. 17 s. per C, (on one hundred weight) the emfer will be found to be 9346, 16 c. as by the operation is evident, price of this any

was as compending as any eramples of 16 2 7578 are this callowing:

> 17. 656 .. 0 262 . 8 16 .. 8

Anfri 934 4 16

More

Ali liqu part moi pari and

will

More Examples to illustrate this Rule are thefe following:

C: 1. 1. 1. 1. 12.	C.	Pener
	1. 3528 302	*
Answ.	3830	8 &
C. 1. 1.	C.	5
1	1. 649 38	77
Anfr	. 690	30

X. Any number of pence under iz is either an Aliquot part of a shilling, or elfe compos of A. liquot parts thereof; fo 3 pence is an A quot part, to wit, of a shilling. Likewise 4 is 12; moreover 5 pence are composed of 2 A more parts, to wit, of 3 pence which is of a failing, and of 2 pence which is of a failing, all which will readily appear by the following Table.

fout) may be reduced to pound by the

¢

duction, which ramber or littling

Pence	Aliquot parts of a shilling.		
	304	(or -	of -)
I.	1.	1	1
2	3528	8 I	
2 3.	1	6	
3 8.	3830	Tinfur.	
4	5	1. :.	
5	. 129	4.65	***
6	1.		
7	149 -	+++	
8	-	+ + 1	
9:	690	the transfer	
12 12 15	pour son	photos pado	: Any nue

S pence are composed of XI. When the given price of i, or an Integer is an Aliquot part of a shilling , divide the number of Integers whose value is required by the denominator of fuch aliquot part, fo will the quotient be the number of shillings which answer the ber of question, which number of shillings (when there is oceasion) may be reduced to pounds by the brief nthe

of a failling. Likewise a

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way of dividing by 20: so if it be required to know what 2686 ounces at 4 pence the ounce will amount unto; the answer will be found 44 l. 15. 4d. for since 4d. is an aliquot part, to wit, -of a shilling, I divide 2686 by 3. so will the quotient be 895-4. or 895. 4d. which shillings being divided by 20, give 44 l. 15. 4d. for the answer to the question, as you see by the following operation.

More Examples of this Rule are there following :

el doide de gardo de gardo : 29 -sup sar la servicia sal. . . 759 sus plus rial servicia de selogica de se

Answ. 18 . 19 2. 6

yard d. yards 1 ... 1 ... 204

Answ. 17 Stillings.

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ad llew es offer sid not low in the s Ligo Dag 1 ... 11 45. 540 180 180

> ... 135 20) 49 5 s. d. 24 ... 15 : 0

XIII. When the given price of an Integer conils of hillings and pence, first multiply the number of Integers whose value is required by the faid gien number of shillings, and subscribe the product ti. is shillings, then divide the said number of Inte-ers, by the several denominators which are corre-or pondent to the aliquot parts contained in the giis en number of pence, and subscribe the quotient or ue motients underneath the aforesaid product of are hillings, all which being added together give the umber of shillings which answers the question : so f it be demanded what 347 yards of cloth will

oft at the rate of s. 10 d. the yard, yard s. d. yards he answer will be ound 135 1.18 s. 2 d. or first 347 being nultiplied by 7, (the 429 shillings, then ividing 347 by 2 nd 3 feverally, (beruse 10 d. is com-

1 . . 7 : 10 . . 347 7 × 347 = | 2429 : iven number of 2) 347(... 173 : 6 illings) produceth 3) 347(... 115 : 8 3) 347(...

20) 271 |8: 2 Anfw. 135:18 : 2

pos'd

pos'd of - and - of a shilling) the quotients will be answ 173 - and 115 =, that is 173 s.6 d. and 115 s.8 d. Laft. of a ly, the fum of all is 2718 s. 2 d.or 135 1.18 s. 2 d,

	1 17 : 9 540
	17 × 540= 1 \$3780
	17 × 540 = \$3780 2) 540(\$3780 270 135
g 1	4) 540(1 135
ц оп. 1	20) 958 5
101, 12	Answ. 479:5:0
	y. s. d. y. 114:6313
	s. d.
	$14 \times 313 = \begin{cases} 1252 \\ 313 \end{cases}$

MIV. When the price of an Integer confifts of fifts of thillings and pence, and that fuch thillings and pour pence joyntly considered do make an aliquot pan of a pound, it will oftentimes be a briefer way that that in the last Rule, to divide the number of Inte \$170 gers whose value is required, by the denominato of fuch aliquot part, fo will the quotient give the anfwei

will will aliqu 767

pot n th

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be infwer to the question in pounds and known parts aft. of a pound. Thus if it be demanded what 767. yards will cost at the rate of 6 s 8 d. the yard, the answer will be found 255 l. 13 s.4 d. For fince 6 s.8 d.is an aliquot part, to wit . of a pound, I divide J. 767 by 3, fo there ari-1 ...6 : 8 .. 767

feth in the quotient 2552, or 255 1.:13 s. Ad. which is the an-

3) 767 (255 .. 13

wer of the question. Note that the Aliquot parts of pound convenient for this Rule are these exprest n the following Table.

Sb. d.	Aliquot parts of a pound.
6 8	1 3
3 4	-
2 6	<u>*</u>
18	112
I 4	15
1 3	16

XV. When the given price of 1 or an Integer confifts of pounds, shillings and pence, reduce the said pounds and shillings all into shillings, then pro-ceed according to the 13 Rule of this Chapter: So site unto 2001 l. 4s. 5 d. for having reduced 3 l. 17s. thento 77 s. I multiply 517 by 77, and write down the particular V 3

Appendix,

particular products; then for the 5 pence which is compos'd of the aliquot parts and of a shilling, I take and of 517, and subscribe the quotients orderly underneath the aforesaid products. Lastly, adding all together the sum is 400245, 5 d. or 2001 l. 43.5 d. for the answer of the question.

C. l. s. d. C.
1 . . . 3:17:5.. 517
77 × 517 =
$$\begin{cases} 3619 \\ 3619 \end{cases}$$

4) 517 (. 129:3 d.
6) 517 (. 86:2
20)4002|4:5
1. s. d.
Answ. 2001:4:5

More Examples of this Rule are thefe following.

C. l. s. d. C.

1... 5: 13: 8 ... 108

$$\begin{array}{c}
324 \\
108. \\
30
\end{array}$$
20)1227|6
l. s. d.

Answ. 613: 16: 0

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C. l. s. d. C.

1 ... 2: 10:6 ... 84

50 x 84=4200

42

20) 424|2(212:2:0

C. l. s. d. C

1 ... 1: 12: 4½ ... 306

32 x:306= | 612
918
3) 306(... | 6:4½

48) 306(... | 6:4½

20) 990 0: 4¹/₂
1. 5. d.
An(w. 495: 0: 4¹/₂

Note, when the given price of an Integer confifts of certain pence together with \$\delta\$ d. or \$\frac{2}{4}\$ d. it will be convenient to take due aliquot part; of the number of Integers propounded for all the given price of an Integer except \$1\$ d. and the faid \$\frac{1}{2}\$ d. or \$\frac{3}{4}\$ d, then for that penny, and \$\frac{1}{2}\$ d. take \$\frac{1}{6}\$ of the faid Integers propounded, and if there be yet a farthing, take \$\frac{1}{6}\$ of the faid quotient which ariseth by taking \$\frac{1}{6}\$; both which quotients give the value in shillings correspondent to \$1\frac{3}{4}\$ d, this will be evident by the sollowing \$Examples\$.

V 4

yard

	54	s. d.
3	326(81 6
: 8)	326(40 9
6)	40()	68
- 6/	81	0 1:

3
$$\overline{x}$$
 720 = | 2160
4) 720(... | 180
6) 720(... | 120
8) 720(... | 90
20) 255 | 0 (127 : 10 : 0 the circ

and the price of many Integers of the fame name quot together with or or of an Integer is required, the value of those Integers may be first found by some of the precedent Rules, and then for the price of tof an Integer, take tof the given price of

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of an Integer; likewise for 1 of an Integer, take 1 of the said given price, also for 3 of an Integer take the composed of 1 and 1 of the said given price: So if it be demanded what 34 C. 3 qu. (to wit, 34 hundred weight, and 2 of an hundred weight) of Sugar will cost at 41, 16 s. 3 d. per C. the Answer will be found 167 1. 4 s. 8 1 d. as by the subsequent operation is manifest.

d. An example of Averdupois greater weight, where the quantity whose price is sought considered ire hundred weights, quarters of an hundred, and en, of some number of pounds, which is not an alience quot part of 28 or 4 C.

f an Inte	15 10 - ha	1931.19	218:	3	24
C. 3 qu.	2) 218	= 5	1090 218 18 109	: 50i 34 bu	far.
T 6	8) 218 of 27 5.3 d.	C	16747	: 6	2 3
he quotient trising for	} - C.			: 10 :	
	316.	20) 25	3	: 1	: o †

The example last mentioned being (of those questions which ordinarily happen in trade) one of the hardest to be resolved by the Rule of Practice. I shall touch upon the aforegoing operation, where you may observe the price of 218 C. 3 qu. to be found after the manner of former Examples ; then for 14 lb. part of the 24 lb. in the question, I take of the price of ! C. Likewise for 7 16. I take balf the pence price of 14 16. and fo there yet remains 3 16. whose gain, price is found by taking -3- of the price of 7 lb. viz. the price of 7 lb.being very near 7 s.2 1 d.or 86 1 d. I multiply 86 by 3, and divide the quotient by 7, fo there ariseth 37 d. or 3 s. 1 d. very near; lastly, shilling all being added together, the fum is found to and 8 ti

and i a far low. Spect albei mann the n is inc

> XV of di pence ers v work uire er C.

pences which a which I under t

be

be very near 25322 so 3 -d. lor 1266 lin Agian a

Note that a quarter of a farthing (or - of abe ny) is the fmallest money expres in the example and where any thing arifeth lefs then a quarter of a farthing it is omitted, but it is tappoled to for low this note +, for which furplufages fome respect ought to be had in adding all together : now albeit, in refolving questions after this practical manner there will be some error, yet the loss for the most part will be less then a farthing, which is inconsiderable.

XVII. When the price of 1 or an Integer confifts of divers denominations, as pounds, hillings, pence; and the price of a certain number of Integers which exceeds not a fingle figure is required, work as in the following Example, viz. If it be required to find what 8 C. will coll at 3.1. 13 s. 7 1 d. per C. it is evident that 8 C. must cost 8 times 3 1.

> C. 1. s. d. C. 1 . . 3 : 13 : $7\frac{1}{2}$. 8 Mr. When the och a cory

Answ. 29:9:0

13 5.7 - d. therefore I multiply by 8, faying, 8 half pence make 4 pence, which I referve in mind again, 8 times 7 pence make 4 s. 8 d. (to wit, & fix pences make 4 s. and there are 8 pence belides) to which adding 4 pence in mind, there will arise 3 .. which I referve in mind, and fubscribe a cypher under the place of pence; again, I fay 8 times 13 thillings make 5 1. 4 s. (to wir, 8 Angels make 41. and 8 times 3 s. make 1 l. 4 s.) to which adding 5 s.

fcribe 9 s. (the excess above the pounds) under the shillings, and keep 5 lin mind; lastly, I say 8 times 3 pounds make 24 pounds, which with 5 pounds in mind make 29 pounds; so that the total product or answer of the question is found to be 29 l.

More Examples of this kind are thefe.

C. l. s. d. C.

1 . 17: 15:
$$5\frac{1}{4}$$
...7

7

Answ. 124: 8: $6\frac{3}{4}$...8

Answ. 149: 00: 6

XVIII. When the price of 1 lb. weight is known, and the price or value of 1 C. (to wit 112 lb.) is required, the answer may sometimes be given more speedily then by any of the former Rules, by this Rule which follows, viz. Find the number of farthings contained in the given price of 1 lb. weight, then take twice that number of shillings, and once that number of groats, and having added them together the sum will give the value of 1 C. to wit 112 lb. weight: So if it be demanded what 1 C. or 112 lb. weight of Cheese will cost at the rate of 3 - pence the poundweight, the answer will be 1 l. 195.44

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For according to the faid Rule, the number of fare things contained in 3 d. (the sale lahil price of 1 pound weight) is 13 y therefore the double of 13 shil-Therefore the fum (which is) the price of 1 C. or 112 16 11 1 : 10: 4 weight) is . . .

The reason of this Rule is evident, for if 1 16. weight coft 13 farthings, then 112.16. must necessa. rily cost 112 times 13 farthings, or (which is the fame) 13 times 112 farthings; but 13 times 112 farthings are equal to twice thirteen shillings together with once thirteen groats, because 112 far? things are composed of twice 48 farthings (or two shillings) and of 16 farthings (or one groat) wherefore the truth of the faid Rule is evident.

Another Example, when Sugar is at 5 d. the pound weight, what is the value of 1 C. (or 112 16. weight?) Anfw. 21. II s. 4 d. For in 5 d. are

contained: 22 farthings therefore 1. the double of 22 fbillings is . . 2 : 4 : 10 22 Groats, make . . 0:7:4

Which added together give ? the price of 1 C. or 112 16. to \$ 2 : 11 :

wit . . XIX. When the gain of (or allowance for) 100 integers confift of some number of pounds not exceeding 10, the gain of as many like integers and known parts of an integer as one will, may be found very briefly by the follow-

Compressions wayes of computing interest . and Falters allow ances.

ing method, viz. If 100 /, gain 3 /. what is the gain

First I multiply 2464)185. 10 diby 3 (the fecond termi) after the manner delivered in the 17 Rule of this Chapter, and white down the product which is 740 0 16 0 6.d. Then I divide the faid product by 100 (the first term in this Rule of Three) in this manner, viz. Idivide 740 pounds by 100, which is performed by curting off towards the right hand

The realion of this Rule is evidenc, Arr. if 1 &. weight coft is brtilingi :toteli./6. modineceffa. rily coff ita riges is lurchings, or (which is the iame to eines no farebings, but ig eines 112 farthings are donal rorwios thirteen thillings together with once thirteen ogoats, because no far? things ale composed of wice 48 farthings (or two hillings) and of it furbilles. (or one groat) where fore the cruth of the frild Rule is evident. Andther Example, when Sugar is at 7 d. the pound weight, what is the volue (80 C. (br 112 B. weight?) dofor 21 Its, 4d For in 5-dare

the two last places of 740, so the quetient gives 7 pounds, and there will be a remeinder of 40 pounde, which 40 pounds I reduce into hillings, for there will arise 800 , to which adding the 16 m which fland in the place of shillings, the fum will be 816 shillings, these are also to be divided by 109. (by cutting aff emo places as before) fo the quotient will give & flillings, and there will remain 16 Millings, which being reduced to pence, and unto them 6 pencerbeing added, (to wit the 6 pence which tands in the place of pence, there will arife 198 pence; these also are to be divided by 100, (by cutting off two places to the right hand as before) fo

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fo the quotient gives 1 peny, and there will remain 98 pence; fo the exact quotient or Answer of the question is found to be 7 l. 8 s. 1 28 d.

More Examples of this Rule are thefe following!

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After the same manner may this following question and such like be resolved, viz. When 100 Ells of Linnen cloth cost 30 L 18 1.9 d. what is the price of 1 Ell? Angles 61.2 des farth.

Ells

XX. When the given gain of (or allowance for) 100 integers confifts of fome number of pounds not exceeding 10, together with fome Aliquot part or parts of a pound, the operation will be little different from the last mentioned Examples, as may appear by the refolution of the subsequent question, viz. What must be allowed for 2156 1. 13 s. 4 d. at the rate of 6 l. 15 s. for 100 1? Anfw. 145 1. 11 s. 6 d. thus found ; firft I multiply the faid 21561. 13 s. 4d. by 6 (the number of pounds in the given allowance 61. 15 s.) after the manner of the last Examples, and fubicribe the product which is 12940 !. underneath the line as you fee, then since 15 s. are equal to 1/1. together with 1/1. I take - of 21561. 13 s.4 d. which is 10781.6 s.8 d. likewife - of the faid 2156 1. 13 s. 4 d. to wit, 539 1. 3 s. 4 d. and having subscribed these quotients underneath the product first found, and added them ither all together, I find 14557 1. 10 s. od. for the total lience product, with which I proceed as in the former land the Examples, and so at length the Answer is found to liven q be 145 l. 11 s. 6 d. View diligently the operation. ame va

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100 . 63 .. 2156: 13 . 4 12940:00 : 0 1078:06:8 539:03:4 1. 145 57:10 : 0 20 1150 12 600

CHAP. III.

Concerning Exchanges of Coins, Weights, and Measures.

He rate or proportion between Coins Weights,&c. of different kinds being known. m either from some good Author, or rather by expeal rience; it will not be difficult, to fuch as underer land the Rule of Three, to know how to exchange a to liven quantity of one kind, for a quantity of the n. ame value in another kind. But fince in fome cases, the common way of working may be much contracted.

tracted, I shall endeavour to shew the most com-

pendious wayes to perform this bulinels.

II. In exchanging of things of different kinds, (whether they be Coins or Weights, &c.) when two things of different kinds are compared together, the question may be resolved by one single Rule of Three, as will be evident by the subsequent Examples, viz.

Quest. 1. How many Riders at 21 s. 2 d feerling the piece, ought to be received for 25 1 1.6 s.4 1 d. of sterling money ? Answer, 237 Riders. For the first and third terms in the Rule of Three, which ariseth from this question, being converted into half

pence, the proportion will be this,

509 . 1 :: 120633 . 237

Quest. 2. If 100 Ells of Antwerp make 75 yards of London, how many yards of London measure will 27 Ells of Antwerp make ? Answer 20- yards.

100 . 75 :: 27 . 20-

III. When more than two different Coins, Weights, Measures,&c.are compared together, viz. when one kind of Coin is compared with a fecond of another kind; that fecond with a third; the third with a fourth; the fourth with a fifth, &c. two different cafes are ordinarily raised from such comparison, viz.

1. How many pieces of the first Coin are equal in value to a given number of It may be

pieces of the last coin : or required toe know,

2. How many pieces of the last Coin are equal in value to a given number of pieces unde (of the first kind of coin.

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An Example of the first case.

If 35 ells of Vienna make 24 ells at Lyons; 3 ells of Lyons 5 ells of Antwerp; and 100 ells of Antwerp 125 ells at Frankfort; how many ells of Vienna are equal unto 50 ells at Frankfort? Answer, 35 ells of Vienna.

For the more easie understanding of the resolution of this question and others of like nature. Let a represent an ell at Vienna; b an ell at Lyons; c an ell at Antmerp, and d an ell at Frankfort; then may the given terms in the question be stated in the sollowing order.

Suppositions
$$\begin{cases} 35 & a = 24 & b \\ 3 & b = 5 & c \\ 100 & c = 125 & d \end{cases}$$
The question 50 d = ? A

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Which order of placing the faid given numbers (or terms) being observed; it appears that if 35 a be accounted to stand in the first place; 24 b in the second; 3 b in the third; 5 c in the ferms; 100 c in the fifth, &c. then all the terms which stand in odd places, to wit, in the fifth, third, fifth, and seventh places, will necessarily fall under the first row or column on the left hand, and all the terms which stand in even places, to wit, in the second, fourth, and sixth places, will fall under the latter column.

in are These things premised, all questions which fall bieces under Case 1. before mentioned may be resolved by this Rule, viz.

X 2

Rule I.

Multiply all the given terms which stand in odd places (to wit, in the first column) according to the rule of continual multiplication, and referve the last product for a dividend: Again, multiply continually all the terms which stand in even places, so shall the product be a divisor, and the quotient arising from the said Dividend and Divisor

shall be the answer of the question.

So in the last mentioned question, if all the numbers in the first column, to wit 35, 3, 100, and 50 be multiplied continually, the product will be 525000 for a Dividend; also if all the numbers in the latter column, viz. 24,5 and 125 be multiplied continually, the last product will be 15000 for a Divisor, and the quotient arising from the said Dividend and Divisor will be 35, which is the number of ells of Vienna required.

35	
3	125
50	

\$25000 : 15000) 525000 (35

The reason of the said Rule I. will be manisest by solving the question propounded by three single Rules of three, thus,

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II.
$$\frac{50.35 \times 3}{1}$$
 4: $\frac{100}{1}$ c. $\frac{35 \times 3 \times 100}{5 \times 24}$ 4 (= 125 d.

III.
$$\frac{125}{1} d$$
: $\frac{35 \times 3 \times 100}{5 \times 24} a$: $\frac{50}{1} \frac{35 \times 3 \times 100 \times 50}{125 \times 5 \times 24} a$.

which fourth proportional last found, to wit, $35 \times 3 \times 100 \times 50$ being well viewed and compared

with the before mentioned order of placing the terms given in the question gives the very Rule I. before express in words.

An Example of the latter of the two Cases before mentioned.

If 10 lb. of Averdapois weight at London be equal to 9 lb. of Amsterdam; 45 lb. at Amsterdam, 49 lb. at Bruges; and 98 lb. at Bruges equal to 116 lb. at Dantzick; how many lb. of Dantzick are equal to 112 lb. of Averdapois weight at London? Answer, 129. 92 lb. of Dantzick.

That the operation may be the more clear, let a represent one pound of Averdapois weight; b one lb. of Amsterdam; c one lb. of Bruges, and d one lb. of Dantzick; then let the question be stated after

the order in the first Cafe, viz.

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I.

II.

III

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Suppositions
$$\begin{cases} 10 & a = 9b \\ 45 & b = 49c \\ 98c = 116d \\ The question 112a = ?d \end{cases}$$

These things premised, all questions which fall under Case 2. before mentioned may be solved by this Rule, viz.

Rule II.

Multiply all the given terms which stand in even places, (to wit in the latter column) and the last odd term in the first column according to the rule of continual multiplication, and reserve the last product for a Dividend; again, multiply continually the rest of the terms which stand in odd places (to wit in the first column) for a Divisor, so shall the quotient arising be the answer of the question.

Or in this latter case if you place the last of the given terms in the same column with the even terms, the rule for solving questions, which fall under the latter case will be this which solloweth,

Multiply continually all the numbers in the latter column for a Dividend; also multiply continually all the numbers in the first column for a Divisor, so shall the quotient arising be the answer of the question. Thus the answer of the last mentioned question will be found 129.92, to wit, 129 \frac{92}{100} lb. of Dantzick, as is evident by the subsequent operation.

Chap.111.

Weights and Méasures.

315

9 45 45 49 98 116 112

44100) 5729472 (129.92

The reason of the said Rule II. will be manifest by solving the question propounded, by three single Rules of three, thus,

I. 9 b. 10 a: : 45 b.
$$\frac{45 \times 10}{9}$$
 a. (= 49 c.

II.
$$\frac{49}{1}c.\frac{45\times10}{9}a::\frac{98}{1}c.\frac{45\times10\times98}{49\times9}a$$
 (= 1164.

III.
$$\frac{45 \times 10 \times 98}{49 \times 9}$$
 a. $\frac{116}{1}$ d.: $\frac{112}{1}$ d. $\frac{49 \times 9 \times 116 \times 112}{45 \times 10 \times 98}$ d.

Which fourth proportional last found, to wit, 49 x 9 x 116 x 112 being well viewed and compa-

red with the before mentioned order of placing the terms given in the question discovers the very

Rule II. before exprest in words.

Note, when the same numbers happen to be Multiplicators in the Dividend, and also in the Divisor, such Multiplicators may be cancelled in both, and thereby much labour will oftentimes be spared.

X 4

Such

ating pro-

Such which have much practice in calculating Exchanges, and do exactly know the rate or proportion between two different weights or meafures or coins, which they would compare together, may by the Rule of Three frame Tables of proportions for the more speedy reducing of a given quantity of one kind of weight, measure, &c. into a quantity of the same value in another kind of weight, &c. In the expressing of which proportions it will be very convenient that the first number or Antecedent of each proportion be made I or unity, and the second term or consequent a Decimal, or else al mixt number whose Fractional part is a Decimal, for then the Coin, Weight, &c. of the one place, (whose term is 1) may be reduced into that of the other place, by help of those Tables and of Multiplication of Decimals without sensible error: For Example, It hath been observed by some ingenious Merchants that 100 lb. of Averdupois weight at London, are equal unto 80 th, in Paris by the Kings beam, and confequenty 1 th. Averdupois is equal to 100 lb. or .89 lb. at Paris, (for if 100 give 89, then I will give . 89) therefore any number of pounds A. verdupois being multiplied by . 89 (with respect unto Multiplication of Decimals, explained in the 26 Chapter of the preceding Book) will produce pounds of Paris: Again, if 80 lb. of Paris be equal to 100 lb. Averdupois, then 1 lb. of Paris will be near equal to 1.1235 lb. of Averdupois; therefore any number of pounds of Paris being multiplied by 3.1235 will produce pounds Averdupois very near.

Upon this ground I have collected the proportions in the following Tables, wherein I would not have any to confide further than they shall know

them

Chap.III. Weights and Measures.

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them to be agreeable to truth, for I have only derived them from those delivered by Mr. Lemes Reberts Merchant, in his Map of Commerce printed at Landon; Anno 1638. and do herein only aim at the instruction of ingenious Merchants and Rastors in the briefest wayes of calculating their exchanges, the rate or proportion being truly known; in which practice, Decimal Arithmetick (which hath no enemy but the Ignorant) will be very serviceable.

A Table for the Reduction of Averdupois weight at London, to the weights of divers forreign Cities and remarkable places.

() () () () () () () () () ()		lb.
	Answerp,	.9615
	Amsterdam,	.9
	Abbeville,	.91
	Ancona,	1 .282
	Avignon,	I .12
V 0 -	Burdeaux,	.91
	Burgoyne,	.91
One pound	Bollonia,	1 .25
of Averdu		.98
pois weight	Callabria.	1 .3698
at London ,	Callais.	1 .07
makes at	Conftan- ?	.8474
	timople,	Loder ;
-	Deepe,	.91
	Danfick,	1 .16
	Ferrara.	I .3333
	Florence,	1 .282
	Flanders 2	
	in general	1 .06
	Geneva,	.9345

Genoa,

```
16.
                             .4084 Suttle
                          1
             Genoa,
                             .4285 grofs,
                          1
             Hamburg,
                             .92
              Holland,
                             .95
              Lixborn.
                             .881
                           1 .07 common weight.
                              .98 filk meight.
             Lyons,
                              .9 customers weight.
             Leghorn,
                           I .3333
             Millan.
                           1 .4285
             Mirando'a.
                           1 .3333
             Norimberg,
                              .88
             Naples,
                           1 .4084
One pound
of Averdu-
             Paris,
                             .89
pois weight ? Prague,
                              .83
                           ı .3888
at London ,
             Placentia.
makes at
             Rotchel,
                           1 .12
             Rome,
                           1 .27
                              .875 by vicont.
             Ronan, }
                              .9017 commonweight.
             Sivil,
                           80. I
             Tholonsa,
                           1 .12
             Turin,
                           1 .2195
                           1 .5625 Suttle.
             Venetia, }
                             .9433 grofs.
            Vienna.
                             .813
```

Of Eschanges, &c. Appendix. The use of the preceding Table will be manifest by the subsequent example, viz.

How much weight at Danfick do 320 lb. Averdupois make? Answer, 371.2th. Seek in the precedent Table for Dansick, and right against it you shall find 1 . 16 which thews that 1 1. Averdupois is equal to 1. 16 lb. at Danfick, therefore multiply 320 by 1. 16, so will the product be 371. 2 lb. of Danfick, as by the Operation is manifest.

> Aver. Danf. Aver. Danf. 1 : 1.16 :: 320 : 371.2 1.16

820

1920 320

320

371 20

A

A Table for the Reduction of the weights of divers forreign Cities and remarkable places to Averdupois weight at London.

Antwerp Amfterdam Abbeville Ancena Avignon Burdeaux Burgoyne Bellonia Bridges Callabria Callais Deepe Danfick Ferrara Rlorence Planders in 7 general Geneva Genoal grofs,	makes at London of Averdupois Weight	lb. 1.04 1.1111 1.0989 .78 .8928 1.0989 .8 1.0204 .73 .9345 1.0989 .862 .75 .78 .9433 1.07 .71 .7
---	--------------------------------------	---

7

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Ü.,		TIb.
1.	Hamburg	1 .0865
3 :	Holland	1 .0526
	Lixborne	1.135
	Commonweight.	.9345
	Lyons lilk weight.	1.0204
	Leghern	
_	Millain	5 i .75
One pound weight in	Mirandola	₹ .7
Ä	Norimberg	₹ .75
	Ner imotery	1.1363
8	Naples	.71
ğ	Paris	₹ 11.1235
3	Prague	1 .2048
۵.	Placentia	.72
=	Roschel	8928
0	Rome	3 .7874
	by Vicont,	1.1428
	Rouan	5
	commonweight.	1.1089
	Sivill	E .9259
	Tholonsa	.8928
	Turin	.82
	Cfuttle,	.64
	Venetia2	
	· Zgros,	1.06
	Vienna	1.23

The

Chap.III. Weights and Measures.

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The use of the last mentioned Table, will be manifest by this example, viz.

In 224 lb.weight at Hamburg, how many pounds
Averdupous?

Answ. 243.376 lb.

Seek in the Table for Humburg, and right against it you will find 1.0865, which sheweth that 1 th.of Humburg makes 1.0865 lb. Averdapois; therefore if 1.0865 be multiplied by 224 the product will be pounds Averdapois.

224

43460 21730 21730

243 3760

One ell at London, makes at

A Table for the Reduttion of English Ells to the Measures of divers forreign Cities, and remarkable places.

Amsterdam	1.6949	
Antwerp	1.6666	
Bridges	1.64	
Arras	1.65	
Norimberg	1.74	
Colen	2.08	-11
Liste	1.66	Ells.
Mastrich	1.57	
Frankford	2.0866	
Danfick	1.3833	
Vienna	1.45	
Paris	.95	
	1.03	
Rouan	1.0166	Aulnes.
Lions	1.57	
Callais		
Venice finne	1.96	1
Lucques	2.	
Florence	2.04	Braces.
Millan	2.3	1 1
Leghorn	2.	
Madera	1.0328	
Isles \$, 5

Sivill

at London makes at	Sivil Lubone Caftilia Andoluzia	1.35 1. 1.3875 1.3625	3	Vares
London	Granado Genoa	1.3625)	Palma
One Ell at	Saragofa Rome Barfelona Valentia	.55 .56 .7125 1.2125	}	Canes

The use of the aforesaid Table will be manifest

by the subsequent example, viz.

In 325 ells of London, how many ells at Antwerp ? Answ. 541,645 ells : Seek in the Table for Anwhich being multiplied by 325 produceth 541.645, ells of Antwerp, as by the operation is manifest.

> 1 ... 1.6666 3:1 325 325 83330 33332 49998 541 6450

A Table for the Reduction of the Meafures of divers forreign Cities, and remarkable places to English Ells.

lat	[Amsterdam]		.59	1
Ē	Antwerp		.6	
One	Bridges	2	.6097	
0	Arras	nde	.606	U
fishing.	Norimberg	S.	5747	· L
	Colen Liste	, a	.4807	1
1 grown	Mastrich	S	.6024	
وويداء	Frankford	Teo.	6369	1
ರಕ್ಷಕ	Danfick	5	4792	150
VE	Vienna		.6896	1
	S Paris	Trada.	1.0526	
One	2 Ronan		.9708	í
0	Lions ?		.9836	
	(Callais		.6369	
Brace at	1 . 1:		1 .5555	1
30	Venice Silk:		.5102	1
2	(Lucques		1 .5	1
	(Florence	5	.4901	1
One) Millan		.4347	
	Leghorn		1.5	
	(Madera Isles		.9681	

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1.4	100000000000000000000000000000000000000
	liar quantity ain the Ming
Sivill W	agranding by 7407 stantor
Lisbone om to	but one and the fame kind
Illinia no L Caltillangion	the nisonlay so 7207 bas
- Andoluzia an	caul Otten inredant pli
Will Congadovin	transmit areas
One Palm ve Case	200 aufer gra 2079
Tone Parin actions	in il 1848 in this man
belogica) Rome it buit	
	11.0 2 60 14 Care and a cal
TO Q (Valentia	Bide X odi bi .8247 Billia
Mediares voti verient	cerning Coins, Preights all
0	and modern.
1	, , , , , , , , , , , , , , , , , , , ,

The use of the said Table will be manifest by the subsequent example, viz.

In 730 Aulnes at Lions, how many ells at Lon-

don ?

Answ. 718.028. Seek in the Table for Lions, and right against it you shall find ,9836 which being multiplied by 730 produceth 718.028 ells of London, as by the operation is manifest.

vil

Exchanges of Goins, &c. Appendix.

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Note, that one and the same kind of Weight or Measure, doth seldom or never alter from its peculiar quantity, in the Kingdom or Commonwealth, where such weight or measure was first established; but one and the same kind of money doth often rise and fall in its value in forreign parts: for which cause I have spared the pains of calculating Decimal Tables for Coins, yet to give some light to such as read modern relations, and want experimental knowledge in this matter, I shall here insert a Table, in the same estate as I find it in the aforesaid Map of Commerce, and refer the Reader, for further satisfaction, to the Tables in Riders Distintary, concerning Coins, Weights and Measures, both ancient and modern.

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Of

Of Exchanges of London, with divers forreign Cities.

Pence

	Placentia fterl.	04	for	1	Crown
	Lyons	64	for	1	Crown
n.,	Rome	66	for	1	Ducat
	Genoa	65	for	. 1	Crown
•	Millan	64.3	for		Crown
	Venice	50	for		Ducas
-9	Florence		for		Ducaton .
with	Naples	53 -	for	I	Ducat
exchange	Lecchie in 7	50	for	1	Ducat
-9	Barri	SI	for	1	Ducat
Z	Palermo	57:	for	1	Ducat
-	Mesina	56 <u>-</u>	for		Ducat
London doth	Antwerp L. 1 A	erl.	for	3	4. Shill.
Z.	La Coleni.	57=	for	1.7	2 Iflem.
m	Valentia	59	for	1	Ducab
Y	Saragosa	64	for	1	Ducat
	Barcelona	53	for	1	Ducad
	Lixborn	_	for	1	Ducat
	Bollenia	53 ±	-	1	Ducaton
	Bergamo	52	for	I	Ducaton
	Frankfort	59:	for	1	Florin
	Genoa	83	for	İ	

Y 3

London

Questions of Tare, Appendix

3888

London exchangeth in the denomination of pena sterling with all other Countries, Antwerp an those peighbouring Countries of Flanders an Holland excepted, with which it exchangeth by th entire pound of 20 shillings English (or ferling.)

CHAP. IV.

Practical Qualtions about various things wir Tare, Gret, Lofs, Gain, Barter, F. Storfhip; and Measuring of Tapestry.

Of abatements and alternances in Traffick

Nithe trade of Merchandize ther dre in ufe various allowances, and abatements, known by the names o Tare, Tret, &c. concerning which

shall give a few examples, whereby the practical Anithmetician will eafily fee, tha there is more difficulty in the name than in the thing; for the rate, or proportion agreed upon in any allowance or abatement, (be it called by what name foever) being once known, the Arith metical work will quickly be dispatche by the Rul of Three, or elfe by that and fome of the former rules mixtly used, as will partly appear by the following questions

Grofs weight is composed of the meat weight of the commodity, marked A.B.C.D. and alfo of the Tare, to wit, the Chest Bag, But, Ge which grofs weight of containerb the commodity.

Queft. r. A Factor buy. eth 4 Chefts of Sugar The each

Cheft in Averdupois greater weight is as followeth, f pence rp and s and by the

things; ter, Fa-

ze there
ices, and
names of
which I
whereby
ee, that
n in the
d upon,
alled by
the Ariththe Rule
the former
y the fol-

for buyof Sugar
of each
of each
olis greaolloweth,
A.

y	C 4. 16.11	
A.	11 1 19	
B.]	10 3 20	
C.	11 2 13	
D. 1	10 1 17	
-		

The total gross weight 44 ... I ... 13

Now supposing the Tare or weight of each Chest, when it is empty, to be 37th, the question is what neat weight of Sugar will remain, when the total Tare is subtracted? Answ. 43 C. 09. 5th.

from 44. 1 . 13 the total grofs weight.

Subtr. 1 . 1 . 08 the total Tare.

Rem. 43. 0 . 05 the neat weight of fugar.

Quest. 2. If from 990 C. 3 qu.21 lb. gross weight, Tare is to be subtracted after the rate of 14 lb. per C.(or 112 lb.) of gross weight, how many C. neat will remain? Answ. 867 C. o qu. 7-18 lb.

I. The gross weight being converted into pounds by the 6th. rule of the 7th. Chapter of the proceeding Book, will give 110985 16.

II. Then by the Rule of Three.

112 . 14 :: 110985 : 13873 8 or 8 . 1 :: 110985 . 13873 8

Subtr. 13873 the total Tare.

C. qu. Ib.

Rest neat 97111 = 867 .. 0 .. 72

Note, when the number of lb. to be abated per of Tare, is an aliquet part of 112, as in the last mentioned example, where 14 = 1/8 of 112, the operation may be thus:

C. C. C. q. lb. C. q. l 1 . $\frac{1}{8}$:: 990:3:21. (123:3:13

 $\begin{array}{c}
990 \text{ c.} = 123 : 3 : 00 \\
3 \text{ q} = 00 : 0 : 10\frac{4}{8} \\
21 \text{ lb.} = 00 : 0 : 02\frac{5}{8}
\end{array}$

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Total Tare 123:3: 138
Reft neat 867:0:073

2 Left. 3. Suppose at some City, there is the second of th

question is, how many th. weight ought he to re-

ceive in all? Answ. 1222 lb. weight. 100 . 104:: 1175 . 1222

This

12 Acres

pendix.

Ĭb. 7₹

ed per C. ast menoperati-

l. lb.

, there is nerchanin as an y 100 lb. tion for Merchant and is to ate, the

This

This kind of allowance is commonly called Tree. Queft. 4. Suppose a Merchant hath 1222 lb, weight of a certain commodity, part whereof he bought at a certain rate per lb. and the rest was allowed to him or cast in as an overplus, after the rate of 4 lb. weight for every 100 lb. weight which he bought; the question is, to know how many pounds near weight he bought? Answ. 1175 lb. weight.

104 . 100 :: 1222 . 1175

This question is the converse of the former, and sheweth how to make abatement for Tree.

Quest. 5. If from 55 C. 1 qu. of gross weight, Twe is to be subtracted after the rate of 16 lb. per C. and from the remainder Tret is to be abated after the rate of 4 lb. per 104 lb. the question is, what the neat weight is worth in money after the rate of 8 l. 8 s. for every C. (or 112 lb?) Answ. 382-1.

I. The gross weight in 1b. is 61881.

11. 112.16:: 6188 . 884

or 7 . 1 :: 6188 . 884 III. 6188—884=5304

111. 6188—884=5304

IV. 104 . 100 :: 5304 . 5100 V. 112 . 82 :: 5100 . 3821

Quest. 6. A Merchant hath bought Linnen cloth at 11 s. per ell, which proving worse then he expected, he is willing to sell it at such a price that he may lose precisely after the rate of 1 \frac{2}{3} l. for every 20 l. that he laid out; the question is to know at what price he ought to sell the ell, that the proportion in the

334 Of Loss, and Gain, Appendit faid loss may be observed? Answ. 10 s. 1 per ell.

I. 20-13=181 II. 20 . 181 : 11 . 10 pence.

Otherwise,

I. 20 . $1\frac{2}{3}$:: 11 . $\frac{\pi}{13}$ II. 11 $-\frac{\pi}{12}$ = $10\frac{\pi}{12}$

2nest. 7. If 100 lb. weight of any commodite cost 30 s. at what price must 1 lb. weight of the commodity be sold to gain after the rate of 10 for every 100 laid out? Answ. 3 24 d.per lb. weight

I. 100 . 110 :: 30 . 33 II. 100 . 33 :: 1 . $\frac{33}{100}$ s. (or $3\frac{24}{25}$ d.)

Quest. 8. A Merchant selleth a parcel of Jewel which cost him 250 l. ready money, for 559 l. pay able at the end of 6 moneths; the question is (his fecurity being supposed to be good) what his gai was worth in ready money upon rebate of interest at the rate of 6 l. for 100 l for an year? Ans. 300 l

559 - 250 = 309 $103 \cdot 100 :: 309 \cdot 300$

Of Barter. Quest. 9. How much Sugar at 8 d.per lb. weight may be bought for 20 C. 0. Tobacco at 3 l.per C.? Answ. 1800 lb.

weight of Sugar.

ob . 20 : sprett to his Factor tid le 1 3 14: 51 :: 60 . 1800

Quest. 10. A. hath 100 pieces of Silks, which are worth but, 3 1. per piece in ready money, yet he barters them with B. at 4 lb. per piece, and at that rate takes their value of B. in Wools at 7 1. 10 s. per C. which are worth but 6 1. per C. in ready money, the question, is to know what quantity of Wools payes for the Silks, and which of the two A. or B. is the gamer, and how much? Anfw. 53 C. of Wools payes for the Silks, and A. gaineth 201. by the barter. , word and bo

7- · I :: 400 · 53-

So it is evident that the true worth of the Wool which B. delivered was 320 1. for which he received only of A. the worth of 300 l. in Silks, and therefore B. lofeth 20 / by the barter.

Queft. 11. A Merchant delivereth to his Factor

6001. upon condition that if the Factor add to it 250 1. of his own money, and bestow his pains in managing the whole stock, he shall then have 2 parts of the total gain. The question is to know what flock the Factors fervice was estimated at? Anfw. 1501,

See brief rules for computing of Factors allowances in the 19, and 20. rules of the Second chapter of this Appendix.

Of Fallor Ship.

I, The Factors part of the gain being -, the Merchant must nocessarily have the remainder, which 15

II. 3 . - :: 600 . 400 III. 400 - 250 = 150

Queft.

at 8 d.per 20 C, of 1800 H.

pendix.

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f Jewels

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of. 300 l.

Queft. 12. A Merchant delivereth to his Factor 320 1. and permitteth him to add to it 64 1. of his own money, to be employed in traffick; and by agreement between them the Factors fervice is eftimated equivalent to a certain stock; which is fueh, that if the total gain be divided proportionably according to those three stocks, the Factor is to receive - of the total gain, in consideration of the faid imaginary flock (being the value of his fervice ;) the question is to know the full part of the gain belonging to each, and what stock the Factors fervice was valued at? Anfw. the Merchant of the gain, and the Factor i, whose service was valued at 96 l. fock,

I.
$$320 † 64 = 384$$
II. $\frac{4}{5} \cdot \frac{1}{5} :: 384 \cdot 96$
III. 64

$$96$$

$$480 \cdot 1 :: \begin{cases} 320 \cdot \frac{2}{3} \\ 160 \cdot \frac{1}{3} \end{cases}$$

Quest. 13. If a piece of Arras hangings, in the form of a long square, hath for its of Measuring length 64 yards Englift, and breadth of Tapestry. 4 yards; how many square ells, or sticks Flemish are contained in that piece, when the length of a Flemish ell is equal to 3 yard English? Answer, 444 square ells or flicks Flemish.

Forasmuch as by supposition, a Flemish ell in length, hath fuch proportion to an English yard in length, as 3 to 4, and consequently the square of the one to the square of the other, as 9 to 16.

Therefore

Therefore in a direct proportion, as 9 is to 16; fo is any given number of square yards English, to a number of square ells Flemish, which will take up equal space with the said square ells English. Also in a direct proportion, as 16 is to 9, so is any given number of square ells Flemish, to a number of square yards English, which will take up an equal space with the said Flemish ells: therefore to resolve the aforesaid question, first find the number of square yards English contained in the said piece of Arras, by multiplying the length and breadth in yards mutually one by the other, then proceed according to the aforesaid proportion; so the work will stand thus,

I. 6 1 × 4 = 25 square yards English.

II. 9 . 16:: 25.44 4 square ells Flemish.

Otherwise,

6 yards English in length, give?

by the Rule of Three in Flemish ells-5

Alfo 4 yards English give in Fle-

Therefore the product of the faid

8 multiplyed by 5 digitary, gives for the fuperficial content as before

Quest. 14. If a piece of Tapestry in the form of a long square be in length 15 - ells Flemish, and in breadth 4 - ells Flemish, how many square yards English are contained in that piece, when 4 ells Flemish in length are equal to 3 yards English? Answ. 37 - square yards English.

I. $15\frac{1}{4} \times 4\frac{1}{3} = 66\frac{1}{12}$. II. $16\frac{1}{3} = 66\frac{1}{12} \cdot 37\frac{11}{64}$

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CHAP. V. mil south in the

Concerning the Interest of Money, and the Construction of Tables to that purpose.

IN resolving questions concerning interest of money, four things are to be well observed, to wit, first, the Principal, or money lent for gain or interest; secondly, the time for which the said Principal is lent; thirdly, the sate of proportion which the Principal bears to the sum of the principal and interest; and sourthly the interest it self: So if 100% be lent upon condition that 106% shall be repaid at the end of a year, the said 100% is called Principal; the time for which the said principal is lent is one year; the proportion which the principal bears to the sum of the principal and interest is such as 100 hath to 106; lastly, the interest it self is 6%.

II. Interest is either Simple or Compound.

111. Simple Interest, is that which ariseth or is computed from the principal only: So if 1001. be lent for two years, the simple interest thereof after the rate of 6 pounds for 100 pounds for 1 year will be 12 pounds, viz. 6 pound due at the first years end, and 6 pounds due at the second years end.

IV. Compound Interest is that which ariseth from the principal, and also from the interest thereof, and therefore it is called interest upon interest: So if 100 pounds be lent and forborn 3 years, and compound interest thereof is to be com-

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puted after the rate of 6 pounds for 100 !. for one year; there will arise besides the simple interest of the principal for 3 years, the interest of 6 pounds (due at the first years end) for 2 years, and the interest of 6 pound (due at the second years end)

for one year following.

V. Rebate or discompt of money is, when a sum of money due at any time to come, is fatisfied by the payment of fo much present money, which if it were put forth at a certain rate of interest for the faid time, would become equal to the fum first due: So if 100 pounds be due at the end of two years, and is to be fatisfied by the payment of prefent money upon rebate, after the rate of 6 pounds per centum, per annum, simple interest, there ought to be fo much ready money paid, which in two years after the faid rate of interest would be augmented unto 100 /. In like manner if the rebate or difcompt were to be made after any rate of compound interest, so much ready money ought to be paid, which at fuch rate of compound interest, for the time agreed on, would become equal to the fum first due. Examples of the manner of computation by rebate may be feen in the tenth and fourteenth Rules of this Chapter.

VI. In the taking of interest, or use money, for

the loan or forbearance of money lent, respect must be had to the rate limited by Act of Parliament, which now restraineth all persons from taking more than 61. for the interest or use of 100%. lent for a year, but what part of 6 1. may be taken for

upon which the Rules for computing Simple interest are grounded.

The foundation

the interest of 100 %. lent for half a year, a quarter

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of a year, a moneth, or any other part of a year, is not exprest in the Act ; In this case therefore we must observe custom and daily practice, so we shall find that 3 1. is usually taken for half a years interest of 100 l. and 30 s. for a quarter of a year, &c. by which practice, this following Analogy, (which is the ground or reason of the common rules for computing simple interest) feems to be assumed for a safe exposition of the Statute, viz. That fuch proportion as the whole year, (fupposed to confift of 365 dayes) hath to any propounded space of time more or less than a year, such proportion any interest, (not exceeding the rate limited by the Act) for any Principal lent for a year, ought to have to the interest of the same Principal for the time propounded: This Analogy being granted, the manner of computing simple interest, for any Principal lent and forborn any cime propounded, will be fuch as is exprest in the two next Sections.

NII. The interest or gain of 100 l. principal money forborn for a year being known, the interest of any other principal money for the same time, may be found out by one single Rule of Three; for as 100 l. principal, is in proportion to the interest thereof, so is any other principal to its interest: So if it be demanded what 270 l. will gain in a year at the rate of 6 l. for 100 l. for one year, the Answer will be found to be 16 l. 4 s. For;

l. l. l. l. l. s. d. 100. 6:: 270. 16,2 (or 16: 4:0

A fecond Example, What is the interest of 175 l. 18 s. 11 d. for a year, at the rate of 6 l. for 100 l. for

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for a year? Answ. 10 l. 11 s. 1 - 62 d. as by the following operation, (which is performed after the practical manner delivered in the nineteenth Rule of the second Chapter of this Appendix) is evident,

1. 1. 1. s. d. l. s. d.
100 . 6 :: 175 : 18 : 11 (10 : 11 : 1 62
multiply by . . . 6

1. 10 55 : 13 : 6

11 13

d. ... 1 62

VIII. If the interest of 100 l. principal for one whole year, or 365 dayes be known, the simple interest of any other principal, for any number of dayes more or less than 365, may be found out by the following Rule, viz.

Multiply these three numbers according to the

A Rule

compating fim-

ple interest fer

Rule of continual Multiplication, to wit, the given interest of 100 l. for a year, the principal, whose interest is required, and the number of dayes prescribed, reserving the last

dayes prescribed, reserving the last dayes.

product for a Dividend: Also multiply 365 by 100 and reserve this product for a

Divisor; Lastly finish Division, so shall the quo-

Note here, that the two principals, to wit 100 l.
and the other propounded, are supposed to be of
one and the same denomination: Also the interest
Z required

required will be of the same denomination with

the given interest of 100 1.

For an example of this Rule, let it be required to find out the interest of 400 % for a week, or 7 dayes, at the rate of 6 l. for 100 l. for a year, or 365 dayes; First multiplying these three numbers 6, 400, and 7 continually, (viz. multiplying 6 by 400, and the product thence arising by 7) the last product will be 16800 for a Dividend, also multiplying 365 by 100, the product is 36500 for a Divifor; laftly, dividing 16800 by 36500 (after cyphers at pleasure are added to 16800) the quotient, (according to the fourth Rule of the 27th Chapter of the preceding Book) will be discovered to be this decimal .4602, which is equal to 9 s. 2 d. I farth. (as will appear by the brief way of vabuing a decimal fraction in the fourth rule of the 26th: Chapter.)

The reason of the above mentioned rule for the computing of interest for dayes, will be manifest by this following way of folving the same question

by two fingle Rules of Three, viz.

I. 100 . 6 :: 400 .
$$\frac{6 \times 400}{100}$$
II. $\frac{365}{1}$. $\frac{6 \times 400}{100}$:: $\frac{7}{1}$. $\frac{6 \times 400 \times 7}{365 \times 100}$

Which fourth proportional in the latter Rule of Three, to Wit, 6 × 400 × 7, 365 × 100, being well viewed, the truth of the rule before delivered will be manifelt.

Hence one vulgar error in computing interest

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is discovered, for some argue thus, 61. is the interest of 100 % for a year, therefore 10 s. (or of 61.) is the interest for a moneth, and confer quently 2 s. 6 d. for a week, or feven dayes, and fo the interest of 400 l. for 7 dayes, computed after that manner would be 10 s. which exceeds the Anfwer found by the preceding Rule by 91d. very near, which fallacy bath its rife from the taking. (or rather miftaking) of 28 dayes for - 12 part of the number of dayes in a year, when indeed the just part of 365 dayes confifts of 30-5 dayes.

Moreover, by the help of this decimal fraction

of a pound, to wit, .000164383,

Another Rule which is very near the interest of for computing one pound for a day at the rate of fimple Interes 6 per cent. per annum (as will appear for dayes. by the preceding rule) the interest of

any principal, (supposed to be pounds or decimal parts of a pound) for any number of dayes propounded, at the faid rate of interest, may be found out by multiplication only, viz. First multiply the faid decimal .000164383 by the principal whose interest is required, then multiply that product by the number of dayes propounded, fo shall this laft product be the intereft required ; (but in these multiplications respect must be had to the cutting off of places in the products, according to the second and third rules of the 26th. Chapter, of the preceding Book;) for example, if it be required to find the interest of 1000 /. for 131 dayes, at the rate of 6 per cent. per ann. the Anfw. will be found 21.534+, or 21/, 10s. 8 d. + for according to the rule last given.

wed. ma-

teres

.000164383 × 1000 × 131 = 21.534 +

But at another rate of interest, a peculiar decimal instead of the said .000164383, (which serves only for 6 per cent.per annum) must be found out by the first rule aforegoing, before the latter rule can take place, the reason of which latter rule doth also evidently arise from two single rules of three.

IX. When an Annuity payable yearly is in ar-

The manner of fumming up Annuities in arrear with allowances of fimple interest.

rear for any number of years, and it is required to know what the same will amount unto, simple interest being computed for each particular yearly payment, from the time it became due, until the end of the term of years, the work will be as in this

following example, viz. If an Annuity, or yearly rent of 1341.105.6 d, be all forborn till the end of 4 years, what will it then amount unto, simple interest being allowed at the rate of 6 per cent. per annum for each years rent, from the time on which it was due, until the end of the said term of four

years? Answ. 586 l. 10s. 6 4.

It is evident by the question, that at the rate of interest propounded, there must be computed the interest of 1341. 105. 6d. (due at the third years end) for one year, (to wit, the fourth year) also the interest of the like sum due at the second years end, for two years, (to wit, the third and fourth years) likewise the interest of the same sum due at the first years end, for three years, (to wit, the second, third and sourth years) all which interest being added to the sum of the sour years rent, the total sum will shew what the said Annuity will a-

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mount unto at the end of the faid term of 4 years.

Explication.

The interest of 134 l. 1 is ... 8: 1:5.16

10 s. 6 d. at 6 per cent. per 2 is ... 16: 2: 10.32

nnum, for 2 is ... 24: 4: 3.48

The sum of the 4 years

rent, (to wit, 4 times is ... 538: 2: 0

134 l. 10 s. 6 d.)

All which added together give the Answer of the question, to wit.

X. When it is required to find out how much ready money will fatisfie a Debt due at the end of any space of time to come, by rebating or discompting at a given rate of simple interest, it may ple interest.

be effected by this rule, viz. First find out the interest of 100 l. at the given rate of interest, for the time which the ready money is to be paid beforehand, then adding the interest so found to 100 l. make alwayes the sum of that addition the first term in a rule of three; 100 l. the second term; and the debt propounded to be satisfied the third term; lastly, the sourch propositional sound out by the said Rule of Three shall be the ready money which ought to be paid in satisfation of the debt propounded.

Example 1. If a debt of 100 l. be payable at the end of a year to come, how much ready money will discharge that debt by rebating or discompting at the rate of 6 per cent. per annum? Answ. 94 l.

Z 3

6 s.

106 . 100 :: 100, 94.3396 t

That is to lay, if 106 l. (which is compos'd of 100 l. principal and 6 l. interest) proceeds from 100 l. principal forborn for a year, from what principal forborn for a year doth 100 l. (compos'd of principal and interest) proceed from? Answ. 94.3396 l. t (or 94 l. 6 s. 9½ d. very near) principal money: therefore 94 l. 6 s. 9½ d. in ready money, is of equal value with 100 l. due at the end of a year to come; for if the said 94 l. 6 s. 9½ d. be put forth at interest for a year, at the rate of 6 per cent. per annum, it will gain 5 l. 13 s. 2½ d. very near, which together with the said 94 l. 6 s. 9½ d. makes the 100 l. the debt first propounded to be discharged by rebate.

Example 2. If 150 l. 10s. be payable at the end of 73 dayes to come, how much present money will discharge the said debt, by rebating after the sate of 6 per cent. per annum? Answ. 148 l. 14 s. 3½ d. + as by the following operation is manifest.

dayes 1. dayes 1. 1. 365 : 6 : 1.73 . 1.2

1. 1. 1. 1.

That is to say, First I seek by a single Rule of Three, the interest of 100% for 73 dayes, at the rate of interest propounded, saying, if 365 dayes (or a year) gain 6% what will 73 dayes gain? Answ. 1-2% or 1.2% Then adding the said 1.2 to 100, I say, by

by a second Rule of Three, if 101.2 l. principal and interest, payable at the end of 73 dayes to come. be equivalent to 100 /. ready money, what ready money is 1501. 10s. (or 150.5) payable at the end of 73 dayes to come equivalent unto ? fo by multiplying and dividing according to the rules of Decimal multiplication and Division, (explained in Chapter 26, and 27. of the preceding Book) the quotient or answer of the question will be found 148.7154 t, that is, 148 l. 14 s. 3 - d. t (for the decimal .7154 being valued according to the brief way at the end of the fourth rule of the 26th. Chapter, will by inspection only be discovered to be 14 s. 3 d. which rule I shall here once for all, advise the Learner to be well acquainted with.

The proof.

Seek (by the Rule of Three) what the ready money found as aforefaid will gain, in so much time as it is paid before hand) at the rate of interest propounded; then having added this gain to the said ready money, if the sum be equal to the debt first propounded to be satisfied by rebate, the ready money was rightly found out. So the last example will be thus proved.

Which fourth proportional 1.7845 being added to 148.7154, the sum will be 150.4999 thich doth not want a farthing of 150% 105, the debt first propounded.

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XI.When

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Of the present pruities by difcompting at simple interest.

XI. When it is required to find the present worth of an Annuity, by rebating or discompting at a given rate of simple interest, the operation will be as in the following example, viz. How much present money is equivalent to an Annuity or rent of 100 %.

per annum to continue five years, rebate being made at the rate of 6 l. for 100 l. for one year, at timple interest; Answ. 425 l. 18 s. 9-d. very near.

It is manifest that there must be computed the present worth of 100 /. due at the first years end; also the present worth of 100 %. due at the second years end, and in like manner for the third, fourth and fifth years; all which particular present worths being added together, the aggregate or fum will be the total present worth of the Annuity, to wit, 8286150 1. in the example above propounded, 425 8821267

that is, 425 l. 18 s. 9 - d. very near.

3.

The operation by decimals (which will come near enough to the truth) will be as followeth, viz.

> I. 106 . 100::100 . 94,33962 + 112 . 100 :: 100 . 89,28571 + 118 . 100 :: 100 . 84,74576 +

124.100::100.80,64516 + 130 . 100 :: 100 . 76,92307 †

Answ. 425,93933 t

Here by the way, from the manner of resolving the last mentioned question, that Rule commonly called Equation of payments, which is insisted on by divers Arithmetical Writers, will be found errone-

ous, which I thus prove.

a. Since that rule aims at the reducing of feveral dayes of payment, upon which particular sums of money are due, unto a mean time upon which the aggregate or total of those particular sums ought to be paid, without dammage to the Debiter or Creditor, there must be necessarily some rate of interest implied; for otherwise why may not any day at pleasure be affigned for one intire payment.

2. If some rate of interest be implied, then equity requires that the present worth of the total sum payable at one intire payment, rebate or discompt being made according to that rate of interest, may be equal to the sum of the present worths of the particular sums of money, rebate being made at

the same rate of interest.

3. In regard the faid Rule doth mention no particular rate of Interest, it ought to be true at any

rate of interest whatsoever.

4. Let us therefore examine the faid Rule according to the rate of 6 per centum, per annum, simple interest, by taking the last mentioned question for an example, which (according to the accustomed manner) will be thus stated, viz. If 500 l. ought to be paid by five equal yearly payments, to wit, 100 l. at each years end, what time ought to be given for the payment of the said 500 l. at one entire payment, without loss either to the Debitor or Creditor.

5. By proceeding according to the faid rule of Equation of payments (which faith, If the sum of the products,

products, arising from the multiplication of each particular sum of money by its respective time, be divided by the sum or aggregate of the said particular sums of money, the quotient will be the mean time to be assigned for one intire payment) there will be found three years, which time (according to the said rule) ought to be given for the payment

of the whole 500 l.

6. Now if 500 l.due at the end of three years to come be worth as much in prefent money, as is the present worth of an Annuity of 100 l. to continue five years, then the faid Rule of Equation is true; 0therwise false; but the present worth of 500 1. due at the end of three years to come, rebate being made at the rate of 6 per centum per annum, simple interest will be found (by the tenth rule of this Chapter)to be 423 1.14 s.6 d.3 f. very near; also the prefent worth of the faid Annuity, rebate being made as before, is found (as appeareth by the resolution of the last mentioned question) to be 425 1.18 s. 9d. very near ; wherefore it is evident that the Creditor loseth 2 1.4 s. 23 d. very near, by receiving the whole 500 l. at three years end : moreover at 6 per centum, per annum, compound interest, he would lofe 1 1.8 s. 6 d. very near, as will be manifest by the Tables of compound interest hereafter expressed : so that the lofs will be either more or lefs according as the rate of interest doth differ : and therefore I conclude the faid Rule, (as alfo all other rules or resolutions of questions which have dependance thereon) to be erroneous.

Although questions of this nature feldom come into practice, yet he that will take the pains, may find out fuch a mean time as is required by the said ch

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id ule Rule of Equation of payments, at any rate of simple

interest by this following rate, wit.

First, by the preceding tenth Rule of this Chapter find out the prefent worth of every particular fum in the question payable at a time to come, by rebating at the rate of interest agreed on; then find in what time, the fum of those prefent worths will be augmented unto the rotal of all the particular fums payable at times to come, according to the first agreement, fo shall the time found out be the mean time for the payment of the whole debt : thus the mean or equated time in the last example will be found to be 2.8979, &c. years, (not three years, as the faid Rule of Equation of payments would have it) for by rebating at 6 per cent. per annum. simple interest, 500 l. payable at the end of 2.8979. &c. years to come, (that is 2 years and 328 daves very near) is worth in ready money 423 % 18 s. 9 d. very near, and the same ready money is also the present value of 100 1. Annuity for 5 years, at the same rate of interest, as before bath been manifested. But to return to the path from which I have made a digression.

From the preceding tenth rule of this Chapter the following Tables 1. and II. are deduced, whose

construction and use are afterwards declared.

Tears	Table I. Which sheweth in decimal parts of a pound, the present worth of one pound due at the end of any number of years to come, not exceeding 7 years, at the rate of 6 per centum, per annum, simple interest.	Years	Table II. Which sheweth in pounds and decimal parts of a pound, the present worth of one pound Annuity, to continue any number of years not exceeding 7, at the rate of 6 per centum, per annum, simple interest.
1	1.943396	r	. 943396
2	.892857	2	1 . 836253
3	.847457	3	2 . 683710
3 4 5 6	.806451	4	3 . 490162
5	.769230	5	4 . 259393
6	.735294	6	4 . 994687
17	.704225	7	5 . 698912

The Construction of Table I.

The numbers in the first Table which are placed right against the numbers of years, 1,2,3,4,5,6, and 7, are decimal fractions, one pound of English money being the Integer, and are thus found (according to the preceding tenth Rule of this Chapter:)

106 . 100 :: 1 . ,943396 † 112 . 100 :: 1 . ,892857 † 118 . 100 :: 1 . ,847457 †

whereby

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whereby it appears, that 1 l. due at the end of a year to come, is worth in ready money .943396 + that is, 18 s. 10 d. 1 f. and fomewhat more. Also 1 l. due at the end of two years to come, is worth in ready money .892857 +, or 17 s. 10 ½ d. rebate being made at the rate of 6 per centum, per annum, simple interest; the like is to be understood of the rest of the numbers in Table I. which may be continued to more years, and other Tables also of rebate may be framed upon the same ground, for moneths, or dayes, by the ingenious Artist.

The use of Table I.

The practical use of the said first Table will be manifest by solving this following question; viz. How much ready money will discharge 345 l. 15 s. 6 d. due at the end of five years to come, by rebating simple interest at the rate of 6 per centum, per annum, Answer, 265 l. 19 s. $7\frac{1}{4}$ d. which is thus found out; viz. In the preceding Table I. right against 5 years, I find the decimal .76923, which shews that 1 l. due at the end of five years to come is worth in ready money .76923, (that is, 15 s. $4\frac{1}{4}d$.) then instead of is s. 6 d. mentioned in the question propounded, taking the decimal .775 which is equal to 15 s. 6 d. (the same being reduced according to the fifth rule of the 23 chapter of the preceding book) I say, by the Rule of Three.

1.,76923:: 345.775. (265.9805 †
That is to fay if 1 l. give .76923 l. what will 345.775 l. give? Answ.265.9805 l. for multiplying 345.775 by .76923, according to the second Rule of the 26 Chapter of the preceding Book, the product will be 265.9805, that is, 265 l. 19 s. 7 d.

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The Confirmation of Table II.

The numbers in the second Table are found out by the addition of those in the first, viz the first number in the latter Table is the fame with the first number in the former, the fecond in the latter is the fum of the first and second in the former; the third in the latter is the fum of the first, second and third in the former, and in that manner the rest are found ; (the reason of which composition is manifest from the example of the eleventh rule aforegoing ;) otherwise, the numbers in Table II. may be found more easily thus, viz. the first number in the faid Table II. is the same with the first number in Table I, the fecond number in the latter Table is compos'd of the fecond number in the former and the first in the latter, the third number in the latter Table is compos'd of the third number in the former and the fecond in the latter, the fourth in the latter is compos'd of the fourth in the former and the third in the latter; the like is to be understood of the rest of the numbers in Table II. which might be continued to more years, and fitted to other tates of interest, but I shall spare that labour, in ragard a more equal way of finding out the prefent worth of an Annuity, agreeable to the accustomed and practical rates of buying and felling Annuities or Rents, for terms of years, is grounded upon a computation of interest upon interest, as will hereafter be mademanifelt, for at limple interest an Annuity will be overvalued.

The use of Table II.

The use of Table II. will appear by this following Y

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ing example; viz. What is the present worth of an Annuity of 100 l. per annum payable yearly during the term of five years, discompt or rebate being made at the rate of 6 per centum, per annum, simple interest? Answer, 425 l. 18 s. 9 d. very near; which is thus found out, viz. In the preceding Table II. right against five years, I find this number 4.259393, which shews that an Annuity of 1 l. payable yearly during sive years, is worth in ready money 4.259393 l. (that is 4 l. 5 s. 2 d. and somewhat more) therefore, I say, by the Rule of Three?

1. 1. 1. 1.

That is to fay, if 1 l. give 4.259393 l. what will 100 l. give ? Answer, 425 l. 18 s.9½ d. very near, for by multiplying 4.259393 by 100, the product (according to the second rule of the 26 Chapter of the preceding Book) is 425.9393, that is, 425 l. 18 s.9½ d. very near. Which operation being compared with the manner of solving the same question before mentioned in the eleventh Rule of this Chapter, the great benefit of Tables of this kind in point of expedition will be apparent.

xII. When it is required to know, unto what fum of money any propounded principal forborn any number of years will at the end of fuch term be augmented unto, interest up.

on interest being computed at a given rate, there must be found a rank of continual proportionals, more in number by one then is the number of years in the question; of which proportionals the first is the principal assigned, the second must increase

or proceed from the first, the third from the second, &c. in such manner or rate, as 106 proceeds from 100 (or as 108 from 100, if the rate of interest be 8 per centum) then will the last proportional be the Answer of the question: So if 300 pounds principal money be put forth at interest upon interest, at the rate of 6 l. for 100 l. for one year, and all forborn until the end of 4 years, there will then be due 378.743088, or 378 l. 14 s. 10 \frac{1}{2} d. very near, as by the four following Rules of Three is manifest.

For the said 300 l. will at the first years end be augmented unto 318 l. which 318 l. being put forth as a principal for 1 year, (will at the second years end) be augmented unto 337.08, again this 337.08 being put forth as a principal for 1 year, will (at the third years end) be augmented unto 357.3048, in like manner 357.3048 being put forth as a principal for 1 year, will (at the fourth years end) be augmented unto 378.743088 which is the number required by the question. And if the work be well examined, it will appear, (as was before declared) that the principal first assigned, to wit 300 l and the numbers resulting successively at the ends of the several years are continual proportionals, viz. these five numbers are so qualified, that if the second be mul-

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tiplied by it felf, the product will be equal to the product of the first and third; also if the third be multiplied by it felf, the product will be equal to the product of the second and fourth; In like manner, if there were more continual proportionals in a rank, if any one proportional which is placed between two next on each fide of fuch one, be multiplied by it felf, the product will be equal to the product of those two extreams (which is a property peculiar to continual proportionals.)

Note here by the way, that if any two numbers be propounded, suppose 300 and 318, and it be required to find to them a third, a fourth, a fifth, &c.in continual proportion, multiply the fecond proportional 318 by

Two numbers being given to find a third, a fourth, a fifth, Oc. in continual proporti-611.

it felf. and divide the product 101124 by the first proportional 300, so shall the quotient 337.08 be a third in continual proportion; In like manner if you multiply the third proportional 337.08 by it felf, and divide the product 113622.9264 by the fecond proportional 318 the quotient 357.3048 shall be a fourth in continual proportion, and after the same manner a fifth, a lixth, or as many as you please may be found out.

From what hath been faid by way of explication of the preceding twelfth Rule, the following Table III. is deduced, the construction and use

whereof is afterwards declared.

Az

Table

7	m of	7	000	440	492	351	234	382	890	296	307	\$84	854	282	349	711	177
	Which sheweth what one pound will amount unto, being forborn unto the end of any term of years under 31, compound interest being computed yearly, at any of these rates, to wit, 4, 5, 6, 7, 8, 9, 10, 11, and 12 per centum, per annum.	-	1.04004 1.05000 1.06000 1.07000 1.08000 1.09000 1.1000 1.11000 1.12000	1,10250 1,133601,14490 1,166401.18810 1.21000,1.232161.25440	1.12486 1.15762 1.19101 1.22504 1.2597 1.29502 1.33100 1.36763 1.40492	1.16985 1.21 550 1.26247 1.31079 1.36048 1.41158 1.46410 1.51837 1:57351	1.21665 27628 1.33822 1.40255 1.46932 1.53862 1.61051 1.68505 1.76234	1,26531 1,34009 1,41851 1,50073 1,58087 1,67710 1,77156 1,87041 1,97382	1.31593 1.40710 1.50363 1.60578 1.71382 1.82803 1.948712.076162.21068	1.36856 1.47745 1.59384 1.71818 1.85093 1.992562.14358 2.30453 2.47596	1.423311.551321.689471.838451.999002.171892.357942.558032.7730	101.48024 1 62889 1.79084 1.96715 3.15892 2.367362.593742.83942 3.10584	111.539451.71031.898292.1048522331632.580422.853113.151753.47854	121.60103 1 79585 2.01219 2.25219 2.51817 2.81266 3.13842 3.49845 3.89597	131.665071.885642.132922.409842.719623.065803.452273.883284.36349	1.73167 1.97993 2.26090 2.57853 2.93719 3.341723.79749 4.31044 4.88711	
	efera)	1.1	1000	3216	6763	1807	8505	7041	9194	0453	\$803	3942	\$175	9845	8328	1044	4
	the en	_	1.1	00,1.2	001.3	01.5	0.11	61.8	12.0	82.3	42.5	42.8	1,3,1	2,3.4	73.8	94.3	-
	a unto at any	10	1000	2100	3310	4641	6105	7715	9487	1435	3579	5937	8531	1384	4522	7974	
	forborz carly,		000	STO F.	102 1.	581.	62,1.	10 I.	303 1.	562.	892.	362.	42.2.	663.	803.	723.	
111.	being jeted ye	6	1.090	1.188	1.295	1.41	1.538	1.677	1.828	1.992	2.171	2.367	2.580	2.812	3.065	3.341	,
E	nto, l	2	8000	6640	1265	2048	5932	3087	382	1093	0000	892	163	817	962	719	
IABLE	being to	-	0.1	01.10	1.2	1.36	21.40	31.5	31.71	31.85	1.99	2.15	2.33	2.51	2.71	2.93	-
LI	ill am erest 12 pe	7	0240	1449	2250	3107	1025	2005	5057	71818	3384	1290	048	5215	10984	17853	
	and int	-	00	60 1.	01	47 1.	22 1.4	511.	53 1.	84	47 1.8	34/1.9	292.1	192,2	92 2.4	00 2.5	
	ompou	9	090.	.123	191.	.262.	.338	418	.503	.593	.689.	.790	868.	,012	.132	2600	
-	s I, c		000	250 1	762 1	1055	528	1 500	1017	745 1	32 1	1 688	0331	185/2	64 2	193 2	
	meth der	5	1.050	1.10	1.15	1.21	270	1.34	1.40	1.477	.55	1 62	1.710	1.79	1.88	1.979	
	ich sheweth what one pound will amount unto, being lears under 31, compound interest being computed y.		1004	1.0816c	2486	6985	1665	5531	1593	685c	2331	8024	3945	0103	5507	3167	
-		4	-	1.0	1.1	1.1	1.2	1,2	1.3	1.3	4.1	0 I.4	1.5	2 1.6	3,1.6	1.7	. (
	Yea	rs.	-	17	3	4	3	0	1	00	9	H	1	-	-	-	_

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The Construction of the preceding Table III.

The numbers 1,2,3,4, &c. to 30, in the first column on the left hand fignifie years ; the numbers 4,5,6,7,8,9,10,11, and 12, placed at the head of the rest of the columns signifie rates of interest, for 100 llent for a year, and the numbers placed in the feveral columns underneath those rates of interest, are found out by the Rule of Three in decimals, in mann er following; viz.

1 100 : 104 :: 1 .. (1.04 100 . 104 :: 1.04 .. (1.0816 III. 100 . 104 :: 1.0816 .. (1.12486

That is to fay, First, if 100 1: put forth at interest for a year be augmented to 104 l. at the years end, what will 1 ?. be then augmented unto at the same rate? Answ. 1.040 l. (that is 1 los. 9 d. 2 f. and somewhat more) which 1.04 (or 1.04000, the cyphers after the 4 being of no value in decimals) is the first number in the second column belonging to 4 per centum, and is placed right against I year in the first column.

Secondly, fay if 100 1. lent for a year be augmented to 104 l. at the years end, what will 1.04 l. be then augmented unto at the fame rate? Anim. 1.0816 l. (that is 1 l. 1 s. 7 d. 2 f.t) which 1.0816 is the second number in the faid column of 4 per cent. and is placed right against 2 years in the first column.

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Thirdly, as 100 is to 104; fo is 1.0816 to 1.124864 (or 11.25.5 d. 2f. t) which 1.12486 is the third number in the column of 4 per centum, and is placed right against 3 years in the first column. Hence it appears, that 1 l. 2t 4 per centum, per annum, compound interest, will at the end of 3 years be augmented unto 1.124864 l. (that is, 1 l. 2 s. 5 d. 2f. and somewhat more.)

After the same manner the fest of the numbers in the second column, as also in the other columns

are found out (mutatis mutandis.)

The use of the preceding third Table.

Quest. 1. What will 136 l. iy s. 6 d. be augmented unto, being forborn 20 years, interest upon interest being computed at the rate of 6 per sensum, per annum? Answ. 438 l. 13 s. 1 d. very near, which is thus found out.

First, looking into the fourth column of the said third Table, to wit, that column which hath the sigure 6 placed at the head of it; I find right against 20 years the number 3.20713, which shews that 11. being continued 20 years at 6 per centum, per annum, compound interest, and all forborn until the end of the said term will be augmented unto 3.20713 1. (that is 3 1.4 s.1 d.2 f. and somewhat more) therefore after the 15 s. 6 d. in the question is reduced to the deeimal .775 (by the sixteenth rule of the 23 Chapter of the preceding book) I multiply the said tabular number 3.20713 by 136.775 (the sum propounded in the question) according to the second rule of the 26th Chapter, so the Product is Aa 3 found

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found to be 438.665,&c. that is,438 l. 13 s, 1 d. for the Answer of the question. View the operation here following.

1 . 3.20713 :: 136.775 . (438.665 t

438 65520575

Quest. 2. If 320 l. be forborn it years, at interest upon interest at 5 per centum, per annum, what will be due at the end of those eleven years for principal and interest? Answer, 547 l. 6 s. 1 d. t. For in the third column of the third Table, under the figure five at the head of the column and right against 11 years you will find this number 1.71033 which shews that 1 l. at the end of 11 years will at 5 per centum, per annum, compound interest, be augmented to 1.71033 (that is 1 l. 14 s. 2 d. 1 f. and somewhat more) wherefore by multiplying the said 1.71033 by 320 the number of pounds propounded in the question) the product will be 547 305, &c. that is 547 l. 6 s. 1 d. t for the Answer of the question, See the following operation.

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After the same manner the numbers belonging to any of the other rates of interest mentioned in the third Table are to be used.

XIII. When an Annuity payable yearly is in arrear for any number of years, and it is required to know what the same will amount unto, compound interest being computed for each particular Annuity from the time it became due, until the end

The manner of fumming up Annuities in arrear with allowances upon interest.

of the term of years, the work will be as in the following example; viz Suppose an Annuity of 300? payable at yearly payments be forborn, and all unpaid until the end of four years, the question is, what will then be due, compound interest being computed at the rate of 6 per centum, per annum, for each yearly payment from the time it becomes due to the end of the said term of four years? Answ. 1312 1.7 5.8 d. very near.

It is evident by the question, that there must be computed what 300% due at the third years end will be augmented unto in one year (to win the fourth year) at 6 per centum. Also what 300% due at the second years end will be augmented unto in two years; (to wit the third and fourth years) like-

wife what 300 l. due at the first years end, will be augmented unto, in the three following years, (to wit the second, third, and fourth years) all which sums being added to 300 l. (the payment due at the end of the fourth year, which is incapable of any improvement) the aggregate or sum will be the total money in Arrear at the end of the sourth year, to wit, 1312 \frac{3848}{10000} l. as may appear by the following operation, viz.

The last payment of the Annuity due at the end of the fourth year 300.

Again, the 300 l. due at the third years end, will in one year after the rate of 6 per centum, be augmented unto

Also 300 l. due at the second years end, will in two years at the rate of 6 per centum, per annum, compound interest, be augmented unto (as appears by the first example of the twelfth Rule aforegoing.)

In like manner, 300 l. due at the first years end, will in three years 357.3048 be augmented unto

The fum due at four years 1312.3848 end

The invention of the numbers before mentioned being well examined, it will appear that if an Annuity or Rent payable at yearly payments be improved proved to the utmost at interest upon interest, and all forborn or, respited unto the end of certain years, the total then due will be the sum of a rank of continual proportionals as many in number as there are yearly payments, the first of which proportionals is the first (or any one) years rent, and the second proportional proceeds from the first in the same rate as 106 proceeds from 100, if the rate of interest be 6 per centum, (or as 108 proceeds from 100, if the rate of interest be 8 per centum, &c.) and so likewise the third from the second, the fourth from the third, &c. (after the manner of the operation in the first example of the twelsth Rule of this Chapter.)

Otherwise,

Find a principal which may have such proportion to 300 as 100 hath to 6, and say by the Rule of Three;

6 . 100 :: 300 . 5000

That is to say, as 6 l. interest hath 100 l. for a principal, so 300 l. interest hath 5000 l. for a principal, then seek what 5000 l. will be augmented unto, being forborn sour years at 6 per centum, per annum, compound interest, (after the manner of the sirst example of the twelfth rule aforegoing) so will you find 6312.3848, from which subtracting the said principal 5000 l. the remainder (as before) is 1312.3848 l. being the sum which 300 l. Annuity will be augmented unto at the end of sour years, according to the said rate of interest, the Annuity being payable at yearly payments.

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If a principal be put forth at interest upon interest payable by yearly payments, and all be forborn until the end of certain years, the total then due is equal to the aggregate or fum of these three numbers, to wit, the faid principal first put forth ; the fum of the annual simple interests of that principal; and the utmost improvement of those simple interests by computing interest upon interest: wherefore if from the faid aggregate the first principal be subtracted, the remainder must necessarily consist of the sum of the annual simple interests, (which are in the nature of an Annuity) and the utmost improvement of those simple interests (or Annuity) by computing interest upon interest.

The Construction of the following Table IV.

Upon the aforesaid grounds, the following Table IV. is calculated, to shew what one pound Annuity, payable at yearly payments, and forborn any number of years under 31, will amount unto by computing interest upon interest at any of the rates exprest at the head of the faid Table.

But the same Table may be more easily composed by the addition of the numbers in the preceding Table III. in this manner, viz. the first number in each of those columns in the following Table IV. at the head whereof are placed the numbers 4, 5, 6, 7, 8, 9, 10, 11, and 12, fignifying rates of in-

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terest per centum, is 1 or unity, the second number in each of these columns in the latter Table is composed of 1 or unity, and the first number in the respective columns of the said preceding Table III.

Also the third number in each of the said columns of this latter Table is compos'd of 1, and the fum of the first and second numbers of the respeclive columns of the former Table, and in that order the rest are found out ; or more easily thus, the third number in the latter Table is compos'd of the fecond number in the latter, and of the fecond in the former; the fourth number in the latter is compos'd of the third in the latter, and of the third in the former, &c. But you are to observe that according to either of these wayes of composing the fourth Table by Addition, the numbers in the preceding Table III. ought to be continued to more places then are there exprest to prevent error which may happen by adding of defective decimal fractions.

rephich heweth what one pound Annuity, payable by yearly payments, and forborn any number of years under 31, will amount unto, at the end of the term, compound interest being computed at any of these rates, to mit. 4,5,6,7,8 9,10,11, and 12 per centum, per annum.

AIX	13 16.6	1215-0	012.0	10.5	92	7.8	6.6	3.4	4.2	3.1.	2.0	1.00	4
16167	2683	2580	0610	8279	1422	9829	3297	1632	4.24646	3.12160	2.04000	1.00000	_
19.59863	17.71298	15.91712	12.57789	11.02656	9.64910	8.14200	6.8019	5.52563	4.31012	3.15250	2.05000	1.00000	5
21.01500	18.88213	16.86994	13.18079	11.49131	9.89746	8.39383	6.63297 6.80191 6.97531	5.41632 5.52563 5.63709	4.31012 4.37461	3.18360	2.06000	1.00000	6
22.55048	20.14064	17.88845	13.81644	11.97798	10.25980	8.65402	7.15329	5.75073	4.43994	3.21490	2.05000 2.06000 2.07000 2.08000 2.09000 2.10000 2.11000	I.00000	7
27 1 (21)	21.49529	18.97712	14.48656	12.48755	10.63662	8.92280	7.33592	5.86660	4.50611	3.24640	2.08000	1,00000	8
26.01918	12.95338	20.14071	15.19292	13.02103	11.02847	9.20043	7. 52333	5.08471		3.27810	2.09000	1.00000	9
27 9749	24.5227	21.38428	15.93742	13.57947	11.43588	9.48717	7.71561	6.10510	4.64100	3.27810 3.31000	2.10000	1.00000	10
30.0949	26.21163	19.50142	16 72200	14.16397	11.85943	9.78327	7.91285	6.22780	4.70973	3.34210	2.11000	1.00000	11
1418,29191 19.5986321.0150622.5504824.3149226.0191827.9749830.0949132.39266	3 16.62683 17.71298 18.88213 20.1406421.4952912.95338 24.52271 26.21163 28.02916	1215.02580 15.91712116.86994 17.8884518.97712120.14071 21.38428 22.71318 24.13313	10 12,00610 12.57789 13.18079 13.81644 14.48656 15.19292 15.93742 16 72200 17.54873	10 58279 11.02656 11.49131 11.97798 12.48755 13.02103 13.57947 14.16397 14.77565	9 21422 9. 64910 9.89746 10.25980 10.63662 11.02847 11.43588 11.8594 112.29969	10.08901	6.63297 6.80191 6.97531 7.15329 7.33592 7.52333 7.71561 7.91285 8.11518	5.75073 5.86660 5.08471 6.10510 6.22780 6.35284	4.57312 4.64100 4.70973 4.77932	3.37440	2.12000	1,00000 1,00000 1,00000 1,00000 1,00000 1,00000 1,00000	12

IV.
Table
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Continuation
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	rs.	4	2	9.	7	8	0	10	11	1.2
	62	1.82453	16 21.82453 23.65749 25.67252 27.88805 30.32428 33.00339 35.94972 39.18994 42.75328	28.67252	27.88805	30.32428	33.00339	35.94972	39.18994	42.75328
	172	3.69751	25.84036	28,21287	30.84021	33.75022	36.97370	40.54470	44.50084	48.88367
	8 2	5.64541	18 25.6+541 28.13238 30.90565 33.99903 37.4502441.30133 45.59917 50.39593 55.74971	30.90565	33.99903	37.45024	41.30133	45.59917	50.39593	\$5.74971
_	9 2	7.67120	19/27.67120/30.53900 33.73999 37.3789641.4462646.01845 \$1.18909/86.93948 63.43968	33.75999	37.37896	41.44626	46.01845	\$1.18909	\$6.93948	63.43968
1.4	0	9.77807	20 29 77807 33.06595 26.78559 40.99549 45.76196 51.16011, 57.27499 64.20283 72.05244	16.78559	40.99549	45.76196	\$1.16011	57.27499	64.20283	72.05244
~	1-1	1.96920	21 31.96920 15.71925 3949272 44.86517 50.42292 56.76453 64.00249 72.26514 81.69873	39,99272	44.86517	50.42292	56.76453	64.00249	72.26514	81.69873
-4	2 3	4.24796	22 34.24796 38,50521 43.39228 49.00573 55.45675 62.87333, 71.40274 81.21430 92.50258	43.39228	49.00\$73	55.45675	52.87333	71.40274	81.21430	92.50258
-	33	6.61788	23 36.61788 41.43047 46.99582 53.43614 60.89329 69.53193 79.54302 91.14788 104.60289	46.99582	53.43614	60.89329	59.531931	79.54302	91.14788	104.60289
-7	43	9.08260	24 39.08260 14 50199 50.81557 58.17667 66.76475,76.78981 88.49732 102.17415 118.15524	50.81557	\$8.17667	56.76475	18684.9	88.49732	102,17415	118.15524
0	5 4	1.64590	25 41.64590 47.72709 54.86451 63.24903 73.10593 84.70089 98.34705 114 41330 133.33387	\$4.86451	53.24903	73.10593 8	4.70089	98.34705	114 41330	133.33387
. 7	4	4.31174	26 44.31174 51.11345 59.15638 68.6764679 95441 93.32397 109 18176 27.99877 150.33393	39.15638	8.676467	9 95441 9	3.32397	192181 60	27.99877	150.33393
-	7	7.08421	27 47 08421 54.66912 63.70576 74.483 82 87.35076 102.72313 121 09994 143.07863 169.37400	53.705767	4.48382/8	7.3507610	12.72313	21.099941	43.07863	169.37400
-	8	9 9 6 7 5 8	28 49 96778 [58.40258 68.52810 80.69769 95.33882 112.96821 134.20993 159.81718 190.6988	58.528ro/8	0,692690	5.33882 11	2.96821	14.20993	\$9.81718	88869.06
N	5 6	2.96628	29 52.96628 [62.32271] 13.63979 [87.34652 103.96593 124.13535] 148.63092 178.39718 214.58275	13.639798	7.34652/10	3 96593 12	4.1353514	18.63092	78.39718	214.58275
-	olgi	6.08403	13 0156 08403 66 438 84 179 05818 94 46078 1113 2 8 321 1136,30753 164 49402 1199 02087 1241.332681	9.05818/9	1.4607811	3.28321 13	6.30753 10	4.49402	99.02087	241.33268
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The use of the preceding Table IV.

The use of the said fourth Table will be manifest by the manner of folving this Question, viz. If an Annuity of 201. payable by yearly payments for 15 years, be all forborn or unpaid until the end of the faid term, what will it then amount unto, upon a computation of interest upon interest, at the rate of 6 per cent. per annum ? Answ. 465 l. 10 s. 4 d.2 f. very near, as by the following operation is evident : For in the column belonging to 6 per centum, (to wit, that column which hath the figure 6 placed at the head of it) right against 15 years, you will find 23.27596, which shews that an Annuity of 1 l. payable at yearly payments for 15 years, will at the end of the faid term (compound interest being computed at 6 per cent.per annum) amount unto 23.27596 l. (or 23 l.5 s.6 d.+) Therefore multiplying the faid tabular number 23.27596 by 20, (20 because the Annuity propounded is 20 1.) the product will be 465.519 t, that is 465 l. 10 s. 4 d. 2 f. which is the Answer of the question; view the following operation.

1 . 23.27596 :: 20 . (465.519 t

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In the same manner the numbers in the other columns are to be used.

of rebate at at a time to come, and it is required to know what it is worth in ready money, rebate being made at a given rate

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of compound interest, the work will not be much different from the twelfth Rule of this Chapter. viz, there must be found a series or rank of continual proportionals more in number by one, than is the number of years in the question; of which proportionals, the first is the money propounded to be rebated, the second must decrease or lessen from the first, the third from the fecond, &c. in fuch manner or rate as 100 decreafeth from 106 (or as 100 from 108 if the rate of interest be 8 per centum) then will the last proportional be the answer of the question: So if 378 743088 /. be due at the end of four years wholly to come, it will be found to be worth in ready money 300 l. rebate being made at compound interest at 6 per centum, as by the four following Rules of Three is manifest, which may be proved by the preceding twelfth rule, where it will appear that 300 l. being forborn four years, will at the faid rate of compound interest be augmented unto 378,743088 1.

Upon this ground, the following Table V. is calculated to shew what one pound due at the end of any number of years to come, is worth in present money, rebate being made at the rates of compound interest, mentioned in the said Table; by the help whereof and of Multiplication, questions of rebate for any sum propounded may be performed without considerable error.

Table

ABLE

442300.387817.340461.299246 263331.231994.204619 -4969899 444012 397113 355534 318630 285840 2596675 468839 414964 367697 329178 15. 355264.481017 417265 362446. 315241 .274538 239392 .209004. 182696 67556- 613913 558391 508349.463193 422410 385543.352184.321973 .759917 710681.665057.622749 583490 547034.513158.481658.452349 649580 584679 526787 475092 428882 387532 350494 317283 287476 sphich shewith what one pound, payable at the end of any term of years to come under 31, is 863837.839619.816297.793832.772183.751314.731191.711780 591898 543933.500248.460427 424097.390924.360610 .901538 .952381 .943399 934579 .925925 .917431 .909090 .900900 .892857 .924556 .907029 .889996 .873438 .857338 .841680 .826446 .811622.797193 792093 762895 735029 708425 683013 65873 1,635518 .821927 783526 747258 712986.680583 64993 620021 593451 567426 30690 676839 627412 582009 540268 501866 466507 433926 403883 worth in ready money, discompt or rebate being yearly computed at any of these rates, to wit, 4, 5. 6, 7. 8. 9, 10, 11, and 12 per centum, per annum, compound interest. 10 0 . 7025861644608 854802 822702 12.624596.556837 3 600573 530321 141.5774741.505067

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00	.493628	493628.415520.350343.295864.250249.211993.179858.152822.13003	.350343	-298864	250249	.211	993	17985	8.1528	322	13003
6	.474642	474642 395733 39012 276508 231712 194489 163508 137677 16506	330812	.276508	231712	194	489	16350	8.1376	777	11670
0	.456386	.456386.376889.311804.258419.214548.178430.148643.124034.	.311804	258419	.214548	178	430	14864	3 .1240	34	103666
17	.438833	438833 358942 294155 241513 198655 163698	294155	241513	.198655	.163	869	135130.111742.09255	0.1117	142	92560
22	.421955	.421955:341849.277505 225713 183940 150181.122846 100668 0826	277505	225713	183940	1150	181	122840	1000	899	08264
23	.405726	.405726.325571-261797.210947.170315.137781.111678.090692.0747	261797	210947	.170315	.137	781	111167	8.090	592	07278
7	.390121	.390121 310067 246978 197146 157699 126405 101525 081705 06588	246978	197146	157699	126	405	10152	180.	105	988990
52	375116	.375116.295302.232998.184249.146018.115967.092396.073608.05882	212998	184249	146018	1115	196	092390	6.073	809	05882
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~	.346816	346816.267848.207367.160930.125186.097607.076277.059742.046893	.207367	.160930	.125186	.097	607	.07627	650.1	742	04689
~	.333477	.333477-255093-195630-150402-15913-089548-069343-053821,041869	.195630	150402	.115913	680	548	.06934	3.053	821	04186
29	.320651	320651. 242946. 184556 140562. 107327-082154. 061039. 048487. 03728	184556	140562	.107327	-082	154	06103	9.048	487	02728
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The Construction of the preceding Table V.

The numbers 1,2,3, 4, &c. to 30, in the first column on the left hand, fignifie years; the numbers 4, 5,6, 7, 8, 9, 10, 11, and 12, placed at the head of the reft of the columns fignifie rates of intereft for 100 % lent for a year, and the numbers placed in the feveral columns underneath those rates of interest are found our by the Rule of Three in decimals, in manner following, viz.

(,9615384615,&ci 104.100:: I 104.100 :: ,9615384 6ist . (,9245562, &c. 104.100::,9245562,846. (,888996 +

That is to fay, First, if 104 decrease to 100, or if 104 Lipayable at the end of a year to come be worth 100 1. ready money, what ready money is 1 1. due at the end of a year to come worth? Answer, 19613384615 + (or 19 1. 2 d. 3 f. very near) So that 1961538 is the first decimal in the second column belonging to a per centum, in Table V. and is placed right against I year in the first column.

Secondly, fay in like manner if 104 decrease to 100, what will .9615384615, &c. (the decimal found by the first rule of three) decrease unto? Answer, 9245562, &c. the first 6 places whereof, to wit, .924556 are the fecond decimal in the faid column of 4 per cent. which is placed right against

two years.

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Thirdly, as 104 is to 100; so is ,0245562, &c. (the decimal found by the fecond Rule of Three) to .888996 + (or 17 s. 9 d. 1 f. +) which is the third decimal in the column of 4 per centum. Hence it appears that 1 l. due at the end of three years to come is worth .888996, + (or 17 s. 9 d. 1 f. and somewhat more) in ready money, rebate being made at the rate of 4 per centum, per annum, compound interest.

fractions in the faid second column, as also in the before columns are found out (mutatis mutandis.)

The use of the preceding Table Vinnant

To exemplifie the faid fifth Table, let it be required to find our how much ready money will difcharge a debt of 3 56 1. payable at the end of feven years to come, by rebating at the rate of 7 per centum, per annum, compound interest? Answ.221 413 s. 11 d.3 f. very near. For in the fifth column, at the head whereof is placed 7; fignifying 7 per centum, right against 7 years, I find .622749, which shews that 1 1. due at the end of 7 years to come is worth in present money .622749 decimal parts of a pound, rebate being made at the faid rate of compound interest. Therefore multiplying the faid tabular number .622749 by the faid 356 1. (the debt propounded) the product (according to the fecond rule of the 26th Chapter) will be 221,698. &c.that is,221 1.13 s.11 d.3 f. which is the Answer of the question. See the subsequent operation.

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1 : ,622749 :: 356 . (221.698 ±

3736494 3113745 1868247

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In the fame manner the numbers in the other columns are to be used.

To find the prefent worth of Amutities by a computation of compound inteAV. The finding out the present worth of an Annuity, is grounded upon this foundation, to wit, if the present money which is paid for the purchase of an Annuity, to continue any term of years, be put forth at any

rate of compound interest, and all forborn until
the end of the said term, and that the total money
then due be put into one Scale: also if the total sum
of the utmost improvements of the annual payments of the Annuity, put forth at the same rate of
compound interest, from the time those annual
payments become due until the end of the term, be
put into the other Scale, the Scales must be even;
wie the said two total sums of money must be equal
one to the other.

Now to find out such a present worth of an Annuity, there are divers wayes, some of which I shall here explain by examples:

First therefore let it be required to find the prefent worth of an Annuity of 378.743088 1. to continue three years compound interest being computed at 6 per cent. per ann. Answer, 1012.3848 1.

357.3048

It is evident by the question that there must be computed (after the manner of the Example upon the fourteenth Rule aforegoing) the present worth of 378 143088 1. due at the first years end; also the present worth of the like sum due at the second years end, and in like manner for the third year; all which particular present values being added together, the aggregate or sum will be the total present worth of the Annuity propounded, viz.

378.743088 l. payable at the end of one year is worth in ready money (as is evident by the fourteenth

rule aforegoing.)

Also the like sum payable at the end of 2 years to come is worth in 337.08

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Again, the like sum payable at the end of three years to come, is worth in ready money
Therefore the total present worth of an Annuity of 378.743088 /. to continue 3 years is

Otherwise.

Find a Principal which may be in such proportion to the propounded Annuity 378.743088 1. as 100 is to 6. Which will be exactly 6312.3848 1. for

6, 100 :: 378.743088 . 6312 ,3848

Then supposing this Principal so found to be a sum due at the end of three years to come, find what it will be worth in ready money, by diminifing it according to the sourteenth Rule of this Chapter, so you will find \$300 l. for the ready money equivalent to the said 6312,3848 l, due at the Bb 2

Intereft. Appendix.

178 end of three years, which ready money 5300 1. being fubrracted from the faid 6312.3848 /. leaves(as before) 1012.38481. for the prefent worth of the faid Amuity of 378.743088 1. to continue three years; compound invereft being allowed at 6 per centum, per amumo, ror rana mond ni bas, bas eresy which particular prefeat values being added toge-

The reason of the latter Rule.

goss i payable at the end It will not be difficult to apprehend that if 6312:3848 1 ready money be put forth as a Principal at interest upon interest, it with at three years end be augmented unto an Aggregate or fum compos'd of thefe three numbers, to wir, the faid Principal 63 12.3848; the fum of the annual simple interests of that Principal, and the utmost improvement of those simple interests by interest upon interest : And because (by the operation aforegoing) 5300 L ready money (part of the faidbeady money 63 12 3848 L) will at three years end be augmented unto 63 12.3848 1. part of the faid Aggregate, there fore 1012.3848 1. the complement or remaining part of the faid ready money 63 12 3848 1 must heceffarily be augmented unto the complement or cemaining part of the faid Aggregate, which remaining part last mentioned is composed of the sum of the aforefaid simple interests, and of their utmost improvement at interest upon interest, that is, the faid remainder is the utmost improvement of an Annuity of 378.743088 / to continue three years, compound interest being allowed at 6 per centum, Chapter for you will find \$300 L for the . munning ney equivalent to she faid 6312,3868 . Buc at the

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The Construction of the following Table VI.

Upon the aforesaid grounds the following Fable VI. is calculated, to shew how much ready money as Annuity of one pound to continue any number of years under 31. and payable at yearly payments, is worth, upon a computation of combound interest at any of the rates per censum, mentioned at the head of the faid Table. But the faid Table VI may more easily be composed by the help of the preceding Table V. in this manner, vie the first number in every of the Columns fexcept the Column of years) in the following Table VI is the ame with the first number in the like Columns repectively in the preceding Table V. the fecond number in each of the faid Columns of the fixth Table is the fum of the first and second numbers in the respective Columns of the fixth Table; the third number in the faid Columns of the fifth Fable is the fum of the first, second and third numbers in the respective Columns of the fifth Table : Or yet more easify thus, the third number in the fixth Table, Is composed of the third in the fifth Table, and of the second in the fixth; the fourth number n the fixth. Table is composed of the fourth in the fifth and of the third in the fixth; the like is to be understood of the rest. But you are to observe that according to this way of composing the fixth Table by Addition, the numbers in the fifth Table must be continued to more places then are there exprest, to prevent error arising by the addition of defective Decimal fractions.

B b 4

Table

31, and payable by yearly payments, compound interest being computed at any of these rates, to wit, 4, 5, 6, 7, 8, 9, 10, 11, and 12 per centum, per annum. 7.36668 6.98186 6.62816 1224 9.10791 8.55947 8.06068 7.60608 7.19087 6.81086 bich sheweth the present worth of one pound. Annuity, to continue any term of years under 7. 72173 7.36008 7.02358 6.71008 6.41765 6.14456 5.88923 5.65022 8558 11.73553 1.71252 1.6900 2.77509 2.72324 2.67301 2.62431 2.57709 2.53129 2.48685 2.44371 2.4018 1.389285.206365.032954.868414.712194.5637 8.30641 7.88687 7.49867 7.13896 6.80519 6.49506 6.20651 5.9376 , 10782 6.80169 6.51523 16.24688 5.99524 5.75901 5.53704 5.3282 8384 7.94268 7.53607 7.16072 6.813696.49235 6.1943 .24213 5.07569 4.91732 4.76653 4.62287 4.485914.35526 4.23053 4.1114 4.451824.22047 4.212364.10019 3.992703.88965 3.79078 3.69589 3.604 5.97129 5.74663 5.53481 5.33492 5.146124.967 3.62989 3.84595 3.465 10 3.38721 3.31212 3.23971 3.16986 3.10244 3.037 9.98964 9.39357 8.85268 8.357657.903777 48690 7.10335 6.74987 6.42 60606 7.78614 191743 1.88509 1.85941 1.83339 1.80801 1.78326 1.75911 .92592 9.89864 9.29498 8.7 5.786375.58239 \$ 6.73274 0.46321 6.20979 .94339 0 8507 8.86325 8.3 .95238 8.11089 7604 Years.

dix.

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The use of the preceding Table VI.

The use of the faid fixth Table will appear by the manner of solving these two subsequent queflions, viz.

Quef. 1. What is the present worth of an Annulty or rent of 56 t. per annum, payable by yearly payments for 21 years, accompting interest upon interest at the rate of 6 per centum, per amum? Answer, 658 1.15 s: 9 d. wery near, the found out; In the fourth Column of the preceding Table VI. under the figure 6 at the head, and right against 21 years, I find 11.76407, which thews that an Annuity of 1 l. payable by yearly payments for 21 years, is worth in prefent money 11.76407 l. (or 111.45 5.3 d. if. and fomewhat more) intereft upon interest being computed on both fides at the rate of 6 per centum, per annum; therefore multiplying the faid tabular number 11.76407 by 56, (56 becanfe the Annuity propounded is 56 pound) the product (according to the second rule of the 26th. Chapter of the preceding Book) will be found to be 658.787, &c. that is 6581. 15 s. 9 d. very near; Wherefore I conclude that the Anfwer of the question is 658 1, 15 s. od. view the following operations

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Queft. 2. What is the prefent worth of an anmual rent of 45 l. payable by yearly payments for 21 years, interest upon interest being computed at 10 per centum, per anunm? Answ. 389 1. 3 s. 10 d. very near ; for in the Column of 10 per centum, in the faid fixth Table, right against 21 years, and under 10 at the head I find this number 8.64869; which thews that at no per centum, compound in teneft, an Annuity or rent of 1 & payable by yearly payments for 21 years, is worth in ready money 8. 64869 l. that 18 l. 12 s. 11 d. 3 f. therefore multiplying the faid tabular number 8.64869, by 435 (the rent propounded) the product will be 389.191 +, that is 6897.3 .. 10 d. very near, which is the Answer of the Queftion. 149 001 there Annuity when money was

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right was in the Column of 19 per real and and an arms right are real arms will discover \$2,626.4

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To the same manner the numbers in the other Columns of Table VI, are to be used.

Moreover

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race to be allowed in houses the Leafens

Moreover the numbers in the faid fixth Table will

at first light shew how many years purchase an Annuity to continue any number of years under 31 is worth, to be sold for present money, compound interest being comits worth.

Trafe for years ney, compound interest being comits worth.

faid rates 4, 5, 6, 7, 8, 9, 10, 11 and 12 per cautum: fo if you defire to know how many years purchase an Annuity issuing out of Lands for 21 years, to begin presently, is worth, if it were to be fold for ready money, when the current rate of interest is 6 per centum : Seek in the first Column of Table VI. for 21 years, and carry your eye from thence equidiftant to the head-line of the Table till you come under 6, which (as before hath been faid) fignifies 6 per centum. So in the fourth Column you will find 11.76407, whereof you need only consider 11.76, which shews that the said Annuity is worth 11 years purchase, (or it times one years rent whatever it be) and 76 parts of one years purchase divided into 100 pares, or 112 years purchase and : little more. The fame Annuity when money was at 8 per centum was worth 10 years purchase and about i part of a years purchase more, as the number in the Column of 10 per centum right against 21 years will discover.

In like manner supposing 10 per centum to be a sit rate to be allowed in the valuation of Leases of houses, the Lease of a house for 21 years will be found by the said Table to be worth 8 years purchase and 64 parts of a years purchase, or 8 years purchase

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purchase and an half, and half a quarter of a years purchase, and somewhat more; But note here, that in valuing of Leases, the rate per centum is to be set higher or lower according to the goodness of the thing leased, and the certainty or uncertainty of the rent.

XVI. When a fum of money is propounded,

and it is required to know what Annuity (to continue any number of the puryears, and according to any given rate) that fum will buy, you may prefuppose at pleasure an Annuity for the term of years propounded, and find the value

the term of years propounded, and find the value of that Annuity in ready money (according to the fifteenth Rule aforegoing) at the rate assigned;

then will the proportion be as followeth;

As the value found is in proportion to the supposed Annuity: so is the sum of money propounded, to the Annuity required.

So if it be required to find what Annuity to begin presently, and to continue 3 years, 500 % in present money will purchase, compound interest being computed at 6 per centum, per annum: The

Answer will be 187 l. 1 s. 1 d. very near.

For presupposing an Annuity at pleasure, to wit, 378.743088 1, payable yearly for 3 years, the walue thereof in present money will (by the fifteenth Rule of this Chapter) be found to be 1012.3848 1. Therefore by the Rule of Proportion, say,

1012.3848 . 378,743088 :: 500 . 187,054 That

That is to fay, if 1012.3848 1. in ready money will buy an Annuity of 378.743088 4 (to continue three years) then 500 % in present money will purchase an Annuity (to continue the same term of years, and at the fame rate of interest) of 187 054. &c. that is 187 l. 1 s. I d. very near, and to youing

The Construction of the following is has Table Vijauminos of yair

Upon this ground the following Table VII. is calculated to fliew what Annuity (to continue any term of years under 31, and at any rate of interest mentioned at the head of that Table) one pound will purchase, by which Table, and by the help of Multiplication, questions concerning the purchase of Annuities, Rents or Pensions, by any sum of ready money propounded, may be refolved without confiderable error. But a more ready way to make the faid Table VII. may be this following, viz.

Forasmuch as it is evident by the construction of the third Table aforegoing, that one pound ready money is equivalent unto 1.06 %. payable at the end of a year to come, at the rate of 6 per cemum, per annum; therefore this 1 00 is to be the first number in the Column intituled 6 per centum in the Subsequent Table VII. Again, the present value of One pound Annuity to continue two years at the faid rate will be found by the preceding Table VI. to be near 1.83339 %. Therefore by the Rule of

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1,83339 . 1 :: 1 . 94543,&c.

That is, if 1,83339 1. ready money will purchase an Annuity of 1 1. (to continue two years:) what Amounty to continue the same time will I L in present money purchase? Answer, an Annuity of . 54543 1. that is 10 s. 11 d. very near, to continue two years; therefore the faid Decimal 54543 1, is to be placed as the fecond number in the fourth Column of the Subsequent Table VII. Hence it follows, that if 1 or unity be divided by every one of the numbers in all the Columns of Table VI. except the first Column of years, the quotients will give the respective numbers to be placed in the like Columns of the following Table VII. In which operation it will be requisite, that the numbers in the preceding Table VI. be continued to more places then are there exprest, to prevent error that will arise by adding of defecive decimals.

Table

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Years.

14 .09466 .1010. 10758 .11434 .12129 .12843 .13574 .14524 .17524 .1582 .236994 .09634 .10296 .10079 .11682 .12405 .13147 .13906 .14682 .

Chap.	11					1	nt	ere	Jt.						3	09
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eceding Ta	6 -	.12029	.11704	11421	.11173	10954	192011	.10590	.10438	.10302	.1018c	10001.	.09973	\$8860.	20800.	.09733
the prece	8	11298	109651	.1 6670	10412	10184	.09983	.09803	.09642	.09497	.09367	.0925c	.09144	84060.	19680	.08882
lation of	.7.	10585	10242	.09941	54960.	.09439	.09228	00000	.08871	812800	.08581	.08456	.08342	.08239	.08144	85080.
A continuation	9	\$6860.	.09544	.09235	.08962	81480	.08500	,08304	.08127	19640	.07822	.076	69570.	.07459	.07357	.07264
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d a M	4	18880.	08219	66820	07613	07388	.07128	61690	06739	,06655	10490.	.06256	.06123	.c6001	.c5887	05783
Yea	-	91		18	61	20	2.1	22	23	24	25	92	27	58	50	30

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The

The use of the preceding Table VII.

Queft. 1. What Annuity or yearly rent iffuing out of Lands, to begin presently, and to continue 14 years, will 320 %. purchafe, compound interest being reckoned on both fides, at the rate of 6 per centum, per annum? Anfw. 341.8 s. 6 d. very near, which is thus found out, viz. In the fourth Column of the preceding Table VII. under 6 at the head of that Column, and right against 14 years you will find this decimal 10758, which thews that 11. ready money will purchase an Annuity of .10758 1. (that is 2 1. 1 d. 2 f. t) therefore multiplying the faid decimal .10758 by the faid 320; the product (according to the fecond Rule of the 26th. Chapter of the preceding Book) will be found to be 34.425, &c. that is 34 1. 8 s. 6 d. very near, which is the Answer of the question.

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34 42560

In like manner, if 10 per centum be thought a fit rate of interest to be allowed in purchasing Lease of houses, 500 l. will buy a present yearly rent of 63 l. 18 s. 1 d. payable for 16 years out of a house. For underneath 10 at the head of the 8th. Column, and right against 16 years, (in the preceding Table VII) you will find this decimal .12781, which be-

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ing multiplyed by 500, (the number of pounds propounded to purchase the Lease) the product will be found to be 63.90500, that is, 63 1.18 s.1 d.t as by the subsequent operation is manifest.

> 1 :.,12781 :: 500 . (63.905 500

63 90500

XVII. Upon the same foundations which have been laid in the 12, 13, 14, 15 and 16 Rules of this Chapter, for the making of Tables which respect yearly payments; Tables may be made for half yearly and quarterly payments,

The making of Tables for balf yearly and quarterly payments.

the interest of 100 %. for year, and

likewise for year being first agreed upon : For if we suppose that at the rate of 61. for 1001. for a year, the interest of 100 l.for - year is 3 l.the numbers 100 and 103 are to be used in the same manner to calculate Tables for half yearly payments, as the numbers 100 and 106 have been before used to form Tables for yearly payments. But if at the rate of 6 per centum, per annum, the interest of 100 l. for ' year ought to be fuch, that being added to the faid principal 100 l. and the whole put forth at interest for the next half year, at the faid rate, the fum then due (to wit, at the years end) must exa-Aly amount unto 106 l. In this case a Geometrical mean proportional number between the extreams 100 and 106 must be fought, which mean will (by the following 18. Rule) be found to be near 102 956301 t. And then the numbers 100 and 102.956301, &c. are to be used inftead of the Cc 2 num -

Appendix numbers 100 and 106 in manner aforesaid. In like manner, if it be supposed that at the rate of 6 per centum, per annum, the interest of 100 l. for - year is 1 l. 10 s. or 1.5 l. the numbers 100 and 101.4 are to be used for the calculating of Tables for quarterly payments, in the same manner as the numbers 100 and 106 for yearly payments. But if at the rate of 6 per centum, per annum, the interest of 100 l. for - year ought to be fuch, that being added to the faid 100 l. and the whole put forth at the same rate of interest for the next - year, and in that manner for the third and fourth quarters, and that the fum due at the years end must exactly amount unto 106%. In this case a series or rank of five numbers in Geometrical proportion continued must be considered, viz. the principal 100 1. (which is the lesser of the two extream proportionals) the three fums (composed of principal and interest) due at the end of the first, second, and third quarters of the year, (which are the three mean proportionals) and 1061. due at the years end, (which is the greater of the two extream proportionals;) now between the said extreams 100 and 106, the first (to wit the leaft) of the faid three mean proportionals is to be fought, which (by the tollowing 20thRule of this Chapter) will be found to be near 101.4673 t. And then the numbers 100 and 101.4673, &c. are to be used instead of the numbers 100 and 106 in manner aforesaid.

XVIII. Two numbers being given to find a Ge-

To find a Geometrical mean proportional number betrucen truo numbers given.

ometrical mean proportional between them; multiply the two given numbers one by the other, and extract the square

root of the product, fo is fuch square root the mean proportional fought: for example, if 8 and 18 are two numbers given, and it is required to find a mean number Geometrically proportional between them, multiply 18 by 8, fo is the product 144, whose square root is 12 for the mean proportional fought; fo that 8, 12 and 18, are three numbers in Geometrical proportion continued, viz. As 8 is in proportion to 12, fo is 12 to 18. In like manner a Geometrical mean proportional between the extreams 100 and 106 will be found near 102.956301 t.

XIX. Two numbers being given, to find the first of two Geometrical mean proportional numbers between the extreams given: multiply the square of the leffer extream by the greater, and extract the cube root of the product, fo is fuch cube-root the leffer of the two mean proportionals required : for example, if 8 and 27 are affigned

To find the first of two Geometrical mean proportional numbers between two extream numbers given. .

for two extreams, the leffer mean will be found 12. for according to the rule, the square of 8 the leffer extream is 64, which being multiplyed by 27 (the greater extre m) produceth 1728, whose cuberoot is 12 the leffer mean fought, then may the greater mean be found more easily by the Rule of Three, for 8 . 12 :: 12 . 18, fo that 12 and 18 are two means Geometrically proportional between the extreams 8 and 27, viz. thefe four numbers are in Geometrical proportion continued, to wit, 8 . 12 . 18 and 27.

To find the first of three Geometrical mean proportionals between suro extream numbers given.

XX. Two numbers being given, to find the first of three Geometrical mean proportionals between the extreams given; multiply the cube of the lesser extream by the greater; and extract the Biquadrate root of the product, so is such Biquadrate root

the first (to wit, the least) of the three mean proportionals required: for example, if 2 and 32 are two extreams given, the first and least of three Geometrical mean proportionals will be found to be 4; for (according to the Rule) the cube of 2 (the lesser extream given) is 8, which being multiplied by 32 (the greater extream) produceth 256, the Biquadrate roos whereof being extracted (according to the 29 Rule of the 33 Chapter of the preceding Treasife) gives 4 for the first and least of the three means fought, the other means may be easily found by the Rule of Three for,

2 . 4 :: 4 . 8 :: 8 . 16 :: 16 . 32

So that these five numbers will appear to be in Geometrical proportion continued, to wit,

2 . 4 . 8 . 16 . 32.

In like manner the first and least of three Geometrical mean proportionals between the extreams 100 and 106, will be found to be near 101 4673, &c. Thus have I shewed the most easie wayes (raised from clear grounds) to make Tables for the resolution of the usual questions which depend upon the computation of interest, by the help of Multiplication only.

Questions

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will pred of 2 read Questions to exercise the precedent Tables, with their nse in solving Questions of the same nature when the number of years exceeds 30.

Queft. 1. If the Lease of a house be worth 153 t. Fine, and 16 1. yearly rent, payable yearly for 21 years, and the Leffee be defirous to bring down the Fine to sol, and fo to pay the more Rent, the queftion is what rent the Tenant shall pay, accompting compound interest at the rate of 10 per centum, per

annum? Answer, 27 l. 18 s. 13 d. near.

First find the difference between the Fines which is 103 1. Then after the manner of the examples of the use of the preceding Table VII. feek what Annuity or rent to continue 21 years, 103 1. ready money will purchase at 10 per centum, so will you find 11 1.18 s. 13d. which being added to the old rent 16 l. gives 27 1. 18 s. 13 d. which the Tenant must pay to the end that the Fine may be diminished unto 50 %.

Quest. 2. There is a Lease of certain Lands to be let for 14 years for 250 l. Fine, and 44 l. Rent per annum, payable yearly, but the Tonant is desirous to pay less Rent, viz. 20 pounds per annum, and to give a greater Fine; the question is what Fine ought to be paid to bring down the rent to 20 l.per annum, accompting compound interest, at the rate of 6 per cent. per annum ? Answer, 473 l. 1 s. 7 d.

First find the difference between the Rents, which will be 24 pounds per ann. Then by the help of the preceding Table VI. feek what an Annuity or rent of 24 lper annum, to continue 14 years, is worth in ready money at 6 per centum, per annum; fo will you find Cc 4

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find 223 l. 1 s. 7 d. which being added to the first Fine 250 pounds, gives 473 l. 1 s. 7 d. which the Tenant must pay, to the end the rent may be brought

down to 20 l. per annum.

Quest. 3. There is a Lease of certain Lands worth 32 l. per annum, more than the rent paid to the Lord for it, of which Lease seven years are yet in being, and the Lesse is desirous to take a Lease in reversion for 21 years, to begin when his old Lease is expired, the question is, what sum of money is to be paid for this Lease in reversion, accompting compound interest at the rate of 6 per centum, per annum? Answer, 250 l. 7 s. 2 d. †

First by adding the 7 years of the Lease in being, to the 21 years you would have in reversion after those 7 are expired, the sum is 28. Then by the pre-

ceding Table VI.

The present worth of 1 l. Annuity for 28 years at 6 per centum, compound interest, is	13.40616
Likewise the present worth of 1 1.5	5.58233
Therefore, the difference of those present worths, shall be the present value of 1 l. Annuity for 21 years in reversion after 7 years	7.82383
Which multiplied by 32 (the yearly rent propounded) gives the Answer of the question,	250.36256

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First by the help of the said Table VI. find out how much 32 l. yearly rent for 21 years is worth in ready money, as if the 21 years were to begin presently, at the rate of 6 per centum, which ready money will be found 376.45024 l. Then by Table V. find what 376.45024 l. due at the end of 7 years to come, is worth in ready money; so will it be 250 l. 7 s. 2 d. which agrees with the Answer before found.

Quest. 4. One would bestow 630 l. to purchase a present yearly rent or Annuity of 60 l. to be paid by yearly payments, the question is to know how many years the said Annuity must continue, compound interest at 6 per centum, per annum, being allowed on both sides. Answ. 17 years, and 23 dayes,

very near.

First I divide 630 by 60, so the quotient will be 10.5, which shews that 10 years purchase and an half are given for the Annuity; then searching for 10.5 in Table VI. in the Column of 6 per cent. I find it not exactly, but the nearest less then it, is 10.47725, standing right against 17 years, and the next greater than 10.5 is 10.82760 which is placed against 18 years, whence I inser that the Annuity must continue 17 years and more, yet, less then 18 years. Now the proportional part of a year to be added to 17 years, may be found out near enough for use, thus, viz. subtract the said lesser tabular number 10.47725 from the greater 10,82760, so the remainder will be found .35035: Also subtracting the said 10.47725 from 10.5 (the quoti-

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ent first found the remainder will be .02275; then fay by the rule of three in decimals, as .35035 the greater remainder is to :02275 the leffer ; fo is 1 year (the difference between 17 and 18 years) to .0649 parts of a year, or 23 dayes +) as will appear by the fourth Rule of the 26 Chapter of the preceding Book) therefore the number of years fought by the question is 17 years, 23 dayes.

Quest. 5. If an Annuity of 96 l. payable by yearly payments for 14 years be fold for 826 1. what rate of interest per centum, is implied in that bargain?

Anfw. 71.55.7-d. near.

First, dividing 826 by 96, the quotient is 8.60416, which fliews how many years purchase was given for the Annuity; then fearthing for 8,60416 in-Table VI. in a right line passing from 14 years, equidiffant to the head line of the Table, I find it not exactly, but the nearest less than it, is 8.24423 (which stands in the Column of 8 per cent.) and the nearest greater is 8.74546, (which stands in the Column of 7 per cent.) whence I infer, that the rate of interest required is between 7 and 8 per cent. and the proportional part of 1 l.to be added to 7 l. may be found out near enough for practice thus, viz. Subtract the faid leffer tabular number 8.24423 from the greater 8.74546, the remainder will be .50123. Alfo fubtract 8.60416 (the quotient firft found) from the faid greater tabular number 8.74546, fo the remainder will be 14130; then fay by the Rule of Three in decimals, as for23 the vide 1 greater remainder, (or difference between the two cent.) tabular numbers) is to .14130 the leffer remainother. der ; fo is t !. (the difference between 7 per cent. one to and 8 per cent.) to .2819, &c. or 5 . 7 d. 2f. which near . added

added to 7 l. gives 7 l. 5 s.7 d.2 f. which is near the

rate of interest per cent. required.

Queft. 6. If a years rent (or one years purchafe) be paid as a Fine, for renewing or adding 7 years to 14 years yet to come of an old Leafe for 21 years, and accordingly a new Leafe be taken for 21 years, to begin prefently, (which proportion is ordinarily observed by Bishops, Deans, and Chapters, Heads and Fellows of Colledges in letting Leafes of their Lands) what rate of interest per centum is implied in that Agreement? Answ. 11 1. 11 s. 8 d. 1f.

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To folve this Question, first I fearch in the preceding Table VI. to find out two numbers fo feated in some one Column of interest, that one of them may stand right against 14 years, and the other against 21 years; and so qualified that the difference between them may be exactly 1 or unity : but not finding any two numbers precifely answering those conditions, I take those numbers that come nearest, which will be found in the Columns of 11 and 12 per cent. for the difference between the numbers 6.98186 and 8.07507 which stand in the Column of 11 per centum, right against 14 years and 21 years is 1.09321 which exceeds 1 (that is 1 years purchase) by .09321; Also the difference between 6.62816 and 7.56200 which stand in the Column of 12 per cent.right against 14 years and 21 years is .93384, which wants .06616 of 1; therefore I dine vide 1 l. (the difference between 11 l. and 12 l. per o cent.) into two parts, in such proportion one to the other, as the said decimals .09321 and .06616 are one to the other, fo I find the faid parts of 1 1. to be th near . 5848 and .4151 5 or 11 s. 8 d. 1 f.t, and 8 s.

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3 d. 2f. +; the former of which being added to 11 per centum, or the latter being subtracted from 12 l. per cent. gives 12.5848 l.or 11/111.8 d.1f.+, which is very near the rate of interest required by the question.

Quest. 7. What is the present worth of 1 l. per ann, payable yearly for 10 years, compound interest being computed at the rate of 11. 5848 l. per cent. Answ. 5 l. 15 s. 0 d. very near, which is found out by the help of the preceding Table VI. in this manner, viz.

The tabular number for 10 years }	5.88923	
The tabular number for 10 years ?	5.65022	
Their difference is	0.23001	۰

Then say by the Rule of Three in decimals, as 1 l. (the difference between 11 and 12 per cent.) is to .5848 l. (to wit, the decimal by which the given rate in the question exceeds 11 per cent.) so is .23901 (the difference found out as above) to .13977 †, which being subtracted from 5.88923 (the greater of the two tabular numbers above mentioned) there will remain 5.74946, or 5 l. 15 s. od. which is near the present worth of one pound yearly rent to continue 10 years, at the proposed rate of 11.5848 l. per centum.

After the same manner the present worth of 1 l. yearly rent payable for 21 years, at the same rate of interest, will be found to be 7.77503 l. or 7 l. 15 s. 6 d. very near, from which if you subtract 5.74946 (being the afore-mentioned present worth of 1 l. yearly rent for 10 years) there will remain 2.02557

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or 2 l.o s. 6 d. which is near the present worth of a Lease of 1 l. rent per annum, for 11 years in reversion, to begin after 10 years yet to come in a Lease are expired; Hence it is evident, that if a Tenant to a Colledge hath 10 years yet to come in a Lease, at 1 l. rent per annum, and desires to have 11 years resewed, or added to those 10, and so take a new Lease for 21 years, to begin presently at the same rent, he must give 2 l. 0 s. 6 d. or 2 years purchase and \(\frac{1}{40}\) part of a years purchase, very near, (according to the fundamental proportion before assumed in the sixth question.) The like may be done for any other term of years under 30, by the help of the said Table VI.

But yet by a Table calculated purposely for the said rate of 11.5848 l. per centum, (according to the fifteenth

Concerning the renewing of a Colledge Leafe of Lands.

Rule of this Chapter) questions of the same kind with the two last, may be more easily answered, and therefore (for that they come often in practice) I shall here insert such a Table, as I find it ready calculated to my hand by Doctor Newton, in his Scale of Interest lately published, which Table is to be used in every respect like to the preceding Table VI. and will be very ready and useful, for the proportioning of Fines, in the renewing of Leases held from Cathedral Churches and Colledges, as will be manifest by the manner of solving the two following questions.

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Queft. 8. If a Colledge-Tenant hath 7 years yet to come or unspent in a Leafe of lands for 21 years, at 1 /. yearly rent, and defires to have 14 years renewed or added to those 7 years, and fo to take a new Leafe for 21 years to begin prefently, what must be pay for a Fine? Anfw. 31.35.0d.

The rule for finding out the answer of the question proposed, and such like, is

this; viz.

From 7.77507 the number which answers to 21 years in this Table VIII.) Subtract alwayes the tabular number which belongs to the number of years to come or unspent in the old Leafe, so the remainder will shew what Fine must be paid for the years to be renewed or added, to make those unspent years in the old Leafe, to be 21 years compleat again, at I l. yearly Bent.

So to folve the question proposed.

TABLE VIII

Shewing the prefent worth of one pound Annuity , for an number of years under 22, at the rate of 11 1.11 3.8 d. 1 3 f. per ceneum compound intereft.

Tears	present worth
ī	0.90034
2	1.69938
3	2.41922
4	3.06438
5	3.64262
6	4.16088
7	4.62540
8	5.04176
9	5.41496
10	5.74948
11	6.04934
12	6.31819
13	6.55907
14	6.77507
15	6.96868
16	7.14226
17	7.29786
18	7.43737
19	7.56243
20	7.67455
21	7.77507
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yearly rent for 21 years, which is -	7-77507
Subtract the present worth of the fame rent for 7 years, (that were unspent in the old Lease.)	4,62540
And there will remain the Fine	3.14967

And there will remain the Fine 3.14967

That is to fay, 3.14967 L. or 3 L.3 s. o.d. (very near) must be paid as a Fine, for renewing or adding 14 years to 7 years, that were unspent in the old Lease, the yearly rent being 1 L. Also the said 3.14967 shows that such a renewal is worth 3 years purchase, and near 15/100 parts of a years purchase, (whatever the rent be.)

Quest. 9. If a Tenant that hath 17 years yet to come, in a Lease of lands held of a Colledge for 21 years, at 50 l. yearly rent, be desirous to renew 4 years, and so make those 17 years to be 21 years compleat again, at the same rent, what must be give for a fine? Answ. 23 l. 17 s. 2 d. 1 f. For, according

to the rule before given,

From the present worth of 1 1. }	7.77507
Subtract the present worth of the	06
fame rent for 17 years (that were un-	7.29786
And there will remain————————————————————————————————————	0.47721
The Product will be the Fine fought, to wit, 23 1, 17 s. 2 d. 1 f.	23 86050

Questions

Questions of this nature may be readily solved without the loss of one fixteenth part of a years Purchase by the help of the following Table IX, which I have drawn from the foregoing Table VIII, for the benefit of fuch as understand not Decimal fractions; for example, if a Colledge-Tenant desireth to have ten years added to eleven years that are yet to come or unspent in a Leafe of lands that he may have a new Leafe for the term of 21 years to begin prefently, he mult give for a Fine, one years Purchase and two quarters of a years Purchase, and three quarters of a quarter of a years Purchale, viz. one years rent, and half a years rent, and three quarters of a quarter of a years rent: Supposing then the rent to be 48 1. per annum, the Fine may be computed thus.

* * * * * * * * * * * * * * * * * * *	a chit	lad street	L 3.	d.
One y	ears rent is	F107 F10 4 4 2 5	-48 : 00	:00
Half :	years ren	t is-	-24 : 00	00:00
Three	quarters of	a quarter.	9:00	00:00
of a year	s rent is-	5 1 7 7 7	Section 5.	477 2 2
The fu	m is the Fine	required	-81:00	: 00

Whence it appears that the Tenant must give 81 1. as a Fine, for adding of 10 years to 11 years that were unexpired in his old Leafe, to the end he may

have a new Leafe for 21 years in being. A

In like manner the Fine for renewing or adding feven years to fourteen years that are unspent in a Leafe of lands to the end there may be a new Leafe for 21 years in being, is valued at one years Purchase precisely, which is the Fundamental proportion assumed in calculating the faid Table-VIII, as before was faid.

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The like may be done for renewing any other term of years under 21, at any rent propofed

But because it may sometimes happen, that the number of years in questions belong-Of finding out ing to the preceding 3, 4, 5, 6 and sabular num. 7 Tables may exceed 30, 1 shall by bers for any the five following questions shew sorm of years how by the help of those Tables, the akeve 30. answer to any question of that na-

ture may be found out near the truth, when the term of years is above 30.

Queft. 10. If 340 l. be put forth at 4 per centum compound interest, and both principal and interest be forborn until the end of 45 years, what will then be due? Answer, 1986 l. very near.

To resolve this question and the like observe this rule, viz. First make choice of any two fuch numbers that if they be added together will make the number of years proposed in the question, as 17 and 28; or 15 and 30, each of which pairs make 45, then looking into Table III. in the Column belonging to 4 per centum, you will find right against 17 and 28 years these numbers, 1.94790 and 2.99870 which being multiplyed one by the other will produce 5.84116 t or 5 1. 16 10 d. which shall be the increase of 11. forborn 45 years at 4 per centum, compound interest, therefore multiplying the faid 5.84116 by 340, the product will give 1985.994, &c. or 1986 l. very near for the Answer of the question.

The reason of the said Rule will be manifest by is I. this Theorem, viz. If there be a rank of numbers appe in Geometrical proportion continued, beginning that

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with 1 or unity, 25 1, 2, 4, 8, 16, 32, 64, 128, &c Alfo if the first term i be cast away, and over or under all the rest of the terms there be placed another rank of numbers, beginning at 1 and proceeding according to the natural order of numbers. as 1, 2, 3, 4, 5, 6, 7, &c. which may be called the Indices of those in the first rank, after the first term is cast away . I fay if any two of those remaining Geometrical proportionals be multiplyed one by the other, the product shall be a proportional, correspondent to that Index which is equal to the fum of the Indices answering to the two proportionals that were multiplyed one by the other.

Proport. 2 . 4 . 8 . 16 . 32 . 64 1380 bas Indices 1 . 2 . 3 . 4 . d 5 . 6 h 7 100 1100

So if 4 and 32, which are the fecond and fifth proportionals in the upper rank, be multiplyed airs one by the other, the product is 128, which hall Co- be the seventh proportional, because the sum of ght the Indices 2 and 5, which answer to the faid 4 the the Indices 3 and 4 is 7, therefore if the third and hich fourth proportionals, to wit, & and 16, be multiat 4 plyed one by the other, the product shall also give the seventh proportional 128, Now for as much as will the numbers in every one of the Columns, except the the first Column of years in the preceding Table lis 1, but tis excluded out of the faid Columns, as bers appears by the Construction of that Table, and for ning that the numbers of years 1, 2, 3, 4, 5, &c. are placed

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placed at Indices shewing the order or feat of those proportionals inserted in the Columns, therefore the rule before given for continuing that Table to

any number of years is manifelt. dans he lake

Quest. 11. If one pound be due of payable 50 years hence, what is it worth in ready money, by rebating at 5 per centum, per annum, compound interest ? Answ. 08720, &c. or rs. 9 d. t which is found out by the help of Table V. in the same manner as the Answer to the last Question, (respect being had to the second and third rules of the 26th. Chapter of the preceding Book concerning

the multiplication of decimal fractions.)

Queft. 12. If an Annuity of one pound payable yearly for 40 years, be all forborn until the end of that term, what will it then amount unto, compound interest being computed at 5 per centum, per annum? Anfw. 1201. 16 s. o d. thus found out; First, according to the second way of calculating the fourth Table in the thirteenth Section of this Chapter, find out a Principal which may have fuch proportion to the proposed Annuity 1 1. as 100 h. hath to 3, faying if \$1. interest bath 100 1. for a principal, what principal must i ?! interest have? Answer, 201. Secondly, feek (after the manner of the preceding tenth question) what 20%, will be augmented unto being forborn 40 years, at the face of 5 per centum, per annum, compound interest, fo you will find 140.798 +, from which fubtra Wing the faid principal 20 1. the remainder will be \$201798+, or 120 1.16 s. which is the answer of the queftion.

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ney, what is it worth, compound interest being computed on both fides at 6 per centum, per annum ? Answer, 141. 1437 9 d. which is found out thus: First, according to the second way of calculating the fixth Table in the fifteenth Section of this Chapter, find out a principal in such proportion to one pound (the proposed Annuity) as 100 is to 6, so will such principal be found 16.66666 +, then after the manner of the preceding eleventh question find out the ready money which is equivalent to 16.66666, due 37 years hence, fo will fuch ready money be found to be 1.92988 + (or 1 1. 18 1.7 4.) which being fubtracted from the faid principal 16.66666, the remainder will be 14.73678 +, or 141.14 s 9d. which is the Answer of the question propounded.

Quest. 14. What Annuity payable by yearly payments to continue 37 years will one pound purchase, at 6 per centum, per annum, compound interest? Answ. Ts. 4d. near, which is found out thus; First find out the present worth of one pound Annuity to continue 37 years, which prefent worth (by the last quettion) will be found 14 73678 to Then fay by the Rule of Three, if 14.73678 1. will purchase an Annuity of one pound; (to continue 37 years) what Annuity to continue the same term will Il. purchase? Answ. .06785 +, or 1 s. 4 d. which is the answer of the

question propounded.

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CHAP. VI.

A Demonstration of the Rule of Three, or Rale of Proportion.

7. Toour numbers are faid to be proportionals; when the first containeth the second fo often as the third containeth the fourth ; likewife when the first is fuch part of the fecond, as the third is of the fourth : So thefe numbers following are called proportionals, viz.

That is to fay, 4 times 6 (or 24) is faid to have fuch proportion to 6; as 4 times 9 (or 36) hath tog. In like manner, - of 12 (or 8) hath fuch proportion to 12; as of 15 (or 10) hath to 15.

11. When four numbers are proportionals, the product arising from the multiplication of the two extreams is equal to the product of the two means,

Demonstration.

By the preceding Definition in 1. these four numbers are proportionals, viz.

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The product of the 4 x 6 x 9 second south and two extreams is B x C x D south of orgong

The product of the 6 x 4 x 9 two means is _____ C x B x D

Therefore the Prop, is manifelt,

side la nominajora Likewife.

By the preceding definition these four numbers are proportionals, viz.

2 x 12 . 12 : : 2 x 15 . 15

The product of the 2 x 12 x 15 thinks

The product of the 12 x 2 x 15 two means is _____

But $\frac{1}{3} \times 12 \times 15 = 12 \times \frac{2}{3} \times 15$

Wherefore the propolition is every way pro-

III. From the last proposition ariseth the Rule of Proportion, commonly called the Rule of Three, or Golden Rule, which teacheth by three numbers given to find a fourth proportional number, in this manner, viz. Multiply the second and third numbers mutually one by the other, and divide the product by the first number; so the quotient shall be the fourth proportional number fought, in a direct proportion. This Rule hath been fully exemplified in the 8th, Chapter of the preceding Book, and the truth of the faid Dd 4

faid Rule may be thus demonstrated, vie. Let there be three numbers given to find a fourth in direct proportion, vie. if 24 give 6, what shall 36 give? Or as 24 is in proportion to 6, so is 36 to a fourth proportional number sought, which fourth proportional, (whatsoever it be) we may suppose to be Q, and then these four numbers will be proportionals, vie.

Therefore by the feçond proposition of this Chapter.

24 x Q = 6 x 36 acilioqo 19 211

By the preceding dell'a rion thek

And because if equal plane numbers be severally divided by one and the same number, the quotients will necessarily be equal between themselves, therefore

$$Q_{\cdot} = \frac{6 \times 36}{24}$$

Whereby it is manifest that the fourth proportional number is equal to the quotient that ariseth by dividing the product of the multiplication of the fecond and third proportionals by the first, which was to be proved.

Note, that every Rule of Three inverse may be made a Rule of Three direct, by making the third term the first, and by proceeding sorward to the other two terms; therefore one, and the same demonstration serveth for both rules.

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A Demonstration of the Double Rule of Feb-

He Double Rule of Fellowship, (commonly called the Rule of Fellowship with time) presup-poseth two things, viz. 1. That the particular Stocks of Merchants in company, have continued unequal spaces of time in the common Stock. 2. That at the end of their Partnership, the total gain or loss is to be divided amongst them, in fuch manner, that their shares shall have fuch proportion between themselves, as those sums of interest money have one to another, which at any rate per centum, simple interest onely being computed, might be gained by the particular Stocks, within the respective times of their continuance in the common Stock : Now for the effecting of such a proportional partition, the faid Double Rule of Fellowship gives this direction, viz. Divide the total gain or loss into fuch parts, which shall have the same proportion one to the other, as is between the products arising out of the multiplication of each: particular Stock by its correspondent time.

For Example, suppose two Merchants A and B to be partners in Traffick, for a certain time first agreed

agreed on between them, and that A doth permit his Stock of 1001. to be employed in their joynt Traffick three moneths, and that B forbears his Stock of 50%, eight moneths; I fay (according to the faid Rule of Fellowship with time) what ever the total gain or loss be, that part thereof which belongs to A must have such proportion to the gain or loss of B as 100 x 3 (or 300) hath to 50 x 8 (or 400.) This rule hath been fully exemplified in the 13 Chapter of the preceding Book, and the truth thereof, taking the two premised Suppositions for granted, may be thus demonstrated.

1. Supposing 100 1. (the stock of A.) to gain in moneths any certain fum of money, as two pounds; I feek how much 50 1. (the flock of B) will gain in the fame time, and at the faid rate, fo I find

2 × 50/. for, JOO

4 for,

2. Having found what 50 1. will gain in 3 moneths, I feek how much the faid 50 1. will gain in 8 moneths, at the same rate, and so I find 2 x 50 x 8 100 × 3

3. Thus it appears, that if 100 l. in 3 moneths doth gain 2 1, then 501, in 8 moneths will gain at

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the fame rate $\frac{2 \times 50 \times 8}{100 \times 3}$; fo that the proportion of the gain of A to the gain of B is.

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ths at the 4. If both the terms (to wit, the Antecedent and Con(equent) of the said proportion be severally multiplied by the said Denominator 100 x 3, the products will be in the same proportion with the numbers or terms multiplied, (by 17 è 7. Euclid) viz. the gain of A will be to the gain of B,

As 2 * 100 * 3 is to 2 * 30 * 8

5. Lastly, because 2 (the supposititious gain first assumed) is a Multiplicator as well in the Anteces dent as in the Consequent of the last mentioned proportion, it may be expunged out of both, and so the gain of A. will be to the gain of B. in this proportion (which was to be proved) to wit,

As 100 x 3 is to 50 x 8

GA .. LEGA SCHAP.

the famerate \$ 50 × 8; fo that the proportion

of the rain of A co the gain of B is. CHAP. VIII.

A Demonstration of the Rule of Alligation ban alternate; and the use of the said Rule in the Composition of Medicines.

LIN order to the Demonstration of the faid Rule, I shall premise this Lemma, viz. if the difference of any two numbers given be multiplied by a number affigned, the product will be equal to the difference between the products which arife from the multiplication of those two numbers severally by the number affigned. The ideal of the months

en cantant de l'el mentioned pro-

A. will ite to the prin of B. in this pron Two lines 9rd A C = 10q A

numbers given. B C = 4

Their difference. A B = 10—4 A multiplicator A D = 5 affigned.

Which suppositions, and the Diagram being well viewed, the truth of the faid Lemma will be evident, viz.

AB AB AD=AC × AD, -BC × BE (AD) $10-4 \times 5 = 10 \times 5, -4 \times$

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11. To add the more light to the following Demonstration of the rule of Alligation Actinate. I hall propound a question which properly belongs to the faid rule viz. Suppose a Vintper having Frenchwines at 5 d. the quart, and at 10 d. the quart, would make a mixture ofctbem in fuch manner, that he might fell the mixt quantity at 7 d. the quart, and to make as much money of the mixture, as if he should fell each quantity of wine at its own perce the queltion is to know what proportion the quantities of both forts of wine in the nixture muft bear one to another. Hare according to the Rale of Allivation alternate. I take the differences between the mean price affighed for the mixture, and the two other given prices? and place those differences alternately, vis. the difference between y and to being 3, Twrite 3 against 3, likewife 2 being the difference between 70113 CTO PZ and 5, I write 2 against 10; fo I conclude, that the quantity to be taken of that fort of Wine of 10 d. the quart, must have such proportion to the quantity of & d. the quart; as 2 to 3. That is to fay, it 2 quarts at 10 d, the quan be mixed with 3 quarts at 5 d. the quart, the total faixture 5 quarts being fold at 7 d the quart, will visid as much money as the faid 3 quarts at 5 d. the quart together with the faid 2 quarts at 10 d. the garr ; 26 istevident by the subsequent work.

B-0 | BA-CA = B-C * A

The difference between B and A is B-A. which multiplied by C produceth (is is evident by the Lemma

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From the premisses it appears, that when two things are given to be mixt in fuch manner as the Rule of Alligation alternate requires, the propolition

to be demonstrated will be this namely.

Three numbers A.B.C. being given in fuch fort, that A.is less then B, but greater then C, if the difference between A. and B. be multiplied by C. and the difference between A. and C. be multiplied by B. the fum of those products will be equal to the product arising from the multiplication of A. by the fum of the faid differences.

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	B-C	BA-	CA = I	-C	A

The difference between B and A.is B-A, which multiplied by C produceth (as is evident by the

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Lemma

Chap. VIII. the Rule of Alligation.

Lemma aforegoing in the first Section of this Chapter) CB—CA. Also the difference between A and C is A—C. which multiplied by B produceth BA—BC. Then the sum of those two products is BA—CA, (for † CB and—CB expunge one the other) which sum is manifestly the same with the product arising from the multiplication of A the mean price, by B—C the sum of the aforesaid differences, (to wit, the sum of A—C and B—A) for † A and—A expunge one another.

When more then two things of different prices are given to be mixt as aforefaid, the Demonstration will not be otherwise, for if the sum of every two products arising from the multiplication of two alternate differences by their respective prices, because the sum of the said differences; the sum of all the said products will also be equal to the product of the mean price multiplied by the sum of all the said products will also be equal to the product of the mean price multiplied by the sum of all the differences; as will clearly appear by view of the

subsequent work,

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Moreover, because if equal numbers be severally divided by one and the same number, the quotients will be equal between themselves, therefore from the premisses, this Corollary will arise.

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which furnasties seletly the fance with the

In the Rule of Alligation alternate, if the aggregate of the products ariting from the multiplication of the feveral alternate differences by their respective prices, be divided by the sum of the said differences, the quotient will be equal to the mean price. This may be a proof of any example of the said Rule of Alligation.

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Age more of this in Mr. J. Dee his Mathematical preface, also Tom 2.0f P. Herigon and Master Mores Arithmetick.

I.Medicines and Simples in respect of their qualities are considered in some of these sive wayes, viz. either as they are hot or cold, moist or dry, or as they are temperate; so that such Simples or Medicines which work heat in our bodies are said to be hot, such cold which are the cause

of coldnels, &c.

II. The mean or middle between the extream qualities of Heat and Coldness; also between Drymess and Moisture, is called Temperate or the Tem-

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perature; from which, each of the faid qualities hot, cold, moist and dry, doth differ in four degrees, so that a Medicine or Simple is said to be either temperate, or else hot; cold, moist; or dry, in the first, second,

third or fourth degree.

III. If the numbers 1,2,3,4,5,6,7,8,9, be plated as you fee from A to B, the differences between 5 (the middle number) and the superiour numbers 6,7,8,9, will be 1,2,3,4, which may represent the 4 degrees of the qualities hot and dry, likewise the differences between 5 and the inferiour numbers 4,3,2,1, will be 1,2,3,4, which may represent the 4 degrees of the qualities cold and moist, the temperature represented by 0, being the mean or middle from whence the said degrees do swerve.

B 9 | 4 | Qualities hot 7 | 2 | and dry. 6 | 1 | Temperature. 4 | 1 | Qualities cold 2 | 3 | and moist. A 1 | 4 |

IV. Since the Rule of Alligation alternate requires, that of two things miscible, the one must exceed the Ee mean

mean propounded and the other be lefs, therefore the questions of Alligation in this kind are to be wrought with the numbers in the aforefaid Co. lumn A B, for by them the degrees and qualities are discovered, being placed as you see in the Column adjacent to A B, and for distinction sake, those numbers in the said Column A B, may be called the Indices or Exponents of the degrees, which Indices are to be used in the same manner as the prices of Merchandizes in the questions of Alligation alternate in Chapter 14 of the preceding Book; and therefore those examples may be compared with thefe.

Prop. I.

Having divers Simples whose qualities are known, to make a composition or mixture of them, in such manner that the quality of the Medicine may be some mean amongst the qualities of the simples, and the quantity thereof any quanti-

ty affigned.

Example 1: An Apothecary hath four forts of Simples, A, B, C, D, whose qualities are as followeth, viz. A is hot in the fourth degree, B is hot in the second, C is temperate, and D is cold in the third degree; the question is to know what quantities of each ought to be taken, to make a Medicine, whose quantity may be 12 ounces, and the quality in the first degree of heat? Seek in the aforesaid column A B, for the Indices or exponents of the qualities of the Simples given, viz. for A which is hot in the fourth degree, take 9, for B which is hot in the second, take 7; for C which

which is temperate, take 5; and for D which is cold in the third degree, take 2; that done, rank those numbers in the same manner as the prizes of Merchandizes in the questions of the 14 Chapter, viz. descend from the highest degree of heat unto the temperature, and so proceed downwards to the degrees of cold, fetting 6 the Index or exponent of the mean quality propounded, which is a degree of heat, as common to them all: then by crooked lines or otherwise, connect two such Indices whereof one may be greater than the mean, and the other els, and proceeding according to the Rules of the fourteenth Chapter you will find that to make a Medicine of o ounces, and the quality refulting to be in the first degree of heat, you must take 1 punce of A (being that Simple which was hot in) 4 ounces of B, 3 ounces of C, and 1 ounce f D, as will be manifest by the proof:

aftly, by the Rule of Proportion you may increase the Medicine to the quantity of 12 ounces, and yet the quality to continue in the first degree of heat, ecording to the following operation.

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The quantity assigned 12 ounces.

By other connexions of the qualities, other quantities of each Simple would arise, but that hath been sufficiently manifested in the questions of the

fourteenth Chapter.

Example 2. Suppose there are five Simples, A, B, C, D, E, whose qualities are as followeth viz. A is hot in 3°. B is hot in 2°. C is hot in 1°. D is cold in 1°. E is cold in 3°. and it is required to mix four ounces of B, with such quantities of the rest, that the quality of the Medicin may be temperate?

Degr		WH.	du	The proof.
18-	1	I	A	8 × 1 = 8
(7-)	3	3	B	/ x 3 = 21
)6-	II	I	C	$6 \times 1 = 6$ $4 \times 4 = 16$ $2 \times 2 = 4$
14	3 + 1	4	D	4 × 4 = 16
(3)	2	2	E	20 x 2 = 4

Proce

Proceed as before, so will you find that to make a Medicine of 11 ounces, and the quality of the Form resulting to be temperate, you must take 1 ounce of A, 3 ounces of B, 1 ounce of C, 4 ounces of D, and 2 ounces of E; then fince the quantity of B, in the composition propounded is limited; viz. 4 ounces. find numbers which may be in such proportion to 4 (the quantity of B' affigned) as the numbers 1, 1, 4, 2, (the quantities of A, C, D, E, in the aforesaid Composition of 11 ounces) are unto 3, (the quantity of B in the said Composition) in manner following:

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$$1\frac{1}{3}$$
 of A.
3 . 1 :: 4 . $1\frac{1}{3}$ of C. to be mixed with
3 . 4 :: 4 . $5\frac{1}{3}$ of D. 4 ounces of B.
3 . 2 :: 4 . $2\frac{1}{3}$ of E.

Prop. 11.

A Medicine being compounded of divers Simples whose qualities and quantities are known, to find the degree of the Form resulting, viz the exact temperament of the Medicine.

Example 1. Suppose a Medicine to be compounded of two Simples, viz. 6 ounces of Bhot in 4°. and 3 ounces of Chot in 3º, and it is required to find the temperament of the Medicine, viz. the de-Prod gree and quality resulting from such mixture? Seek in the aforesaid Column AB for the Indices of the respective degrees, and qualities of the Simples given, and dispose them orderly in ranks right against their respective quantities, then multiply each Index by its respective quantity, and divide the sum of the products by the sum of the quantities, so will the Quotient be the Index of the degree and quality of the Medicine;

 $9 \times 6 = 34$ $8 \times 3 = 24$ $9) 78 (8 \frac{2}{3})$

So in the said example, the Quotient will be found 8 3, which is the Index of 3 2 degrees of heat, and therefore the said Medicine is hot in 3 2 de

grees.

Forasmuch as any two quantities miscible according to the rule of Alligation alternate, are in such proportion one to the other, as the respective alternate differences between the mean quality of the mixture and the qualities correspondent unto the said quantities, the demonstration of the aforesaid rule will be manifest by the Corollary aforegoing in this Chapter.

Example 2. Suppose a Medicine to be compounded of 4 Simples, whose qualities and quantities are known, viz. 2 ounces of A hot in 3°. 3 ounces of B hot in 2°. 4 ounces of C temperate, and ounces of D cold in 4°. and let it be required to

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find the mean quality refulting from such mixture. According to the aforesaid rule, I multiply each Index by its respective quantity, and divide the sum of the products by the sum of the quantities, so the quotient is $4\frac{3}{7}$, which is the Index of $\frac{4}{7}$ degrees of cold, (for the difference between 5 the Index of the temperature, and $4\frac{3}{7}$ the Index found, is $\frac{4}{7}$ degrees of cold) which is the quality of the said Medicine.

Example 3. Suppose a Medicine to be compounded of several Simples, whose qualities and quantities are as followeth, viz. 4 ounces of a Simple which is cold in 2°. and moist in 1°. 3 ounces hot in 3°. and (in respect of dryness and moisture) temperate; 3 ounces hot in 2°. and dry in 2°. 6 ounces hot in 1°. and moist in 4°. 4 ounces cold in 3°. and moist in 2°. the question is to know the temper resulting?

In the resolution of this question there must be two distinct operations, each of them like to that

in the last example, viz.

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i. Find

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ipounintities ounces and s red to 1. Find in the fame manner as before, the degree and quality refulting from the commixture of the qualities hot and cold, so will you find $5\frac{-7}{22}$ which is the Index of $-\frac{7}{2}$ degrees of heat (for the difference between 5 the Index of the temperature and $5\frac{-7}{22}$ the Index found, is $-\frac{7}{22}$ degrees of heat.)

			10 81 1 13		
Oun.	Prod.	Ind.	Оши.	Prod.	1 31
3 × 4 =	12.	4 ×	4 =	16	
8 × 5 =	40	5 ×	5 =	25	
7 × 3 =	21	7 ×	3 =	21	
6 × 6 =	36		6 =		
2 × 4 =	8	3 ×	4 =	12	
				-	
22)	117 (5 7	7 ::2	22)	80 (3	-7 1X

2. Find in the same manner, the temper resulting from the mixture of the qualities dry and moist; so will you find 3—7 which is the Index of 1—4 degree of moisture; so the quality of the said Medicine is 7 degree of heat, and 1—1 degree of moisture, as by the operation is manifest.

Prop. III.

To augment or diminish a Medicine in quality according to any degree assigned.

Suppose a Medicine to be compounded as followeth, viz. 1 dram of a Simple hot in 4°. 2 drams hot in 3°. 2 drams hot in 2°. 1 dram hot in 1°. 1 dram ix.

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dram cold in 19. and 1 dram cold in 20. Then will the quality of the faid Medicine be in 1 degree of heat, (as will be manifest by the second Proposition.) Now let it be required to augment the faid Medicine in quality, viz. to add fuch a quantity of some one of the Ingredients, (or some other simple) which may raise the quality of the Medicine 1 degree, fo that the temperament of the Medicine after it is increased in quantity, may be in 2°. of heat. Make choice of fuch a simple, the Index of whose quality may exceed the Index of the quality affigned, viz. make choice of that simple which is hot in 3°. whose index is 8, then proceed according to the I example of the first Proposition; so will you find that if I dram of the aforesaid Medicine be mixed with - dram of that fimple which is hot in 3°. the temper refulting from fuch mixture will be in 2°. of heat.

Lastly, by the Rule of Three, fay, if 1 dram require dram, what shall 8 drams (the quantity of the

Medicine first given) require?

Answ. 4. drams: So that if 4 drams of a simple which is not in 3°. be mixed with 8 drams of a Medicine which is hot in 1—degree, the temper resulting will be in 2°, of heat, as by the operation is manifest.

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If it be required to diminish a Medicine in qua. lity, you are to make choice of fuch a Simple, the Index of whose quality may be less than the Index of the quality affigued, and then to proceed as before

Here observe, that if in questions of this nature, the quantities of the Simples be express by weights of divers denominations, they are to be reduced to that weight which is of the lowest denomination in the question, according to the fixth rule of the feventh chapter of the preceding book.

The augmenting or diminishing of a Medicine in respect of quantity; Also the finding of the value of any quantity of a Medicine, the prices of the ingredients being known, will be familiar to such as understand the Rule of Proportion, and therefore I shall not insist upon them.

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CHAP. IX.

A Demonstration of the common Rule of False by two Positions.

I. W Hat the ordinary double Rule of False is, and how to be used in resolving such questions which cannot be readily applied to any of the other rules of Ariebmetick, hath been sully declared in the 15 and 31 Chapters of the preceding book; it remainesh to shew what kind of operation is presupposed before the said Rule can be applied to the resolution of a question, and then to demonstrate; the truth of the Rule is self.

the question requires to be performed with the number sought and some given number or numbers; the same kind of operation in every respect is to be made with each of the two seigned numbers, (commonly called Positions) and the said given number or numbers, which threefold process being finisht, (whether it be by any one, or all of these rules, to wit, Addition, Subtraction, Multiplication, and Division) there will arise three remarkable numbers or results, to wit, one resulting from the true number sought, and two others resulting from the

the two feigned numbers; then from these three results, the errors are collected, which are nothing else but the differences between the true result, and

each of the two falfe refults.

III. After the faid errors or differences are difcovered, the Rule of False will be of no force unless this Analogy or proportionality doth arife, namely, the first error must have the same proportion to the fecond; as the difference between the number fought and the first feigned number hath to the difference between the faid number fought and the fecond feigned number; here therefore it may be demanded, what kind of operation will produce the faid Analogy? To this I answer, when the question requires the number fought to be increased leffened, multiplied or divided by fome given number, or the number arising from such operation to be increased, lessened, multiplied or divided by some given number; in any of those cases, the aforefaid Analogy will necessarily arise, as I shall here mamifelt in all the faid cales. Firft, therefore I fay, when unto each of three numbers (namely, the number fought by the Rule of False and the two feigned numbers) one and the same number is added, the faid Analogy will enfue, for in this cafe the difference between the first sum and the second, will be equal to the difference between the first and fecond of the faid three numbers ; likewise the difference between the first fum and the third, will be equal to the difference between the first number and the third, which may be proved in manner following.

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Suppositions.

Let there be three numbers, to wit,

A . B . C

Suppose also that the first number A is greater then either of the numbers Band C.

Suppose also, some number as D (3) to be added to each of the said three numbers, so will the three sums be,

A + D | 15 B + D | 10 C + D | 8

The Proposition to be demonstrated is, that the difference between the first sum and the second is equal to the difference between the first number and the second; also that the difference between the first sum and the third is equal to the difference between the first number and the third.

Demonstration.

The difference between the first number and the second is,

A-B

The difference between the first sum and the se-

A + D-B-D

But the latter difference is manifestly equal to the former, (for † D and D expunge one the other) to wit,

$$A + D - B - D = A - B$$

Therefore the first part of the proposition is proved.

Again, the difference between the first number

and the third is,

A-C

The difference between the first sum and the third is,

A+D-C-D

But the latter difference is manifestly equal to the former, for + D and — D expunge one the other) viz.

A+D-C-D=A-C

Wherefore the proposition is fully proved.

The like property might be proved after the

fubtracted from three numbers feverally.

Secondly, when three numbers (namely the number fought by the rule of False and the two feigned numbers) are severally multiplied by one and the same number; the aforementioned Analogy will likewise ensue, as may be thus proved.

Suppositions.

Let there be three numbers, to wit,

A . B . C

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Suppose also that the first number A is less than either of the numbers B and C.

Suppose also, each of those three numbers to be multiplied by one and the same number as D (4) and the three products to be these,

DA 12 DB 20 DC 32

The Proposition to be demonstrated is, that the difference between the first product and the fecond, hath such proportion to the difference between the first product and the third, as the difference between the first number and the second, hath to the difference between the first number and the third, vie.

$$DB - DA \cdot DC - DA :: B - A \cdot C - A$$

Demonstration,

Forasmuch as (by the 17th Prop. of the seventh book of Euclids Elem.) If a number (D) multiplying two numbers (B—A and C—A) produceth other numbers (DB—DA and DC—DA) the numbers produced by the multiplication shall be in the same proportion as the numbers multiplied are, therefore

DB-DA . DC-DA :: B-A . C-A

which was to be demonstrated.

Likewise when 3 numbers are divided by one and the same number the demonstration will not be otherwise;

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otherwise; and because by the second Section of this Chapter, the errors in the rule of False are the differences between the true result and the two salie results, therefore from the precedent demonstrations it is evident; that the afore-mentioned Analogy or proportionality (namely, when the first error hath such proportion to the second; as the difference between the number sought and the first seigned number, hath to the difference between the said number sought and the second seigned number) will succeed from such operation as is before declared in the beginning of the third Section of this Chapter.

To know whezher a question be refolvable by the Rule of False or not. IV. Now to discern what kind of operation will not produce the said Analogy, observe this note, viz. when a question requires some given number to be divided by the number sought or any part thereof, also

when the number sought or some part thereof is to be squared, cubed, &c. Likewise when some parts of the number sought are to be multiplied one by the other; I say from such operations the aforementioned Analogy will not arise, and in those cases, the ordinary rule of False will be useless; as may partly appear by the two following examples, viz. What number is that by which if 360 be divided the quotient will be 24? Here if two positions or seigned numbers be taken, and 360 be divided by each of them, the errors will not be in the same proportion with the differences between the true number sought and the two seigned numbers, and therefore the rule of False will be used in vain; yet if it be asked what number is that which being multiplied

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by 24, the product will be 360, the answer to this latter quellion is the fame with the answer to the former, and may be found by the rule of Falfe, but fuch kind of interpretations and inferences are not alwayes obvious, and therefore fince the preparative work of the rule of Falfe, (after a number is taken by guess for the number sought) proceeds gradually from one condition in the question to another, it will for the most part be easie to determine whether the ordinary rule of Falfe will take place or not, by comparing the conditions of a question with the note before given.

Another Example; a certain person being demanded what number of years he had lived, answered, if i of that number were multiplied by i of the fame number, the product would thew the number, or his age: here it will be in vain to fearch the number fought (which is 40) by the rule of Falle, for the aforementioned Analogy or proportionality will not fucceed, and the question cannot easi-

ly berefolved without Algebra.

Now from this supposition, that after the preparative work of the rule of Falle is finisht, the errors will be in fuch proportion as aforefaid, I shall make it manifest that the Rule of Falfe will discover the number fought.

V. In the Rule of two falle Politions there are 3 cases, viz. the errors are either both excesses and noted with +, or else both defects and noted with -, or laftly one of the errors is noted with t, and

the other with

In the two first cases, the Rule is this, Multiply the Politions or feigned numbers by the altern errors, viz, the first Polition by the lecond error,

Destoil.

The demonstration of the faid Rule here fol.

Gafe I. When the errors are both excesses and noted with t. ten when the only seem w

Suppositions.

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i. Let fome number unknown and fought > by the rule of Falfe be represented by , . . . 2. Let the first Polition (or feigned num- 3 B ber) be

3. And the fecond feigned number C

4. Suppose also that B is greater then C, and each of them greater then A.

5. Moreover suppose the error of the first F polition to be

6. And the error of the fecond polition? to be .

7. Suppose also that this Analogy will be found in the faid numbers, viz.

B-A . C-A .: F . G

8. The proposition to be demonstrated.

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mort 10 to noitheantal launs ed sycherad I ver Demonstration.

9. Forafmuch as by fuppolition in yo.

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iou ente will ar fe, vic. io. Therefore by comparing the rectangle of the extreams to the rectangle of the means,

GB-GA-FC-FA

11. And by equal addition of FA.

FA + GB-GA = FC

12. Again, forasmuch as by supposition in 4°.

B > C

t. Let fome number unknown and fourth

13. And confequently out of 49, and 129.

a. And the feecond polition,

14. Therefore out of 99, and 139; 1 1 100 100

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15. Therefore

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16. Therefore

FA-GA > 0

Ff 2

17. There-

17. Therefore by equal subtraction of GB from the equation in 11°.

FA-GA=FC-GB

18. Wherefore by dividing both parts of the last equation by F-G, equal quotients will arise, viz.

$$A = \frac{FC - GB}{F - G}$$

which was to be demonstrated.

Case II. When the errors are both defects, and neted with —

Suppositions.

1. Let some number unknown and sought } A by the rule of False be represented by }

2. Let the first position (or feigned num- } B

3. And the fecond polition, C

4. Suppose also that B is lesse then C, and each of

5. Moreover, suppose the error of the first F

6. And the error of the fecond Polition . . G

7. Suppose also that this Analogy will be found in the said numbers, viz.

A-B . A-C :: F . G

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Chap.IX. the Rule of False.

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8. The Proposition to be demonstrated.

Demonfration.

9. Forasmuch as by supposition in 7°.

10. Therefore by comparing the rectangle of the means to the rectangle of the extreams.

11. And by equal addition of FC

123 Again, for almuch as by supposition in 4°.

Hode ever and following the first error, and refere entry one of format 12% who as

duct by the fun of the and errory ray quotient half be be non of the set
$$\mathbf{a}_{j}$$
 the function:

The Demonstration cours factor 3 als berefole

14. Therefore out of 9°. and 13°.

is from humb-Dice Two and fought by ?

15. Therefore dead de la lange

FA > GA Ff 3

16. There-

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FA-GA > 0

17. Therefore by equal subtraction of GA from the equation in 110.

Demonstruison. FA-GA = FC-GB

o. Foralmuch as by supposition in 18. Wherefore by dividing both parts of the last equation by F-G, equal quotients will arife, vic.

10. Therefore by 30mg ing the recengle of the means to the recenge of the decreams.

which was to be demonstrated.

Cafe III. When one of the errors to an excels (10 wit, noted by to and the other a defect) (noted

In this third Cafe the Rule of Folfe is this, via. Multiply the Politions by the altern errors, to wit the first Polition by the second error, also the fecond Polition by the first error, and referve those products, then dividing the fum of the fuid-products by the fum of the faid errors, the quotient shall be the number sought by the question.

The Demonstration of this latter Rule here followeth. za. Therefore out of o', and

Suppositions.

1. Let fome number unknown and fought by ? the rule of False be represented by

2. Let the first Position be 3. And ix.

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A Demonstration of, &c. Appendix. equation by F + G, equal quotients will arife, viz.

Suppose also the transpose than C, and also S. More ver, ful to The error of the first &

which was to be demonstrated. ...

The learned Herigonius (in cap. 13. Tom. 2. of bis Cursus Mathematicus) hath delivered another, way of resolving the rule of False, namely, by the two following rules, viz,

When the figns of the Errors are unlike.

Rule I. As the fum of the errors is to the first error. fo is the difference of the supposed numbers to a fourth proportional, which being added to the first supposed number, when the faid first supposition is less then the second, or subtracted from it when it exceeds the fecond; the fum or remainder will be the true number fought.

o. I arafinuch as by leppolitic When the figns of the Errors are unlike.

Rule II. As the difference of the errors is to the bifferzor, fo is the difference of the supposed numbers to a fourth proportional, which being added to the first supposed number when the signs are or fubtraced from it when the figns are + , the fum or remainder will be the number fought.

Both which rules the faid Herigonius demonstrateth geometrically by lines, upon a fupposition of the Analogy or proportionality before mentioned in the third Section of this Chapter and the fame may likewife be eafily demonstrated according to the precedent method by letters with the C H A P.

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A Collection of pleasant and subtil Questions, to exercise all the parts of Vulgar Arithmetick. To which also are added various practical Questions about the menfuration of Superficial Figures and Solids.

West. 1. If a wedge of Examples of the Rule of Three mixtly wied Gold weighing 173 th.of with other rales. Troy weight be worth 6795 16. ferling, what is the value of 1-3 grain of that Gold? Answ. 2 pence.

times (or 18) of 10 f ada 11 4123 4743 1001 34 20 12 14 4680 1 21d 10

Queft. 2. A man dying gave to his eldeft Son 2 of of his estate, to his fecond Son ; of i of his estate, and when they had counted their Portions, the one had 40 1 more then the other, the remainder of the estate was given to the wife and younger children, the question is, what was the portion of the eldeft Son, also of the second, and how much did belong to the wife and younger children? Anfw. done

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Answ. The eldest Sons portion 100 l. the second

Sons portion 60 l. and 440 l. for the wife and younger children.

The fractions being reduced, it will be manifest that the eldest Son had i, and the second i also the difference of the said fractions is in, then say,

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			hesetick.	60
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-05 7 %	e second Sons po difference of the eldest Sons po	rtion	S 6 40	100
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Luftly, 600 160 = 440 for the mile and mon-

Quest. 3. A young man received 6621. which was $\frac{1}{3}$ of $\frac{1}{3}$ of his elder brothers portion, and $3\frac{1}{3}$ times of his elder brothers portion was $1\frac{1}{3}$ times of his fathers estate, the question is, what was the fathers estate? Answ. 5601.

Bird dayse of the work in 20 dayes, and Burd a work in 20 dayes, and Burd work in 20 dayes, and be found that work in 20 dayes, and bow much do be found to the found, and how much do the food, and how much do the food.

First find wham quanticy of the work will be

ndix. Chap.X. Questions. 447 cond done by each workman in one and the fame time; and then it will be as the fam of those quantities is in proportion to the faid time, for is t or the whole that work to the time wherein furth work will be oni-rence boll addition a smark and dayastad workland or 3600 no mago sabod enus il storis yeb add I wal. Es min Cilentedance . Hence it appears that A and B working together 20 dayes, will finish that work once, together with of the fame work; therefore fay again by the Ex Rule of Three, PANwork adayes the more D can son and by all we four firems standog sogsther 1: Then fav ich by the rule of Three: Dayes . TiAsuQue Areus adsto leo, zubuli mihi lumina binu nes qui Ofque etiama dextri fic quoque planta pedie. he plied with while off what have certain and with white and if the cock of courses and ship and population the an Orisufficiant der harend Die fommieren ihm arefin

The fense is this. A brazen Lyon being placed in an artificial fountain, conveyeth water duty a Castern by two streams is thing from his eyes, also by one from his mouth, and by another at the host for of his right foot. Now the Pipesthrough which these streams passe are of different capacities.

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in fuch fort, that by the right eye fet open alone, the rest of the streams being stope, the Cistern will be filled in two dayes; (the length of a day being the supposed to be as hours) by the lest eye alone in three dayes; by the soot alone in four dayes, and by the mouth alone in six hours. The question is, to find in what time the Cistern will be filled, if all that those streams be set open at once?

Answer, 12 day.

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The sum is 9. Cisterns that will be filled in 3 dayes by all the foun streams running together: Then say by the rule of Three.

Cift. Dayes Cift. day

2007. 6. A Ciffern in a certain Conduit is supplied with water by one pipe of such bigness, that if the cock A at the end of the pipe be ser open, the Cistern will be filled in hour; moreover at the bottom of the Cistern two other cocks B and C are placed, whose capacities are such, that by the Cock B set open alone (all the rest being stopt) the Cistern supposed to be full) will be emptied in 13 hour; also by the cock C set open alone the Cistern will be emptied in 2- hour; now because more water will be insused by the cock A, then can

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will e expelled by both the cocks B and C in one and eing he same time; the question is to find in what e in time the Ciftern will be filled if all the faid three and tocks be set open at once? Answ. 1 2 hour.

if all chapter, find how many times the ciftern will be emptied in one and the same space of time, by the cocks B and C running together; also how much of the ciftern will be filled by A in the fame time, then will the difference shew how much of the ciftern is gained by the filling cock in the faid time : Laftly, as the cifterns or parts gained are in proportion to the correspondent time; so is the whole ciftern, to the time wherein it will be gain. ed or filled.

hou, cift. hon. cift.

1.
$$2\frac{1}{3} \cdot 1 :: 1\frac{3}{7} \cdot (\frac{10}{40}) \frac{3}{2} \begin{cases} C \\ B \\ Add 1 \end{cases}$$

Add 1 $\frac{1}{40} \begin{cases} B \\ B \\ B \end{cases} C$

hou, cift. hou.

11. $\frac{1}{4} \cdot 1 :: 1\frac{3}{7} \cdot (2\frac{6}{7} \text{ filled by } A)$
 $\frac{1\frac{12}{49} \text{ gained by } A}{1\frac{12}{49} \text{ gained by } A}$

bon. cift. 13 :: 1 III.

Queft.7. Suppose a Dog, a Wolf, anda Lion; were to devour a Sheep, and that the Dog could eat up the fheep in an hour, the Wolf in 3 hour, and the Lion in - hour ; now if the Lion begin to eat hour before the other two, and afterwards all three

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three eat together, the question is, in what this the sheep would be devoured? Answ. 120 hour.

Thus it appears that of the theep would be eaten by the Lion, before the Dog and Wolf began to eat.

II. Proceed according to the fourth question, so will you find the remaining; to be eaten by them all in 512 hour, which added to 8 gives 114 hour, in

which time the theep would be devoured.

Quest. 8. Is 20: 1. be to be distributed amongst three persons A,B,C, in such sort, that as often as A takes 5, B shall take 4, and as often as B takes 3, C shall take 2; what shall be the share of each?

Answ. A 51 4 1. B 41 5 1. C 27 53 1.

Find three Numbers which may expresse the proportions of their suares, by the Rule of Three, or (to avoid fractions) thus,

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Quest. 9. A Governour of a certain Garrison, being desirous to know how much money the Port of passage of the Garrison did amount unto in certain moneths, made choice of a loyal servant, giving him order to receive of every coachman passing with a coach 4 d. of every horseman 2 d. and of every footman 1 d. Now at the years end, the servant making his accompt to the Governour, giveth him 94 l. 15 r. 10 d. and lets him know that as often as 5 passed with coaches, 9 passed on horseback; and as often as 6 passed on horseback, 10 passed on foot; the question is, how many coaches, horsemen, and sootmen passed? Answer, 2500 coaches, 4500 horsemen, 7500 footmen.

Find 3 proportional numbers after the manner of the eighth queltion, which will be 5,9,15, then

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Coaches . . 20 o Horsemer 18 15 Footmen . 7-If 45 . . 22750 :: 9 . 4500

Quest, 10. A Factor would exchange 780 l. ferling for double Ducats, Dollars, and French Crowns, the Ducats at 7 s. 6 d. the piece, the Dollars at 4s. 4d. and the French Crowns at 6 s. the piece; to be in such proportion, that - of the number of Ducats may be equal to tof the number of Dollars, and i of the Dollars equal to of the Crowns the question is, how many pieces of each coin he shall receive for his 780 pounds.

Anfw 600 Ducats, 900 Dollars, 1200 Crowns. Find three proportional Numbers (after the manner of the eighth question) which will be 6,4,3.

ng his seconderto the Covernour, -sland ee bollen of mice en hotel Tellion to the many coaches, songe, assente Costinganina

Thus it appears that fix times the number of Ducats must be equal to four times the number of Dollars, also equal unto three times the number of Crowns. Then make choice of 3 numbers to answer those proportions, fuch are these, 2,3,4,

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(for 6 × 2 = 4 × 3 = 3 × 4) with which numbers proceed as followeth:

3 . 1 :: 360 . 1200 crowns.

Quest. 11. Twenty Knights, 30 Merchants, 24 Lawyers, and 24 Citizens, spent at a dinner 64 pound, which was divided amongst them in such manner, that 4 Knights paid as much as 5 Merchants, 10 Merchants as much as 16 Lawyers; and 8 Lawyers as much as 12 Citizens; the question is, to know the sum of money paid by all the Knights, also by the Merchants, Lawyers and Citizens.

Answer, The 20 Knights paid 20 pounds, the 30 Merchants 24 pounds, the 24 Lawyers 12 pounds,

and the 24 Citizens 8 pounds.

Find four numbers to express the proportions of their payments, by the Rule of Three, or (to avoid fractions) in manner following, so will the proportional numbers be 4,5,8,12, viz. 4 Knights paid as much as 5 Merchants, or 8 Lawyers, or 12 Citizens.

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320 . 400 . 640 . 90		2 14 ms 2.

thus found, 4 × 10 × 8=320

10 × 8 × 5 = 400 8 × 5 × 16 = 640 5 × 16 × 12 = 960

Then presupposing that a Knight is to pay 4.s. proceed as followeth viz.

Quest. 12. A' certain man with his wife did usually drink out a vessel of Beer in 12 dayes, and the husband found by often experience, that his wife being absent, he drank it out in 20 dayes; the question is, in how many dayes the wife alone could drink it out? Answer 30 dayes.

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Note, it is to be supposed that the husband in 12 of the 20 dayes wherein he drank alone, did drink as much as in the 12 dayes wherein he drank with his wife, hence it followedly, that in the remaining 8 of the said 20 dayes, he drank as much as his wife did in 12 dayes. Therefore by the Rule of Three say, If 8 give 12, what 20? Answ. 30. view the following form of the work.

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Carpenters, A, B, C, working in such fort, that A alone will finish it in 30 dayes, B in 40 dayes, and A, B, C, together in 13 dayes, in what time could C alone build the house? Answ. 120 dayes.

I. After the manner of the fourth question, find in what time A and B working together will finish the house; Answ. 17- dayes.

work dayes work dayes.

II. Supposing the work of A and B to be performed by one person, as D, the house will be built by D in 177 dayes, but by D and C together in 13 dayes; Then find (according to the 12th. que-

As6 Arithmetical. Appendix. fiion) in what time C will build the same; Answ. 120 dayes.

From 17½ and solution with the Subfract 15 and solution a

Then if 27 . 15 :: 177 . 120

The proof may be wrought according to the

fourth or fifth questions.

Quest. 14. Two Travellers A and B perform a journey to one and the same place in this manner, viz. A travels 14 miles every day, and had travelled 8 dayes before B began; upon the ninth day B sets forward, and travels 22 miles every day; the question is, to find in what time B shall overtake A? Answ. at the end of 14, dayes.

I. Find how many miles A had travelled before

B fet forward? Anfw. 112 miles 3 For

day miles dayes miles
1 . 14 :: 8 . 112

II. Find how many miles B gains of A in a day;
Answ. 8 miles; For

22 -- 14 = 8

miles day miles dayes.

III. If 8 . I :: 112 . 14

Quest. 15. There is an Island which is 36 miles in compass. Now if at the same time; and from the same place, two sootmen A and B set forward

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to travel round about the faid Island, and follow one another in fuch manner that A travelleth every day 9 miles, and B 7 miles; the question is to find in what space of time they will again meet, also how many miles, and how many times about the Island each footman will then have travelled?

Answer, They will meet at the end of 18 dayes from their first parting, and then A will have travelled 162 miles (or 4 times the compass of the Island) and B will have travelled 126 miles (or

3 times the compais of the Island.)

miles
From ... 9
Substract 7

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A box 436) 162 (41

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mult. 18.

Quest. 16. Two footmen A and B depart at the same time from Landon towards York, travelling at this rate, viz. A goeth 8 miles every day, B goeth 1 mile the first day, 2 miles the second day, 3 miles the third day, and in that progression he goeth forward, travelling in every following day one mile more then in the preceeding day, the question is, to know in how many days B will overtake A?

Answer, 15 dayes.
To resolve this and such like questions, double 8 (the number of miles which A travelleth daily)

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which makes io, from which fubfract 1, the remainder is 15 the number of dayes fought one sno

Dieft. 17) If Excetter be diffant from Landon 140 miles, and that at the fame time one footman A departed from London to wards Executor a trayelling every day 8 miles; and another B from Exceter towards London, travelling every day 6 miles; the question is, in how many dayes they will meet one another, and how many miles each fobstes will have then the welled? and Hiw & bes (buell!

Answer, They will meet at the end of 10 dayes, and then A will have travelled 80 miles, and B 60

miles.

add { 8 miles travelled daily by A

fum . 14 miles which A and B together . .81 . did travel dayly.

m. da. miles da.

1450 (2349 . 10 in which time A and B will meet each other. 10 + 8 = 80 miles travelled by A

10 208 200 milesotratelled by B. smil arrhista to me. A goeth 8 miles ever

Quelt 18: A cererin footman A departeth from London to wards Lincoln, and at the same time and ther footman B departeth from Dincoln wowards London; alfo-A travellerh every day 21 milesmore then B. Now suppoling those two Cities to be too miles diffant one from the other, and that thofe two footmen do meet one another at the end of 8 dayes after the beginning of their journeys, the question is, how many miles each will have then travelled ,

Chap X. Questions.

A 59

Fravelled, as also how many miles each travelled daily?

Answer, A 60 miles, B 40 miles. Also A travel-

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led 7 miles every day, and B s miles.

Hence it appears that at the time of their meeting A had travelled to miles inove than Briwhich 20 miles being substracted from 100 miles leaves 80 miles, whereof the half is 40 miles which B had travelled, therefore A had travelled 60 miles. Now to find how many miles each travelled dai-

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cose of which (to wir A) is threved being round; the whole adimmference of the Dyal in one day; and the original and the original pales and the both are one fill any that both at once in the pales are the both at one content or one fill are the what time they will be as

Quest. 19. There is an Island which is 134 miles in compass; now at the fame time, and strom the same place, two footmen A and B begin a journey round about the said Island, but they stravel towards contrary parts, at this rate, viz. A traveleth 11 miles in every 2 dayes, and B 17 miles in 3 dayes: the question is to find in what space of time A and Swill meet one another, and how many miles each will then have travelled?

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3. 17: 12. 68 miles travelled by B.

Queft. 20. If a Clock hath two Indices (or hands) one of which (to wit A) is carryed twice round the whole excumference of the Dyal in one day; and the other (B) once in 30 dayes, and that both

at once shewing the same point begin to be moved; the question is, in what time they will be a-

i dufver, & day os 12 hours, on lequion in

Hence it appears; that in soudants A will have run through 60 cibeumference and Bone circumference and Bone circumference only in the same time, therefore A gains

a dayes a they dell on is to hird in a but space of time A al. 1 exwith meet one another, and bowming

dix. Chap. K.

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this of B 39 circumference, in 30 dayes therefore fay, a Hore in fuch fore that the Hare takes hee lead

1 and circum, and days ods to circum wol vday a rol Feel of bertown leaps of ant from

Queft. 21. If 6 th. of Sugar be equal in value to 7th of Railins , 7th of Railins to 2th of Almonds; 3th of Almonds to 5th of Currans 32th of Currans to 18 d. how many pence are the value of 3 16. of Sugar? Anfw. 21 d.

18000 de T) 3780 (21 VII

Queft. 22. If 3 dozen pair of Gloves be equal in valueto 2 pieces of Ribbon; 3 pieces of Ribbonto y dozen of points; 6 dezen of points to 2 vards of Flandersviace, and 3 yards of Flanderslace to 81 Millings how manywdozen pair df andife. z dozen pair of Gloveschning and tho

who height is five feet, and breadth four teet, are to Rulf (03 dGlo to 20 RacHing benling to sel es 3 R = 7 P. 3 Son brev and a second a second and a second and a second and a second and a second and a second and a second and a second and a second and a second

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Queft- 23. Suppose a Greybound to be courfin 2 Hare, in fuch fort that the Hare takes five leap for every four leaps of the Greybound, and that the Hare is one hundred of her own leaps distant from the Greybound; now if three of the Greybounds leap be equal to four leaps of the Heres, the question is to know how many leaps the Greybound must take before he abtain his prey di y or shand to di Anfwer, 1200 leaps nag youm wed & 81 of ant

of Sugar ? dafa. 21 d. I. If 3 . 4 :: 4 . 5

Thus it appears, that 4 of the Greybounds leap are equal to st of the Hares leaps, and because by the question the Greybound takes 4 leaps for every of the Hares therefore the Greybeund in every four of his leaps gains of one of the Hares leaps; therefore fay by the Rule of Three 8

24 J. 3.4090 :: 04 Ctove H. II in value to 2 pieces of Ribbon; 3 pieces of Rib-

2 of Queft a 40 There is a contain room who fe Bafis de a long fquice, which is in circuit you feet and the beighe of the walls or lides of the roomsis significati all which washi bifithe poomiercept la sipaco waken out for a windowin be form of a dong. forare, whose height is five feet, and breadth four feet, are to be furnished with Hangings of elDbroad Huff at 3 s.4 d.the yard, the question is to know how much money the Mill will colt ?

Answer, 5 1. 17/s, 63 do 18 = ... 25 S. = ? C. leap

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Then because gos as for the yard is eq 50 + 81 = 410 [fquare foet. 10 971 up] 5 × 4= 20 [ubtract

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34 × 3 = 11 | Square feet in one yard of Stuff.

disheard been If 11 40 : 399 0 1410 101

Duck 25 There is a cerenin Walk which is a eap long fquare, whose length is go yards, and breadth le by 7 yards, to be paved with Rones each of which berys ing in the form of a long square is 28 inches in four length, and 24 inches in breadth, the question is to know how many luch stones will be requisite to pave the faid Walk?

Answer, 540.

Queft. 28. A Merchan we radorf Codort Co.

Quest. 26. Suppose a piece of Tapestry to be 33 yards English in length, and 3% yards in breauth, the question is, how many square ells Flemish are contrined in that piece of Tapestry, when the length of 1 ell Flemish is equal to 1 of a yard English? Answer, 37 1 square ells Flemish.

53 × 38 = 2133 [quare yards.

Then

Then because of a square yard is equal to 1 Square of Flemiff measure (for 10 3 = 2) fay,

If 16 . I : : 1333 . 37 36

Queff. 27. A Workman hath performed a piet of Tiling bearing the form of a long square, who length is 273 feet, 7 inches ; and breadth 21 feet inches; now when Tiles are fold at the rate and in 11 . 10 3 d. for 1000 tiles, and every square of tilin out consisting of 10 feet as well in length as in breadthe doth take up 1000 tiles, what doth the said piece half tiling amount unto? ad Answer, 34 1.17 7 deor d. 200 d of of they

fur ingin the foim of a 18th fquere is 28 inches in

100 • 142 :: 843731 83.64 400r

Queft. 28. A Merchant would bestow 220 1. i 00 Cloves, Mace and Nutmegs, the Cloves being a 5 s. the pound, the Mace at 11 s. the pound, and the he Nutmegs at 6 se the pound; now he would have o qua each fort an equal quantity, the queltion is hor idd many pounds he may have of each fort?

qualitantis, dow mary fquareelle Flewillette conto the Cortbut piece of Topefing, when the length of i ell Florifb is equa to t of a pard Frelia!

Antwer 37 - Janare elle Flemilb.

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feet Queft.29. A Factor is to receive a sum of money, ate and is offered Dollars at 4 s. 4 d. which are worth tiling out 4 s. 3 d, or French Crowns at 6 s. 1 d. which eads re worth but 6 s. the question is by which coin he eees hall sustain the least loss?

Answer, the Dollars.

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piec who hap. X. A.

d. d d. d. $\frac{4}{52}$. 1. :: $73\frac{7}{2}$. $1\frac{43}{104}$

That is, in receiving the Dollars every 6 s. 1 d.

oofeth 1 d but in receiving the Crowns 6 s. 1 d.

i oofeth 1 d. which is a greater loss than 1 d.

Answer, 1 moneth.

Consider, that as he receives more Oxen to feed, be ought to keep them all the less time; therefore

work as the question imports by the Rale of Three inverse.

		mon.	. 010	Oxem	e in the	3.	35,000
	O. I.	12	· atm	20	10000	II	JE 004
Oxen.	0.0	2	. 233	5	19505	mon.	Oxen
If 20	9,5	10		25		(8	25
Shon	19 114	in sv	iponi	D2 81	7 1)	61	. 10

16 25 13 . . 35 (1 mgn Queft, 31. Two Merchants wie. A and B,have entered Company; A put the Rule of out a certain sum, leaving the remainder to continue 8 moneths longer. B puts in 250 l. and at five he Fellowship. moneths end puts in three hundred pounds more, who and then his whole fum continues feven moneths longer. Now at the making of their Accompt. A 33 findeth that he hath gained 106; pounds, and B wh gained 133 pounds; the question is to know how qui much A took out of the bank at 4 moneths end?

> 250 x 5=1250 add 300 550 × 7=3850

Answer, 2401.

. 5100 :: 1062 . 4080 500 × 4 = 2000 [ubtrait

8) 2080 (260 Lastly, 500-260 = 240 taken out by A. 90

Doch 33. Two Merchane A safe in cons

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pour the film of their Proof. The money or sectioning in company o moneth, the money o

monache they gon a non which they divide e

bes them v 300 70 21 = 12000 fromport

Subtract 240

ribe took of B, which

260 × 8 = 2080 relier part be nico of will the g

4080 pleiplie at beir rot er ive timee

5. A put Queft. 32. Five Merchants, viz A,B,C,D, and E. takes are gained 2025 l. which they divide in fuch fort, onti. hat of the share of A is equal severally to of five he share of B. of C. of D. of B the question is; ore, what was the share of each Merchant?

eth Answer, A 162 l. B 324 l. C 405 l. D 486 l. E 648 l.
A Divide a number at pleasure into such parts
b which may be in such proportion as the shares relow quired, and proceed according to the subsequent ? operation,

2. (162 for A whereof is 81 4: (324 for B whereof 4 is 81 If 25 . 2025 :: \ 5. (405 for C mbereof is 81

6. (486 for D whereof : is 81 8. (648 for E whereof is 81

Appendix

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Quest. 33, Two Merchants A and B are in company, the sum of their stocks is 300 l, the money of A continuing in company 9 moneths, the money of B 11 moneths, they gain 200 l, which they divide equally, the question is to know how much each Merchant did put in?

Answer. A 165 L B 135. L.

Divide 300 into two such parts, which may be in proportion as 11.to 9, so will the greater part be the stock of A, and the lesser the stock of B, which stocks being multiplied by their respective times; the products will be equal.

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Quest. 34. Two Merchants, viz. A and B are in company, A did put in 325 l. more then B, and the stock of A continued in company 7 moneths; B put in a certain sum which is unknown, and it continued in company 102 moneths, after a certain time they divide the gain equally; the question is what each Merchant did put in?

Answer, B 7501. and A 1075 1.

Divide the product of the difference of their flocks multiplied by the time of A, by the difference of their times, so will the quotient be the flock of B, which added to 325 l. gives the stock of A.

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Quest. 35 A Goldsmith hath some Gold of 24 Carects, others of 22 Carects, and another fort of 18 Carects sine, he would so mix these together that the mass mixed might be 60 lb. and that the whole mixture might bear 20 Carects sine. How much of each sort must be take?

Examples of the Rule of Alligation. How the fineness of gold and hiver is estimated, v. p.111.

Answer,
$$\begin{cases} 12 & \text{of } 24 \text{ Carests.} \\ 12 & \text{of } 22 \text{ Carests.} \\ 12 & \text{of } 12 \text{ Carests.} \end{cases}$$

$$\begin{cases} 24 & 2 \\ 20 & 18 \end{cases}$$

$$\begin{cases} 24 & 2 \\ 218 & 10 \end{cases}$$

$$\begin{cases} 2 & 12 \\ 2 & 12 \end{cases}$$

$$10 & 60 :: \begin{cases} 2 & 12 \\ 2 & 12 \end{cases}$$

$$6 & 36 \end{cases}$$

Note, some may think that questions of Alligation are capable only of so many several answers as there are different wayes to connect the mean rate or price with the extream rates or prices; yet it is most certain, that any or-

Main mol tions

dinary question of Alligation, where three or more things are propounded to be mixt in such manner as that rule requires, is capable of infinite answers if fractions be admitted, and sometimes of many answers in whole numbers, which are not discoverable by the common rule of Alligation: so albeit to the last mentioned question, the said rule of Alligation can find but one answer only, which is before given, yet there are eight other answers in whole numbers, which are these that follow the invention whereof I have shewn in the 19th Question of the thirteenth chapter of my second Book of the Elements of Algebra.

Of 24	Carects	18	16	14	10
Of 22	Carects	3	6	9	13
Of 18	Carects Carects Carects	39	38	37	35

of	24	Caretts	18	6	1 4	2
Of	22	Carects	18	21	24	27
Of	18	Carells Carells Carells	34	33	32	3.1

See chap. 8. of Quest. 36. An Apothecary hath sethis Appendix. veral Simples: vix. A hot in 3°. B hot in 2°. C temperate, D cold in 2°. and E cold in 4°. Now he desires to make a Medicine of those Simples, in such fort that the temper thereof in respect of quality may be in 1°. of heat, and the quantity 8. Drams, the Demand is what quanti-

ty of each Simple he must take?

Answer, 4 Drams of A, Dram of B, 1 Dram of

C. 1 Dram of D, and 1 Dram of E.

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Quest. 37. A Merchant buyeth 2 forts of Clothes, viz, of blacks and of whites for 68 l. 2 s. after the rate of 21 s. the yard for the blacks, and 12 s. the yard for the white, and he taketh so much of each fort, that of the number of yards of the black, are equal to 1 of the white; the demand is

how many yardshe bought of each fort ?

Answer, 22 yards of black, and 40 yards of white.

Queft. 38. A certain person A payeth unto the
use of B for ever 2500 l. in present money, upon
this condition, that B shall pay unto A an Annuity
or yearly rest to be continued four years, the equality of their agreement being thus grounded,
wiz. the said 2500 l. is supposed to be put forth at

Hh 2 interest

interest for a year, (to commence from the time of their agreement) at the rate of 8 per centum, per annum. Then from the fum of that principal and interest, (arising due at the years end) the first payment of the Annuity being subtracted, the remainder is likewise supposed to be put forth at the same rate of interest for the second year; then from the composed of this principal and interest, (due at the second years end) the second payment of the Annuity being subtracted, the remainder is likewife supposed to be put forth at the same rate of interest for the third year; then from this principal and interest the third payment of the Annuity being subtracted, the remainder is in like manner supposed to be put forth at the same rate of interest for the fourth year : lastly, from this principal and interest the fourth and last payment of the Annity being subtracted, there must be nothing left: the question is, what sum of money must be yearly paid to fatisfie those conditions?

Answer, 754 17602 1. as will be manifest by the sub-

sequent proof.

se dinor and adapt be.

I. 100 . 108 :: 2500 . 2700

Subtract the first payment 754 \(\frac{14.17}{17002} \)

II. 100 . 108 :: 1945 \(\frac{3485}{17002} \)

Subtract the second payment 754 \(\frac{14.17}{17002} \)

1346 \(\frac{2.8}{170.2} \)

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Quest.39.

Mula, Asinaque duos imponit servulus utres
Impletos vino; segnemque ut vidit Asellam
Pondere desessam vestigia sigere tarda,
Mularogat; quid chara parens cunctare, gemisque?
Vnam ex utre tuo mensuram si mihi reddas,
Duplum oneris tunc ipsa feram; sed si tibi tradam
Vnam mensuram, sient aqualia utrique.
Pondera: mensuras dic docte Geometer istas?

The fense is this. A mule and an Ass carried two nnequal quantities of Wine, each consisting of a certain number of measures, in such sort, that if the Ass inparted one of her measures to the Mule, then the Mules number of measures so increased would be the double of those which the Ass had remaining; but if the Mule gave one measure to the Ass, then the Asses measures with that increase would be equal to the Mules remaining measures. The question is, how many measures each carried?

Answer, the Mule 7, and the Ass.

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Quest.

Queft, 40.

Æs, ferrum, stannum miscens, aurique metallum, Sexaginta minas pensantem singe coronam.
Æs aurumque duos simul efficiunto trientes.
Ternos gnadrantes stanno mixtum impleat aurum.
At totidem quintas auri vis addita ferro,
Ergo age dic fulvi quantum tibi conjicis auri
Miscendum, dic quantum aris stannique requiras?
Dic quoque sufficiant duri quot pondera ferri.
Prescriptam utvaleas rite efformare coronam.

The sense is this, Suppose a Crown that shall weigh 60 lb. is to be made of Gold, Brass, Iron, and Tin mixed together in such proportion that the weight of the Gold and of the Brass together may be 40 lb. the joynt weight of the Gold and of the Tin 45 lb. and the joynt weight of the Gold and of the Iron 36 lb. The question is how much of every one of those four metals must be taken?

Answer,
$$\begin{cases} 30\frac{1}{2} & \text{of Gold.} \\ 9\frac{1}{2} & \text{of Brass.} \\ 5\frac{1}{2} & \text{of Iron.} \\ 14\frac{1}{2} & \text{of Tin.} \end{cases}$$

Leeft. 41. One being demanded what was the present hour of the day, answered, that the time then past from noon was equal to of 3 of the time renaining until midnight. The question is, what a block it was? (supposing the time between noon and midnight

Chap. X. Questions 475 midnight to be divided into twelve equal parts or hours.)

Answer, 36 hour after noon.

Quest. 42. A Factor delivers 6 French Crowns and 2 Dollars for 45 shillings sterling; also at another time he delivers 9 French Crowns and 5 Dollars (at the same rate with the former) for 76 shillings. The question is to know the value of a French Crown, also of a Dollar?

Answer, A Crown was valued at 6 s. 1 d. and a

Dollar at 45.3 d.

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Quest. 43. A certain Usurer received 36 Dollars for the simple interest of 1861. Lent for a certain time unknown; also he received 50 Dollars for the gain of 3601, at the same rate of interest for a certain time unknown; now the sum of the moneths wherein both the said numbers of Dollars were gained was twenty moneths. The question is to know in what time as well the 36 Dollars as the 90 Dollars were gained?

Answer, The 36 Dollars were gained in 83 moneths, and the 90 Dollars in 113 moneths, as

may be proved by the Double Rule of Three.

Which answer may be discovered by the follow-

ing Canon found out by the Algebraick art.

Multiply the Dollars first gained, the latter Principal, and the given time, according to the rule of continual Multiplication, for a dividend; then multiply the first Principal by the Dollars last gained, also multiply the latter Principal by the Dollars first gained, and reserve the sum of these two last products for a Divisor; lastly, divide the Dividend first found, by the said Divisor, so shall the quotient be the time wherein the first number of Dollars

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was gained, which subtracted from the time given in the question discovers the time wherein the latter number of Dollars was gained.

$$36 * 360 * 20 = 259200$$

$$186 * 90, + 300 * 36, = 29700$$

· · 20-8 = 11 3 And confequently

Examples of the 2. 44. If 3481 Souldiers are Extradion to be placed in a square battel, how many are to be fet in rank or in

File ?

Answer, 59; (for the square root of 3481 is

59) Queft .45. If 4050 Souldiers are to be fet in battel in a figure, which beareth the form of a long fquare in fuch manner, that the number in File may be to the number in Rank as 1 to 2; how many Souldiers are to be placed in rank and how many In File?

Answer, 90 in rank and 45 in File (found by this

Canon or general rule) viz.

As the greater term of the proportion given is to the leffer, fo is the number of men to be placed in battel to a fourth proportional, whose square root is the leffer number fought (whether it be for the rank or File)alfo as the leffer term of the given proportion is to the greater; fo is the number of men to be fet in battel to a fourth proportional, whose square root is the greater number sought (whether it be for the rank or File.)

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I. | 2 . 1 :: 4050 . 2025 II. | /q . 2025 = 45 (men in File. III. | 1 . 2 :: 4050 . 8100 IV. | /q . 8100 = 90 (men in Rank.

The proof.

Or when one of the numbers fought (whether it be for the rank or File) is found, the other may be discovered by Division, viz.

Quest. 46. Suppose the wall of a Garrison to be in height 21 feet, and the breadth of the Moat surrounding the said wall to be 28 feet; the question is, what length must a scaling ladder have to reach from the outermost side of the Moat to the top of the Wall?

Answer, 35. (to wit, the square root of the sum of the squares of 21 and 28.)

$$21 \times 21 = 441$$
 $28 \times 28 = 784$

$$7q. 1225 = 35$$

Quest. 47. If 100 l. being put forth for interest at a certain rate, will at the end of two years be augmented

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augmented unto 112 36 l. (compound interest, or interest upon interest being computed) what principal and interest will be due at the first years end?

Answer, 1061. (composed of 1001 principal and 61. interest) which 106 is a mean Geometrically proportional between 100 and 112.36 (and may be found by the eighteenth rule of the fifth Chapter of this Appendix.)

100 × 112. 36 = 11236 (106

2xest. 48. If 1001 being put forth for interest at a certain rate, will at the end of three years be augmented unto 115, 76251. (compound interest being computed) what principal and interest will be due at the first years end?

Answer, 105 l. (composed of 100 l. Principal, and 5 l. interest.) which 105 is the first of two mean proportional numbers between 100 and 115.

7625 l. (See the nineteenth rule of the fifth Chap-

ter of this Appandix) a then dignel hider, al no

Various Practical Questions to exercise Decimal Arithmetick, in the mensuration of Superficial Figures and Solids.

See the second Section of the 23 chapter of the preceding Book. Quest. 49. If the side of a square Superficies be 3 feet, what is the Area or content of that Superficies? Or (which is the same thing) how many squares, each of which is a soot

square, are contained in that Superficies?

Answer,

Answer, o square feet, which content is found out by multiplying the given side 3 by it felf, viz. 3 multiplied by 3 produceth o.

In like manner, if the fide of a square pavement of stone be 15.7 feet, the superficial content of that pavement will be 246.49 feet, that is 246 feet and an half very near, (for 15.7 multiplied by it

felf produceth 246. 49.)

Likewife, a fquare piece of Wainscot whose side is 3. 24 yards, will be found to contain 10. 49 t yards, or 10 yards and an half almost; for, 3.24 multiplyed by it self, to wit, by 3.24 will produce

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Also if the side of a square piece of Land be 37. 25 perches, the content in square perches (neglecting the fraction in the product) will be sound 1387, which being reduced (according to the seventh Tables in Rule 4, chapter 7. of the preceding book) will give 8 acres, 2 roods, and 27 perches for the content of that square piece of land.

Queft. 50. If a long square be 8 feet in length, and 5 feet in breadth, what is the superficial con-

tent ?

Answer, 40 feet; which content is found out by multiplying the length by the breadth, viz. 8 multiplyed by 5 produceth 40. So if one of the lights of a glass window supposed to be in the form of a long square, hath for its length 3.06 feet, and breadth 1.47 feet, the content of that glass will be 4.4982 feet, or 4 feet and an half almost, (for 3.06 multiplyed by 1.47 produceth 4.4982.)

In like manner if there be a piece of Wainscot, Plaistring, or any other superficies in the form of

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a long square, which is in length 6. 325 yards, and in breadth 3. 214 yards, the superficial content will be found 20. 32 t yards, that is 20 yards, one quarter of a yard, and somewhat more, for, 6. 325 multiplyed by 3.214 produceth 20. 32 t.

Likewise a piece of Tiling in the form of a long square whose length is 18. 5 seet, and breadth 11. 7 seet will be sound to contain 216. 45 square feet, which will be reduced to 2.1645 squares of Tiling, by allowing (according to custom) 100

fquare feet to one square of Tiling.

Also if a piece of land in the form of a long square be 48.75 perches in length, and 36.25 in breadth, the area or content in perches will be sound 1767. 18 t which 1767 perches being reduced will give 11 acres and 7 perches for the content of that piece of ground.

Quest. 51. If it be required to set forth in a Meadow one acre of grass to ly in the fashion of a long square, and that the length thereof be limited or agreed to be 20 perches, what must the

breadth be ?

Answer, 8 perches which breadth is found out by dividing 160 (the number of square perches contained in an acre) by the given length 20. If two acres were required, then 320 (to wit, twice 160) must be divided by the given side, whether it be the length or breadth; so if 7. 25 perches be prescribed for the breadth of two acres, the length must be 44. 13 + perches.

In like manner, if the breadth of a Board be 1. 32 foot, and it be demanded how far one ought to measure along the side thereof to have a superficial foot, or a soot square of that Board: divide

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dix. by the given breadth, fo you will find in the quotiene this decimal fraction . 757 + which reprefents three quarters of a foot or nine inches and somewhat more, and so much in length ought to be measured along the side of that Board to make a fuperficial foot. Likewise if the breadth of a board be given in inches, then 144 (the number of square inches contained in a Superficial foot square) being divided by the given breadth, the quotient will shew how many inches ought to be measured along the side of that board to make a superficial foot; so the breadth of a board being o inches, the length forward to make a superficial foot will be found 16 inches.

Quelt. 52. If the three fides of a piece of land that lyes in the form of a triangle be 15 perches. 14 perches, and 13 perches, what is the area or number of square perches contained in that trian-

gle ?

Answ. 84 perches, or half an acre and four perches, which content is found out by this Rule,

viz.

From half the fum of the three fides of any plane triangle, fubtract each of the three fides feverally, and note the three remainders, then multiply the faid half fum and those three remainders one into the other, (according to the rule of continual Multiplication :) that done, extract the square root of the last product, fo shall fuch square root be the area or content of the triangle.

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Perches
The 3 fides of a triangle
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historia. The state of the order of a
The fum of the 3 fides 42
The half of that fum 21
The 3 remainders found out by sub- 5 tracting each side from the half sum-
The product arising from the conti
The square root of which product is 84
Another Example,
Perches
2010 A 41 1 76 Hea Dan 11 21 Hes 800 124 (120 1)
The 3 sides of a triangle
The fam of the 3 lides 328 . 4
The half of that fum
The 3 remainders found by subtra. 241 · 2 ding each side from the half sum 49 · 1
The product arising from the continual multiplication 223 355380. 1096 of the four last numbers
The square root of that product -4832. 7 + Wherefore
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Wherefore I conclude that the content of a plane triangle whose three sides are 120.5 perches : 1126 perches, and 90.3 perches, is 4832.7 + perches, which reduced give 30 acres and 32 perches (the fraction of a perch being neglected.)

Now foralmuch as every irregular piece of ground may be divided into triangles, for a fourfided field will be divided into two triangles by one imaginary straight line feading overthwart from corner to corner called a Diagonal line, a five-fided field into three triangles by two Dingo. wals a fix fided ground into four Triangles by three Diagonals, &c. the rule before given will be of excellent use to find out the Contents of large fields, especially if the land be of a dear value, as alfo when any controversie ariseth by reason of the different admeasurements of Surveyors of land : for if the lides of those Triangles be meafured in the field, and their lengths be agreed on, all Artifts to whom the reason of the rule before given is known, will agree in one and the fame contenr. But yet this way of measuring presupposeth that there is no obstacle, as Water, Wood, or other impediment, to hinder the measuring of the fides of those Triangles into which the field is dis vided as aforefaid.

Queft. 53. If the diameter of a Circle be 28,25.

what is the circumference?

Answer, 88.749 + : for as 113 is in proportion to 355's or as 1 is to 3.14159, fo is the diameter to the circumference : Therefore multiplying alwayes the diameter given by the faid 3.14159 the product shall be the circumference required.

Queft. 54. If the diameter of a Circle be 28.25 whar

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what is the superficial content of that Circle?

Answer, 626.79 +: for as 1 is in proportion to.78539, so is the square of the diameter to the superficial content. Therefore multiplying alwaies the said decimal fraction .78539 by the square of the given diameter (which square is the product of the multiplication of the diameter by it self) the product thall be the superficial content required.

Queft. 55. If the diameter of a Circle be 28.25, what is the fide of a square which may be inscri-

bed within the same Circle?

Anjwer, 19.975 + for the square root of half the square of the diameter, or the square root of the double of the square of the semidiameter, shall be the side of the inscribed square sought. Otherwise, 25 1 is to 707106, so is the diameter to the side required. Therefore if you multiply (alwayes) the said 707106, by the diameter given, the product will be the side of the inscribed square required.

Queft. 56. If the circumference of a Circle be

88. 75 what is the diameter ?

Answer, 28. 240 t for as 355 is to 113, or as 1 is to .318309, so is the circumference to the Diameter. Therefore if .318309 be multiplied alwayes by the given circumference, the product shall be the diameter required.

Queft. 57. If the circumference of a Circle be 88. 75 what is the superficial content of that Cir-

cle

Answer, 626.801 t for as 1 is to .079578, so is the square of the circumference to the superficial content Therefore if .079578 be alwayes multiplyed by the square of the given circumference, the product shall be the superficial content sought.

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Quest. 58. If the circumference of a Circle be 88.75, what is the side of a square that may be inscribed within the same Circle?

Answer, 19.975 + for as 1 is to .225078, so is the circumference to the side required. Therefore if .225078 be alwayes multiplied by the circumference given, the product will be the side of the inferibed square sought.

Queft. 59. If the superficial content of a Circle

be 616.8, what is the diameter?

Answer, 28.25 + for as 1 is to 1.27324, so is the content to the square of the diameter. Therefore multiplying alwayes 1.27324 by the given content, the square root of that product shall be the diameter required.

Quest. 60. If the superficial content of a circle

be 626.8, what is the circumference?

Answer, 88.75 + for as 1 is to 12.5664, so is the content to the square of the circumference. Therefore if 12.5664 be alwayes multiplied by the given content, the square root of the product shall be the circumference required.

Queft. 61. If the superficial content of a Circle be 626.8, what is the side of a square equal to the

fame Circle?

Answer, 25.035 + for the square root of the gi-

ven content is the fide of the square required.

Quest. 62. If the side of a Cube be 12 inches, how many cubical inches are contained in that Cube?

Answer, 1728. What a Cube is may be well represented by a Dye, which is a little cube it self, being a rectangular or square solid that hath an equal length, breadth, and depth, and is compreli

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hended under six equal squares; now if the side of one of those equal squares (which is also the side of the Cube) be 12 inches, the superficial content of that square will be 144 square inches, (for according to the preceding 49th question, 12 multiplied by 12 produceth 144) which multiplied by the depth 12 inches, produceth 1728 cubical inches, and such is the solid content of that Cube whose side is 12 inches: so that by one foot of timber or stone in whatsoever kind of solid it be sound, is understood a Cube, containing 1728 cubical or dye-square inches, and consequently half a soot solid contains 864 cubick inches, and a quarter of a foot solid contains 432 cubick inches.

In like manner, if the side of a Cube of stone be 2.53 feet, the solid content of that Cube will be found 16.194 + feet, for 2.53 being multiplied by it felf produceth 6.4009 superficial feet, which product being multiplied by the said 2.53 will pro-

duce 16.194 + folid feet.

Also if the side of a Cube of stone or wood be 6 inches, or .5 foot, the solid content will be found 216 cubick inches, or .125 parts of a foot solid (for 6 multiplied cubically produceth 216, likewise .5 multiplied cubically produceth .125) whence it may be infered, that 8 little cubes of stone or wood, each of which is balf a foot or 6 inches square, are contained in a foot of stone or timber; for 8 times 216 produceth 1728, (being the number of cubick inches contained in a foot solid) likewise 8 times .125 produceth 1, (to wit, one entire foot solid.)

Quest. 63. If the breadth of a squared piece of timber, supposed to be straight and terminated at both

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both ends by two equal squares, be 1.55 foot, the depth also 1.55 foot, and the length 17.33 feet, how many cubick feet are contained in that piece of timber?

Answer, 41.635 feet, that is, 41 feet and an half, and about half a quarter of a foot. Which folid content is found out by this rule wiz. multiply the breadth 1.55 by the depth 1.55 the product will be 214025 superficial feet, which is the content of the Base, (that is, the Area of either of the two equal squares at the ends of the piece) lastly multiplying the said Base 2.4025 by the length 17.33 the product will be 41 635 t, which is the solid content required.

In like manner if the breadth of a squared piece of timber, supposed to be straight and terminated at both ends by two equal long squares, (which are called the Bases) be 2.34 feet, the depth 1.61 foot, and the length 17.58 feet, the solid content will be 66.23 † feet; for (as before) multiplying the breadth by the depth, and that product by the length, the last product shall be the solid content

required.

2 ueft. 64. If the breadth, as also the depth of a fquared piece of timber having equal square bases, be 1.55 foot, how far ought one to measure along the length of that piece of timber to make a foot

folid ?

Answer, .416 parts of a foot, or 5 inches very near; which decimal is thus found, viz. First find the superficial content of the base, which will be 2.4025: (for, 1.55 multiplied by 1.55 produceth 2.4025.) Then dividing 1, (to wit 1 solid foot) by the Base 2.4025 the quotient will be .416 +

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or 416 parts of a foot, or five inches almost, and so far ought to be measured along the length of the piece to make a foot solid. In like manner, if the breadth be 2.34 feet, and the depth 1.61 feet, the length forward along the piece to make one solid foot will be found .265 parts of a foot, or three inches and almost 1 part of an inch.

Quest. 65. If a straight squared piece of timber be terminated by unequal Bases, whereof one contains 1.92 superficial foot, the other .85 soot, and the length of that piece of timber be 17.4 feet, what is the solid content, or how many Cubical feet are contained in that piece of timber?

Answer, 23.474 + feet, (found out by one of Mr. Oughtreds Rules for measuring a segment of a Pyramid in Problem 21. Chapter 19. of his Clavis Mathemat.) The Rule is this.

Multiply the greater Base by the lesse, and extract the square root of that product, then multiply the sum of the two Bases and that square root by one third part of the length of the solid propounded, so shall the last product be the solid content required.

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Example.

Quest. 66. A Pyramid is a folid comprehended under plane surfaces, and from a triangular, quadrangular, or any multangular Base, diminisheth equally lesse and lesse till it finish in a point at the top; now if the superficial content of the Base of a Pyramid be 5.756 feet, and the height thereof. 14.25 feet, (which height is the length of the perpendicular line that falleth from the top of the Pyramid to the Base) what is the solid content of that Pyramid?

Answer, 27.341 + feet: for if the Area of the Base of a Pyramid, be multiplied by one third part of the height thereof, the product shall be the solid content of the Pyramid; therefore 5.756 × 4.75 = 27.341 feet = the solidity of the Pyramid pro-

pounded.

Note, If a Pyramid be cut into two segments by a Plane parallel to the Base, one of those segments will be a Pyramid, and the other will have two unequal Bases, for the measuring of which latter seg-

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ment, a rule hath been already given in the fixty fifth question, the Area of each Base being known.

Quest 67. A Cone is a solid, which hath a Circle for its Base, from whence it grows equally lesse and lesse (like a round Steeple of a Church) till it finish in a point at the top; now if the Area of the Base of a Cone be \$1.756 feet, and the height thereof be 14.25 feet, what is the solid content of that Cone?

Answer, 27.344 feet: for if the Area of the Base of a Cone be multiplied by one third part of the height thereof, the product shall be the solid con-

tent of the Cone.

Note, If a Cone be cut into two fegments by a Plane parallel to the Base, one of those segments will be a Cone, and the other segment will have two unequal Bases which are Circles, the solidity of which latter segment may be found out by the rule before given in the 65 question, the Area of each Base (or circle) being known.

Quest. 68. A Cylinder is a solid which may be well represented by a Stone roll, such as are used in Gardens for the rolling of Walks. Now if the circumference of a Cylinder be 4.57 feet, and the length 3.25 feet, what is the folid content of that

Cylinder?

Answer, 5.4 feet, thus found out: First by the help of the given circumference 4.57, find out the superficial content of that Circle, (being the Base of the Cylinder) which content (by the preceding 57th question) will be found 1.6619 t foot, then multiplying the said 1.6619 by the given length 3.25, the product will be 5.4008 which is the solid content required.

Queft.

estions. 49

Quest. 69. If the Base of a Cylinder be 1.6619 soot, how much in length of that Cylinder will make a foot solid?

Answer, .601 parts of a foot; For 1 (to wit, 1 folid foot) being divided by the base 1.6619, gives in the quotient the decimal .601 + for the length

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Quest. 70. A Globe is a perfect round body contained under one Planesin the middle of the Globe there is a point called the Center, from whence all straight lines drawn to the outside are of equal length, and called Semidiameters, the double of any one of which is equal to the Diameter of the Globe; now if the Diameter of a Globe of Stone be 1.75 feet, how many feet folid are contained in

that Globe?

Answer, 2.807 + seet, for as 21 is in proportion to 11, or as 1 is to .5238, so is the Cube of the Diameter to the solid content of the Globe: Therefore, multiplying alwayes the Cube of the Diameter by the said decimal .5238, the product shall be the solid content required: So the Diameter 1.75 being first multiplied by it self, the product will be 3.0625, which multiplied by the said 1.75, gives in the product 5.359375, to wit, the cube of the diameter, which being multiplied by .5238, the product thence arising will be 2.807 +, which is the solidity of the Globe propounded.

Queft. 71. What is the Diameter of a Glabe of

ftone which contains 4 cubical or solid feet?

Answer, 1.96 + foot, for as 11 is in proportion
to 21, or as 1 is to 1,9090909 so is 4 (the solid
content given) to a fourth proportional, to wir,
7.636363 + whose cubick root is 1.96 + the diameter required.

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Concerning the gaging of Vessels.

The easiest and aptest wayes for practice in gaging, are those which are performed by the help of Tables, or Gaging rods purposely composed: Nevertheless to give the Reader of this Treatise some light in this matter, I shall here insert one rule to find out the number of Gallons contained in a full Tun, Pipe, Hogshead, Barrel, or such like vessel, according to Mr. Wing ate's way of reducing

a Vessel to a Cylinder. The Rule is this ;

Having found the difference of the two diameters at the bongue and head of the Veffel, take 7 of that difference and add it to the leffer diameter; then square that fum and referve the product ; that done, if the content be required in Wine gallons, multiply the product referved, this decimal fraction .0034, and the length of the veffel, one into the other, (according to the Rule of continual Multiplication) fo shall the last product be the number of Wine gallons required : but if the content be required in Ale gallons, multiply the product before referved, this decimal fraction .0027, and the length of the veffel, one into the other continually, fo shall the product be the content in Ale gallons . This Rule I shall first explain by two queflions, and then flew how it is raifed.

Queft. 72. If the diameter at the bongue of a reflet be 32 inches, the diameter at the head 28.2 inches, and the length 39 inches, (which dimensions

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are faid to agree very near with those of an English vessel called a Pipe) what is the content of that

vessel in Wine gallons?

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Answer, 126.278 Wine gallons, that is 126 Wine gallons and about a quart more (found out by the rule above given, as will be manifest by the following operation.)

Explication.

The Diameter at the bongue --- 32 . 0 The diameter at the head ______ 28 . 2 Their difference-Which multiplied by -7, that is, - 0 . 7 The product will be _____ 2 . 66 Which added to the leffer diame- 30 . 86 ter gives the mean diameter-Which mean diameter being fquared (that is, multiplied by it 952. 3396 felf) produceth ----Which product multiplied by -- 0.0034 The product thence arising will be- 3.2379t Which multiplied by the length of 39.0 the veffel -The product is the number of 126.278+ Wine gallons fought, viz. -

Queft.73. If the diameter at the bongue of a barrel be 23 inches, the diameter at the head 19.9 inches, and the length 27.4 inches ; what is the content of that barrel in Ale gallons?

Auswer, 36.031 Alegallons, that is 36 Gallons and about a quarter of a Pint more (found out by

the preceding Rule.)

Explication

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Explication.

BUILD OFFICE STONE OF THE STONE OF STONE STONE STONE
The diameter at the bongue23 . 0
The diameter at the head 19 . 9
Their difference 3 . I
Which multiplied by 7 that is - 0 . 7
The product will be 2. 17
Which added to the leffer diame-
ter gives the mean diameter
Which mean diameter being)
Which mean diameter belog) fquared (that is, multiplied by it \ 487.0849
felf) produceth
Which product multiplied by 0.0027
The product thence arising is 1,315 t
Which multiplied by the length?
of the vessel
Ale gallons fought to min and 36.031 t
Ale gallons fought, to wit

The reason of the Rule.

Two things are taken for granted in the faid Rule, viz. First, it is supposed that if - of the difference of the two diameters at the bongue and head, be added to the lesser diameter, the sum shall he an equated or mean diameter, (near enough for practical use though it be not exact) viz. It there be a Cylinder whose diameter is equal to that mean diameter, and whose length is equal to the length of the vessel, that Cylinder shall be equal to the capacity of the vessel very near. Secondly,

the

the faid Rule presupposeth that 221 cubick inches are equal to a Wine gallon, and 282 equal co an Ale gallon; concerning which equalities (efpecially the latter) Artifts differ somewhat in their experiments; but according to any equality which in that particular shall be agreed on, from this that follows a rule may be framed, and Tables thence calculated for gaging a full vessel without considerable error.

Taking then those two things above mentioned for granted, we may rightly infer that if a Cylinder hath for its Base a Circle whose superficial content is 231 inches, every inch in length of that Cylinder will contain 231 cubick inches, or one intire Wine gallon; Now forasmuch as all Circles are in fuch proportion one to the other as the squares of their diameters, it shall be as 294.11844, (to wit, the fourre of the diameter of that Circle whose superficial content is 231) is to 1; (to wit. the superficial content 231 considered as the Base of one Winegallon) or as 1 is to .0014 : So is the Square of the equated (or any other) diameter, to the superficial concent of that Circle in Wine gallons and parts of a gallon, which content multiplied by the length of the veffel will produce its folidity or capacity in Wine gallons: Therefore the first part of the preceding rule for finding of the number of Wine gallons contained in a full vessel is manifest : And after the same manner, suppoling as before 282 cubick inches are equal to an Ale gallon, the decimal .0027 prescribed in the faid rule will be found out.

Upon those grounds Mr. Wingate compos'd his Gaging rod; Mr. Onghtred also in his Circles of Proportion

ber

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Proportion hath delivered another rule for Gaging, from whence his Gaging rod is deduced; but the particular confiructions of those rods, and likewise the making of Tables for the same purpose, being handled by several Artists, I shall not

infift upon them.

Now if the industrious and more curious Arithmetician, after he is well exercis'd in vulgar Arithmetick, desires further knowledge in finding out the Answers of subtle Questions about numbers, his best Guide will be the admirable Algebraical Art, which discovers rules for the solving of Problems, as well Arithmetical as Geometrical, that are above the reach of any of the rules of common Arithmetick, or practical Geometry, as may partly appear by the two rules in the aforegoing 52 and 65 Questions, as also by the two following Questions, with which I shall conclude this chapter.

Quest. 74. To find two numbers in a given proportion, suppose the lesser to the greater as 2 to 3, and such, that if the lesser number be added to the square of the greater, also if the greater number be added to the square of the lesser, the two sums shall be square numbers whose roots are expressible by rational or true numbers: (fractions being admit-

ted for numbers.)

Answer, 1 and 3.

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The proof. The square of 10 (the greater num- 3 ber) is-To which adding the leffer number-The fum in its least terms will be-Which is a square number whose ? root is-Again, the fquare of the leffer} number) is ---To which adding the greater num-3 The fum in its leaft terms will be-

Which is a square number whose

Alfo the faid numbers - and are one to the other as 2 to 3, wherefore the question is folved. Which numbers -1 and 3 are found out by this following

Theoreme.

If the fraction & be divided into any two parts . either of those parts being increased with the fquare of the other part shall give a fraction having a rational fquare root.

Wherefore by dividing into the two fractions and 3, which are in the prescribed proportion of 2 to 3, those fractions will fatisfie the conditi-

ons in the question propounded.

Likewise these two fractions 722 and 1083 will answer the question, and are found out without extracting any root; but the manner of finding out the faid Theorem and last mentioned fractions. Ihave shewn in the 24th question of my third book of the Elements of Algebra.

Appendix.

Queft. 75. To find three numbers, fuch that the fquare of any one of them being added to the other two numbers, the fum of fuch addition shall be a square number, whose root is a rational num-

Answer, 1, 8, and 16. The proof. First, the fquare of the first number Lain A To which adding the fecond and? 6 of third numbers 3 and 16, the fum will be-Which is a square number whose ! root is-Secondly, the fquare of the fecond i number 8 is-To which adding the first and third ? numbers 1 and 10, the fum in its least terms will be-Which is a square number whose t Thirdly, the square of the third num- 2 256 ber 16 is To which adding the first and second? numbers I and the fum in its leaft 229 terms will be-Which is a square number whose

root is Wherefore it is manifest that the three numbers 1. 15 and 16 will fatishe the conditions in the que-Rion, which may be folved also by other numbers, but the manner of finding them out I have thewn in the 32th Question of my third Book of the Elements CHAP. of Algebra.

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CHAP. XI.

Of Sports and Pastimes.

Probl. I.

To discover a number which any one shall have in his mind, without requiring him to reveal any part of that or any number what soever.

A Fter any one hath thought upon a number at pleasure, bid him double it, and to that double bid him add any such even number which you please to assign, then from the sum of that addition let him reject one half, and reserve the other half: Lassly, from this half bid him to subtract the number which he first thought upon; then may you boldly tell him what number remaineth in his mind after that subtraction is made, for it will alwayes be half the number which you assigned him to add.

For example, suppose he thought upon 6, the double thereof is 12, to which bid him add some even number at your pleasure, suppose 4, so will the sum be 16, whereof the half is 8, from which if he subtract 6, (the number first thought on) the remainder is 2, (to wit, half the number 4, which was by you assigned to be added) which remainder you discover, notwithstanding all the operation was performed in his mind, without his making known of any number whatsoever. Note that the adding of an even number as aforesaid is not of necessity, but only to avoid a fraction which will arise by talking the half of an odd number.

The reason of the Rule.

If to the double of any number (which number for diffinction fake I call the first) a second number be added, the half of the sum must necessarily confist of the said first number, and half the second; therefore if from the said half sum the first number be subtracted, the remainder must of necessity be half of the second number which was added.

II. Ploor a anumber se

Two numbers, the one even and the other odd, being propounded unto two persons, to the end they may (out of jour sight) severally chuse one of those numbers; to discover which of these numbers each person shall have chosen.

Suppose you have propounded unto Peter and John two numbers, the one even and the other odd, as 10 and 9, and that each of those persons is to chuse one of the said numbers unknown to you. Now to discover which number each person shall have chosen, you must take two numbers, the one even and the other odd, as 2 and 3; then bid Peter multiply that number which he shall have chosen; by 2; and cause John to multiply that number which he shall have chosen by 3; that done, bid them add the two products together, and let them make known the sum to you, or else demand of them whether the said sum be even or odd, or by any other way more secret endeavour to discover it, by bidding them to take the half of the said sum,

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for by knowing whether the faid fum be even or odd, you do obtain the principal end to be aimed at, because if the said sum be an even number, then infallibly he that multiplied his number by your odd number (to wit, by 3) did chuse the even number, (to wit 10) but if the faid fum happen to be an odd number, then he whom you caused to multiply his number by your odd number, (to wir, by 3) did infallibly chuse the odd number, (to wit o.)

For example, if Peter had made choice of 10, and John 9, suppose you willed Peter to multiply his number 10 by 2, and John to mulciply his number 9 by 35 the products will be 20 and 27, whereof the fum is 47, which being an odd number, you may thence conclude that John whom you caused to multiply his number by 3 did chuse the odd number 9, and therefore Peter did chuse 10. But if you had willed John to have multiplied his number o by 2, and Peter to have multiplied his number 10 by 3, the products would have been 18 and 30, whereof the fum is 48, which is an even number, from whence you may infer that he that multiplied his number by 3 did chuse the even number, and therefore Peter had chose 10, and John 9.

Demonftration.

The reason of the said rule is very easie, and dependeth principally upon the 28 and 29 propositions of the oth book of Enclid; for one may infer from the 21 of the same book, that an even number multiplied by any number whatfoever produceth an even number, but an odd number is of a different nature for if it be multiplied by an even num-Kk ber

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ber the product is an even number (by the said 28 proposition) and if it be institutibled by an odd number the product is odd, (by the said 29 proposition). Therefore if in making this sport it happeneth that the even number be multiplied by your odd number, both the products shall be even, and confequently the sum shall be installibly an even number (by the said 21 proposition.) But if it happen that you cause the odd number to be multiplied by your odd number, that product will be odd, and the other product even, therefore the sum of these two products shall be an odd number, (as Clause hath demonstrated upon the 23. of the 9th of Exception)

Probl. 3.

A certain number of distinct things being propounded, to dispose them in such an order, that custony away alwayes the ninth, or the tenth, or any other that shall be assigned, anto a certain number, this eremaining may be such as were first intended to be left.

This Problem is usually propounded in this manner, viz fifteen Christians and fifteen Turk being at Sea in one and the same Ship in a terrible from, and the Pilot declaring a necessity of casting the one half of those persons into the Sea, that the restmight be saved, they all agreed that the persons to be cast away should be fet out by lot after this manner, viz. the thirty persons should be placed in a round form like a Ring, and then beginning to count at one of the Passengers, and proceeding circularly, every ninth person should be cast into the Sea, until of the thirty persons there

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doids Never will fame depart.

In which verses you are principally to observe the vowels, with their correspondent numbers before assigned, and then beginning with the Christians, the vowel of in from significant that four Christians are to be placed together; next unto them, the vowels (in min) significan that five Tarks are to be placed; In like manner of (in birs) denoteth 2 Christians, a (in with a (in wire) a Christians, of (in will) 3 Christians, a (in very a Christians, is (in will) 3 Tarks, a (in fame) a Christians, w (in part) a Tarks, of (in de) 2 Christians, w (in part) a Tarks.

The invention of the faid Rule and fuch like, dependeth upon the Jubsequent demonstration, viz. if the number of persons be thirty, let thirty figures or exphere be placed circularly, or else in a right line as you see,

That done, begin to count from the first, and

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mark the ninth (or what other shall be assigned) by putting a point or cross over it, then count forward from that which you have marked, and place another point over the next ninth, and continue to do the same, beginning again when you shall be at the end, if the cyphers are placed in a right line and passing over those, which you shall have already marked, until you have marked the number required, as in the example propounded, until you have marked fifteen, for then all the cyphers marked shall be those which shall remain. Hence it is evident, that if you observe how those cyphers which are marked, are disposed amongst those which are not marked, you will casily make a rule for any

number whatfoever is rear risch this

By this invention (as some do conjecture) the famous Historian Jofephus the few, preferved his life very subtilly, in the Cave to which himself and forty of his Countreymen had fled, from the furious and conquering Romans, at the Seige of forapata, for his laid Countrymen having most wickedly refolved to kill one another, rather then yield to their enemies, he at length (when no arguments that he could use would diffwade them from so horrid an act) prevailed with them to execute their tragical delign by lot, and fo by the help of the aforefaid artifice, (as we may suppose) himself with one other person only remaining alive, after the reft were inhumanely murthered, they agreed to put an end to the lot, and thereby fave their lives. This ftory you may fee at large in the fourteenth Chapter of the third book of the Hiftory of Tofephus of the Warrs of the fems, ... a niged sono and T

Probl.

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Probl. 4.

Many numbers which proceed from 1 or unity in a progression, according to the natural order of numbers, (such as these, 1,2.3,4,5,6, &c.) being placed in a round form like a Ring; to discover whith of those numbers any one shall have thought upon.

Let any multitude of numbers in the aforesaid progression, suppose these 10, to wit, 1.2.3.4.5.6. 7.8.9.10. be written upon 10 ivory counters (or for want thereof upon 10 small pieces of paper) which may be represented by these 10. letters, A. B. C. D. E. F. G. H. K. L. viz. suppose 1 to be written upon the counter A, 2 upon B, 3 upon C, &c. Then having placed those counters circularly as you see (with their blank faces uppermost, and the figures underneath, that the subtilty of the sport

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may the better be concealed) let any one think upon any number of unities which doth not exceed
to; that done, bid him touch one of those counters at pleasure, and to the number on the backside of the counter touched (which you cannot be
ignorant of, having noted well the place of 1 or
K k 3 A)

war nun In l bac fall

A.) add fecretly in your mind, the just number of all the counters, and reserve the sum; then bid him imagine in his mind the counter touched to be the number which he thought, and from that counter to count backwards, until he shall have made up the aforesaid sum, which you reserved, so will his computation infalliby end upon the counter upon which the number thought upon is written.

For example, suppose that he thought 7 or G, and that he touched B, to wit, 2. Add to 2 the number of all the counters, to wit, 10, so the sum will be 12, then bid him to count unto 12, beginning at B and going backwards, and esteeming B to be the number thought, to wit, 7, so will 8 fall upon A, 9 upon L, 10 upon K, 11 upon H, and lastly, 12 upon the counter G, which being turned up will shew 7 the

number thought.

The reason of this rule is not difficult to be apprehended, two principles being presupposed, the one is this, to wit, many counters or things whatfoever being disposed orderly one after the other, in one continued line, whether it be right or circular, if you value or name the first counter to be fome number of unities at pleasure, and continue to count forward according to the natural order of numbers, until another number be named which falleth upon the last counter; or if you imagine or name the last counter, to be the same number of unities as before you put upon the first, and continue to count backwards unto the first counter ; I fay, that the same number will be named at the end of both those computations : for example, in these o letters A.B.C.D.E.F.G. H.K. if the letter A be esteemed ter if for ter

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effeemed to be 4, and from thence you count forwards unto K, according to the natural order of numbers, the letter K will fall upon the number 12. In like manner, if you effeem K to be 4, and count backwards from K to A, the letter A will likewise fall upon 12.

4. 5: 6. 7. 8. 9. 10. 11. 12 A. B. C. D. E. F. G. H. X 12. 11. 10. 9. 8. 7. 6. 5. 4

The other principle is this, to wit, many counters being disposed in a round manner like a Ring, if you esteem any one of those counters to be some number at pleasure, and then from that counter if you count circularly, until you end upon the counter where you began, the number last named will be equal to the sum of the number of all the counters, and of the number which you put upon the first counter; for example; if D be one of 10 Letters placed in a circumference, and that imagining D to be 7, you begin with it, and count round the whole circumference, according to the natural progression of numbers, till

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K 9 3 C
H 8 4 D
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you end with D where you began; the number 17 which is composed of, 10 and 7 will necessarily fall upon D; for 9 (which is the number of letters in the circumference belides D) being added to 7 (which was first purupon D) makes io, to which i being added (because D doth end as well as begin the circumference) the fum is 17.

Now these two principles being presupposed, it will not be difficult to apprehend the reason of the aforesaid rule in all cases that can happen; for imagine that one hath thought upon 7, or the counter G. then that counter which he shall touch must either be the same counter G or some other

that precedeth or followeth G.

First therefore supposing the counter or number touched to be the fame with the number thought, the truth of the rule will be then evident, for by the rule given, he shall begin to count from the same G unto 17, putting 7 upon G, therefore by the second presupposition the number 17 will fall

upon G.

Secondly, imagine that he touched a counter or number following Gthe number thought, as L or 16. then according to the rule adding to. (the multitude of all the counters placed circularly) unto 10 or L, (the counter touched) bid him count backwards unto 20 by beginning at L and esteem L to be 7. Now because by beginning to count at Gwhich is 7, and proceeding to count forward, the number 10 will fall upon L, therefore by the first presupposed principle if we esteem L to be 7 and count backwards, the number to will infallibly fall upon G, and then the number 20 shall also fall upon the fame G by the fecond presupposed principle.

Laftly, imagine he touched some number or counter which precedeth 7 the number fought, as Bor 2; then adding 10 to 2, you are to bid him count unto 12, he having first imagined B to be the number thought 7, and going backwards to A, L. K,&c. Now because by proceeding to count at B. which is 2, and beginning to count forward to C. D, &c. the number 7 falleth upon G. Therefor eif one imagine that G is 2, and from thence count backwards towards F. E. &c. the number 7 will fall upon B, (by the first presupposed principle) therefore when one affumeth B to be 7, and counteth towards A.B &c. to any affigned number, it is in effect as much as when one imagineth G to be 2, and counteth towards F. E. &c. unto the faid affigned number, for each of those computations will end in the same point ; but it is manifest (by the second presupposed principle) that esteeming G to be 2. and counting towards F.E.D.&c. round the whole circumference, the number 12 will fall upon the fame G. And because G being supposed to be 2, and counting on the same coast as before, the number 7 falls upon B, therefore if the computation be continued on the same coast from B 7 unto 12, the number 12 will fall upon the same G. So that the practice of this sport in all its Cases is fully demonstrated.

Note, that to the number of the counter touched, you may not only add the number of all the counters once (as the Rule directs) but twice, thrice or more times: for example, B being touched, you may cause him to count unto 12, or unto 22, or to 32, 42. &c. the reason whereof is evident from the

fecond presupposed principle.

Probl.

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Many numbers being shomed by pairs, to vit, two by two, unto any one, that he may think upon any one of those pairs at pleasure; to discover the pair that was thought upon.

Let 20 numbers, suppose these, 1.2.3.4.5.6.7.
8.9.10.11.12.13.14.15.16.17.18.19.20. be written upon Ivory counters, (or for want thereof upon small pieces of paper) to wit, 1 upon one counter, 2 upon another, 3 upon a third, &c. Then dispose them into pairs as you see; with suppose 1 and 2 to be one pair, 3 and sour to be another

F 1.	2
3.	14
5.	6
7:	8
9.	10
13.	12
15.	16
17.	18
19.	20

pair, &c. and of these pairs let any one think upon which pair he pleaseth. That done, you are to distribute the said 20 numbers in ranks, in the form of a long square, until there he 5 numbers in length, and 4 in breadth, after this manner, viz.

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lay the three first numbers 1.2. and 3 in a rank (as you see in the second figure) from A towards B, then place 4 underneath 1, and 3 after 3 (in the said rank A B.) Again place 6 under 4, and 7 after 5 (in the said rank A B.) Then place 8 under 6, also 9.10. II on the right hand of 4 in the rank C D. Again place 12 under 9, and 13 on the right hand of 11 in the rank C D. and 14 under 12. Moreover place 15. 16. 17 on the right hand of 12 in the rank B F. Lastly, place 18. 19. 20 on the right hand of 14 in the rank G H, so will all the numbers be ranked, as you see in the Table. That done, you are to demand of him that thought upon two numbers as aforesaid, in what rank or ranks the said numbers do happen to be found, viz.

A	1	2	3	5	7	B
C	4	9	S. 13. 15. 15. 15.	11.	13	D
E	6	12	15	16	17	F
G	18	14	18	19	20	H

in which of the ranks AB, CD, EF, GH, or in which two of the faid ranks: now if he answer that the two numbers which he first thought upon are in the first rank AB, then 1 and 2 shall be the numbers thought upon 3 if in the second CD, then 9 and 10 shall be the numbers thought; if in the third rank EF, then 13 and 16 shall be the numbers thought; if they are in the fourth rank GH, then 19 and 20 shall be the numbers thought; but if he shall say, that the numbers thought are in different ranks, then you are heedfully to mark the said numbers 1 and 2, 9 and 10, 15 and 16, 19 and 20, which

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which may be called the keys of the fport, in ret gard they ferve not only to differer the two numbers thought, when they are both in one and the fame rank (as aforefaid) but alfo when they are in two different ranks, for in this latter cafe as foon as it hath been declared to you in which two ranks the two numbers thought are placed, you must take the key of the highest of those two ranks, and descending in a down-right line from the first number of that key unto the lower of the faid two ranks, you shall there find one of the two numbers thought, and upon the right hand of the fecond number of the faid key, at the fame diftance fidewife from the fecond number of the key, as one of the numbers thought was distant from the first number of the key, you shall find the other number thought.

For example, suppose the two numbers thought are 7 and 8, and that it shall be declared into you that they are in the first and fourth ranks, take then the key of the highest of these two ranks, to wit of the first, which is 1 and 2, and descending down-right from 1 unto the fourth rank, you shall there find 8 one of the numbers thought, then seek side-wise on the right hand of 2 (the second number of the key) a number as far separated from 2, as 8 is distant from 1, and you will find 7 the other

number thought.

Again, suppose the faith that the numbers thought are in the second and third ranks; take then the key of the second rank which is 9 and 10, and descending down right from 9 to the third rank, you shall there find 12 which is one of the numbers thought; then seek lidewise on the right

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hand of 10 (the second number of the key) a number as far distant from 10 as 12 is from 9; and you shall find 11 which is the other number thought.

The reason of this will be apparent from a serious consideration of the placing of the numbers according to the rules before given, for it is thereby evident that of the two numbers coupled two by two, there can never be found more then one pair in one and the same rank, and of all the other pairs one number is alwayes found in one rank, and the other number in another rank.

Note alfo, that this foort may be practiced with divers persons at once, and not only with 20 numbers , but with any fuch multitude of numbers which is produced by the multiplication of any two numbers which differ by 1 or unity; 29 30; which is the product of 5 multiplyed by 6, and 42 which is the product of the multiplication of 6 and 7. That which is chiefly to be regarded is the placing of the numbers in ranks according to the directions before given, and for the more eatie com. prehending of that order, I have in the following Table ranked 30 numbers in their due places, which being compared with the former Table, and well viewed, will be a clearer illustration than can be exprest by many words. loug of overe, which are

Eo. Jiz	2	1 3	15	7	9
4	11	12,	13	1315	17
6.	114	19	20	21	23
8	16	22	25	26	27
10	18	24	28	1 29	130

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Probl. 6. osl sei)

Three jealous husbands with their wives, being ready to pass by night over a river, do find at the river side a bout which can carry but two persons at once, and for want of a Bournanthey are necessitated to row them-selves over the river at the several times: the question is how these six persons shall pass two by two, so that none of the three wives may be sound in the company of one or of two men untess her husband be present.

They must pass in this manner, wit, First two women pass, then one of them bringeth back the boat and repasseth with the third woman; that done, one of the three women bringeth back the boat, and sitting down upon the ground with her hulband permitteth the other two men to pass over to find their wives; then one of the said men with his wife bringeth back the boat, and placing her upon the ground he taketh the other man and repasseth wich him; lastly, the woman which is found with the three men entreth into the boat, and at twite goeth to setch over the other two women.

Probl. 7.

Two merry companions are to have equal shares of & Gallons of wine, which are in a vessel containing exactly & Gallons, now to make this equal partition they have only two other empty vessels, whereof one containeth 5 Gallons, and the other 3, the question is how they shall exactly divide the wine by the help of those three vessels.

First, from the vessel which containeth 8 gallons and

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and is full of wine, let 5 gallons be poured into the empty veffel of 5, and from this veffel fo filled let 3 be poured into the empty vessel of three, so there will remain 2 gallons within the veffel of 5. Then let the three gallons which are within the veffel of 3 be poured into the veffel of 8, which will now have 6 gallons within it, that done, let the 2 gallons which are in the veffel of 5, be put into the empty vessel of 3, then of the 6 gallons of wine which are within the vessel of 8 fill again the five, and from those 5 pour out 1 gallon into the vessel of 3, which wanted only 1 gallon to fill it, fo there will remain exactly 4 gallons within the veffel of 5. and 4 gallons within the other two veffels. question may be resolved in another way, but I leave that as an exercise to the wit of the ingenious Reader.

Now albeit at first sight it may be thought by some, that the two last mentioned Problems cannot be resolved by any certain rule, but only by many trials, yet by infallible argumentation and discourse, the solution of those questions may be sound out or else the impossibility of them, if by chance they should have been propounded impossible; as the most ingenious Gasper Bachet hath manifested in a little Book in the French Tongue, intituled Problemes plaisans & delectables qui se sont par les nombres, from which Book I have extracted the

Contents of this Chapter.

Soli Deo Gloria.